

EE 459/611: Smart Grid Economics, Policy, and Engineering*

Lecture 1: Course Information and Overview

Dr. Luis Herrera
Dept. of Electrical Engineering
University at Buffalo

Fall 2020

Course Information

- **Instructor:** Luis Herrera
- **Contact Info:** 224 Davis Hall, lcherrer@buffalo.edu, 716 431-2832
- **Class Times:** Tu/Th 12:45 pm – 2:00 pm
- **Class Location:** Online/Zoom (Record)
- **Office Hours*:** TBA (will send email when decided)
- **TAs:** Lalit Marepalli
- **Website:** UBLearns blackboard (will upload blank notes prior to class), **please use them to follow along**

Course Information

- **Course Information:**

- ✓ This course provides an introduction to electric power markets and the mathematical techniques^{*} to better use available energy resources.

- ✓ Topics include the description of thermal power plants and renewable energy sources.

} Cost operation
→ \$/kW

- ✓ Formulation of the cost associated with generation will be presented.



- ✓ Optimization theory will be introduced with the aim of minimizing cost of supplying loads.



- ✓ Particular methods include economic dispatch, unit commitment, and optimal power flow.^{*}

Grading Policy

489/611

- **Homework (35%)**
 - Assigned approximately every two weeks
 - Most will use Matlab (may use CVX toolbox – instructions will be provided)
- **Quizzes (10%):** approximately 7-10, 20 mins quizzes on UBLearns
- **Midterm (25%):** Exam
- **Final Project (30%)**
Matlab

Course Materials

Textbook:

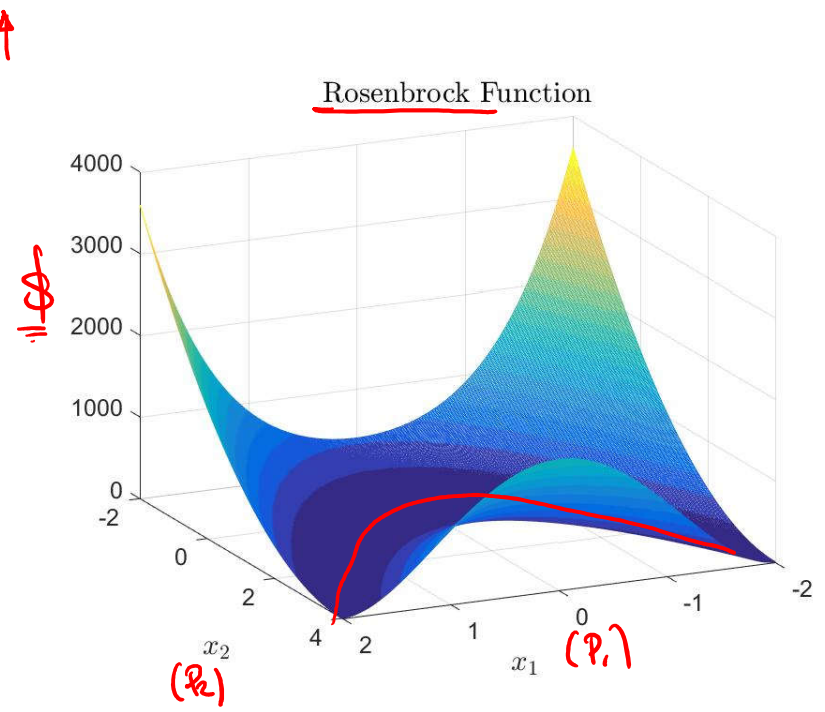
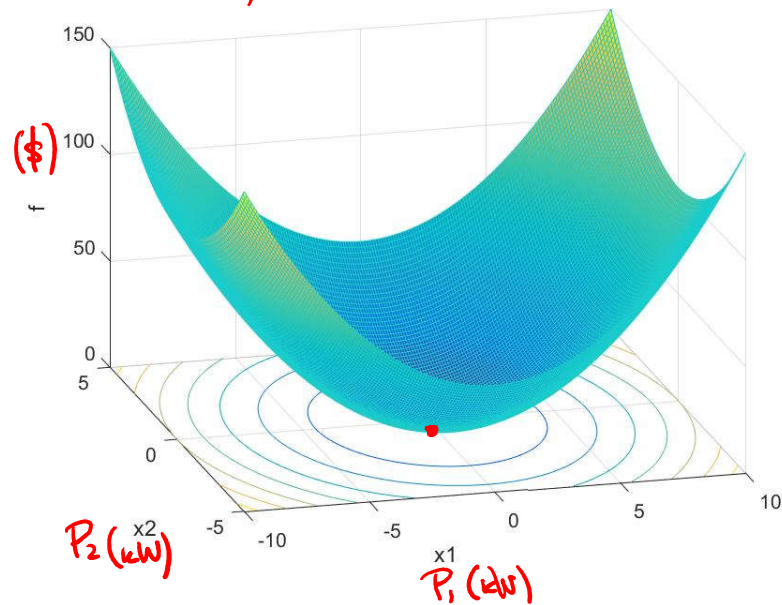
- A. Wood, B. Wollenberg, and G. Sheble, "Power generation, operation, and control." Wiley, 3rd Edition, 2013.
(Book not strictly required but it is a very good reference)

*○ Matlab + Optimization Toolbox

- Optional optimization software:

* CVX (convex optimization) <http://cvxr.com/cvx/>

$Cost = z = f(x_1, x_2)$ minimum



Tentative Topics

- **Power System Economics** (1-2 lectures)
 - Power generation terminal characteristics ($\$/\text{kW}$)
 - Cost of power generation
- **Mathematical Background:** (2-3 lectures)
 - Linear Algebra
 - Multivariable Calculus

-
- **Optimization Theory**
 - **Economic Dispatch**
 - **Unit Commitment**
 - **Optimal Power Flow**
 - **Other Topics**
 - State Estimation
 - Power electronics
 - Automatic Generation Control

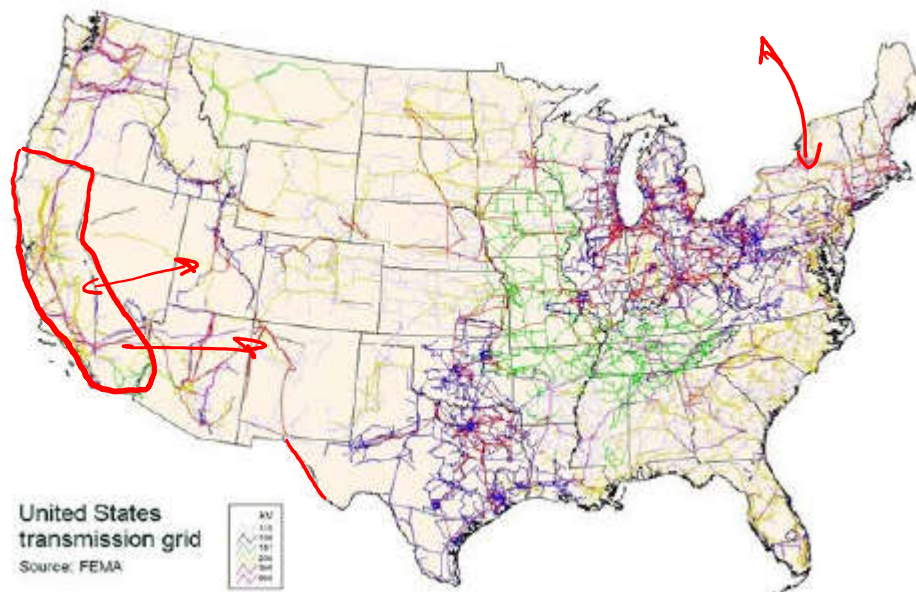
Today – 09/01/2020

- Today we will mainly look at an overview of the topics we will cover in class
- Motivation from power systems

Power Systems in US

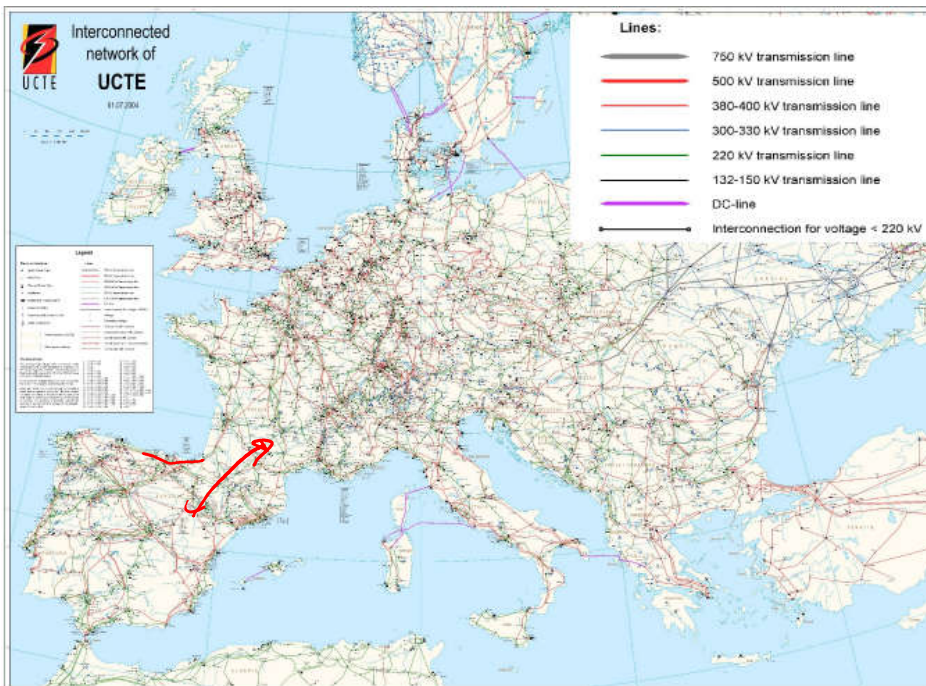
- Power system in the US: colors represent transmission line voltages

ISOs / RTOs

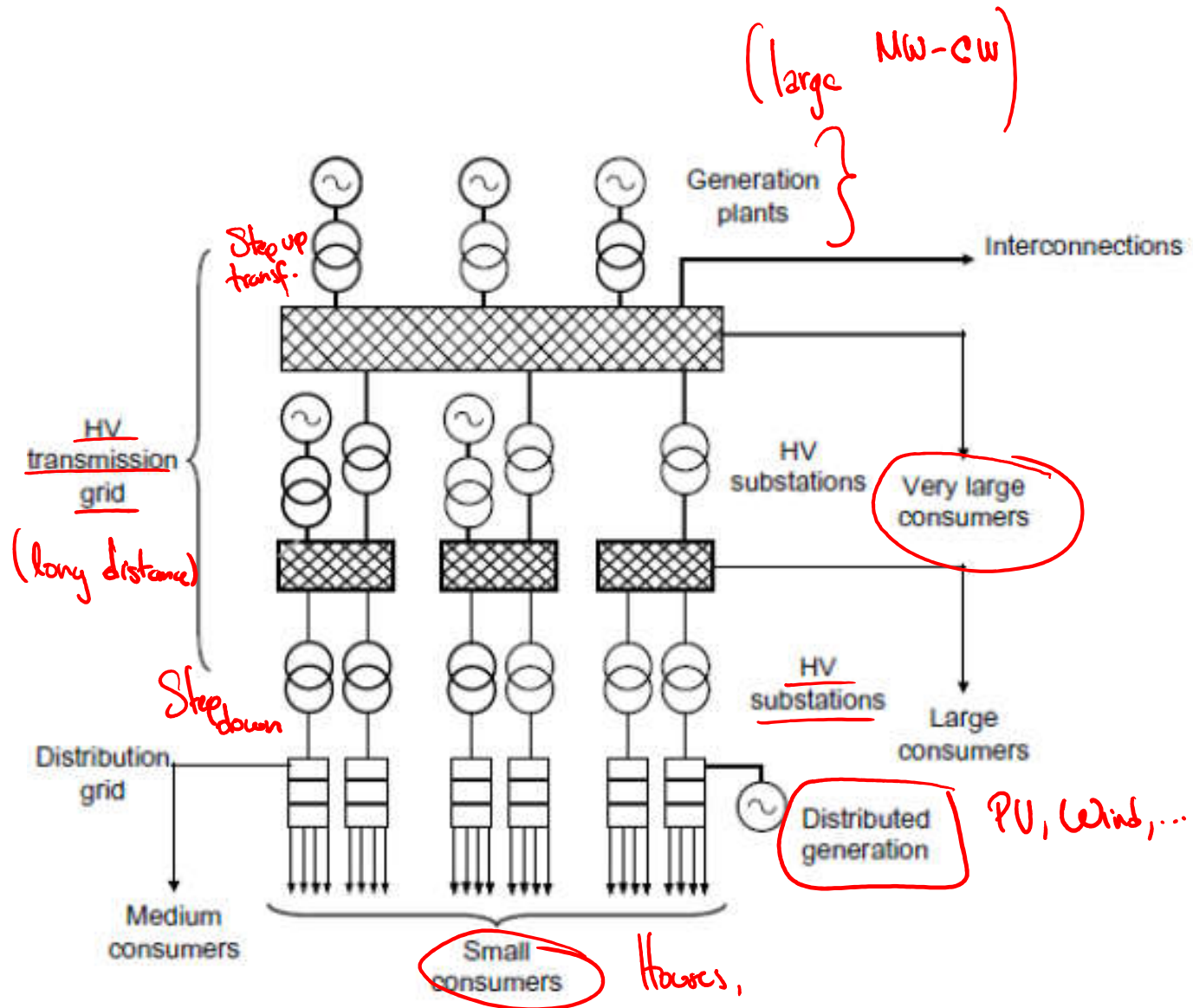


Power Systems in Europe

- Power system in the Europe: colors represent transmission line voltages



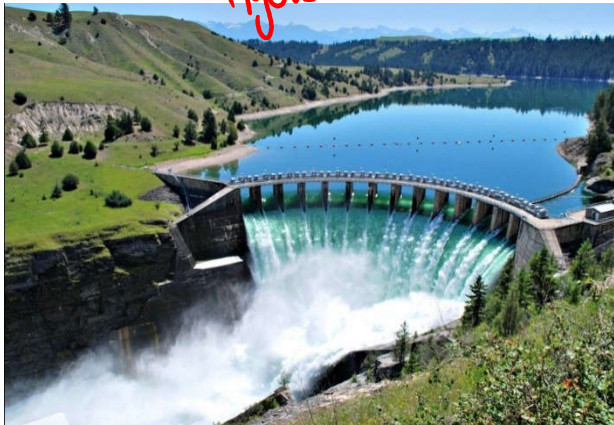
Power System Components



Example Energy Sources

Power output vs. Cost

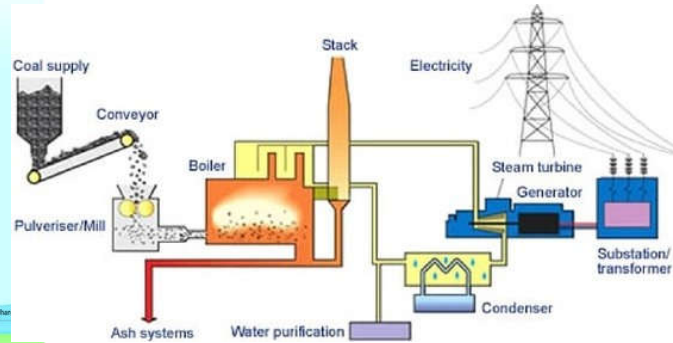
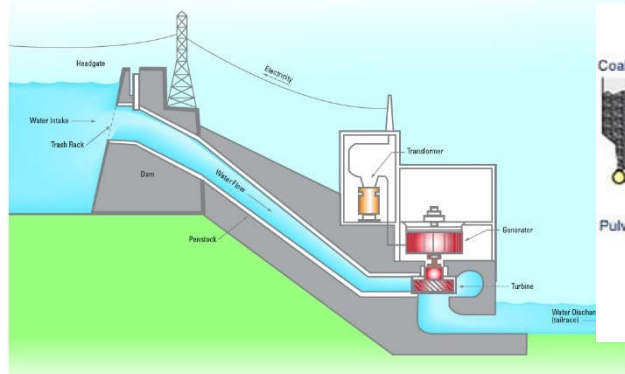
Hydro



Coal (Thermal)



Wind

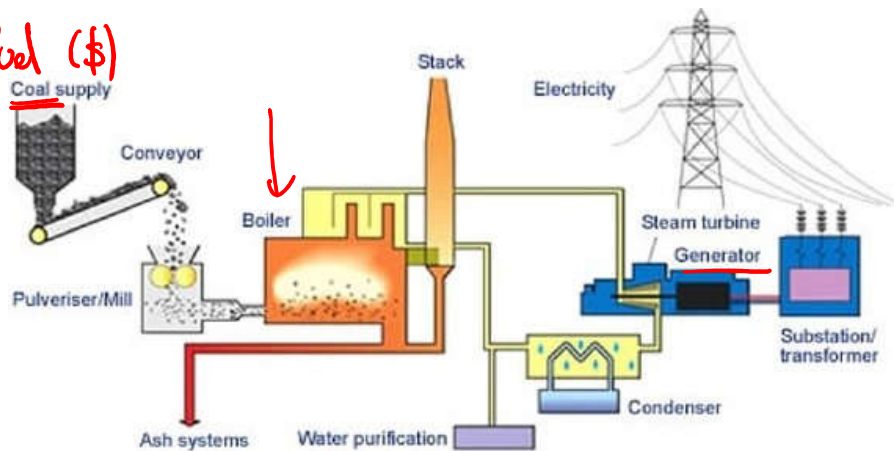


Solar

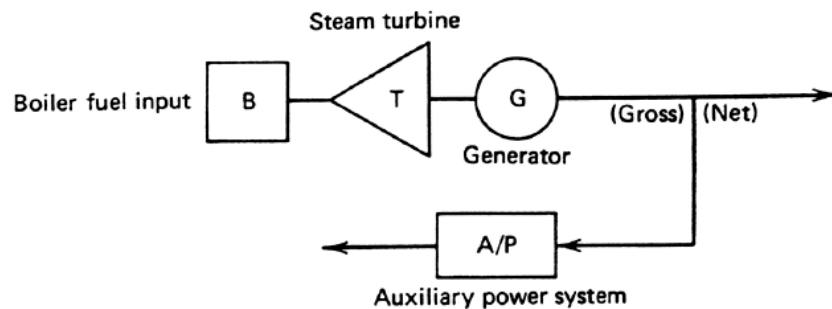
Cost Associated with Source Operation

- Cost associated with running a generation plant

Cost
fuel (\$)

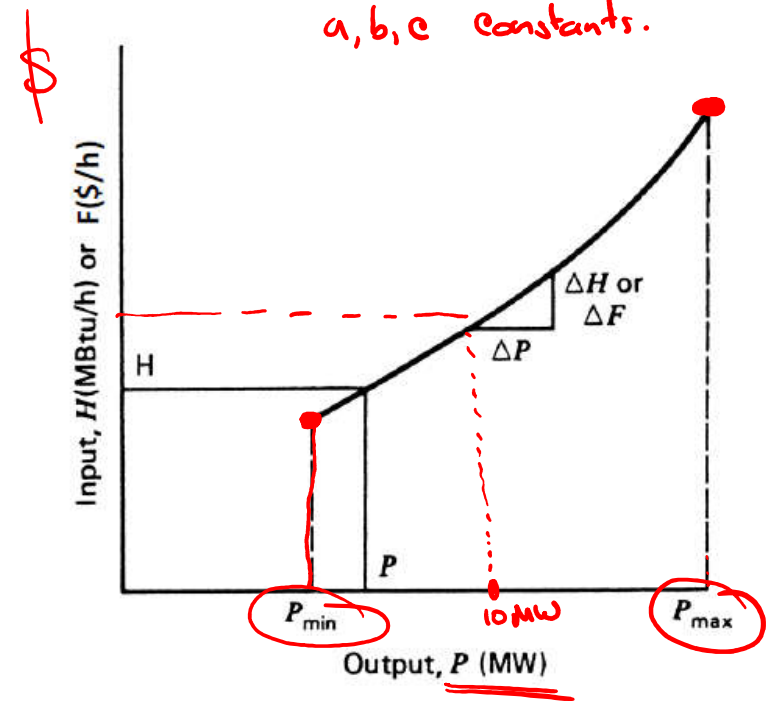


don't want to turn on/off frequently



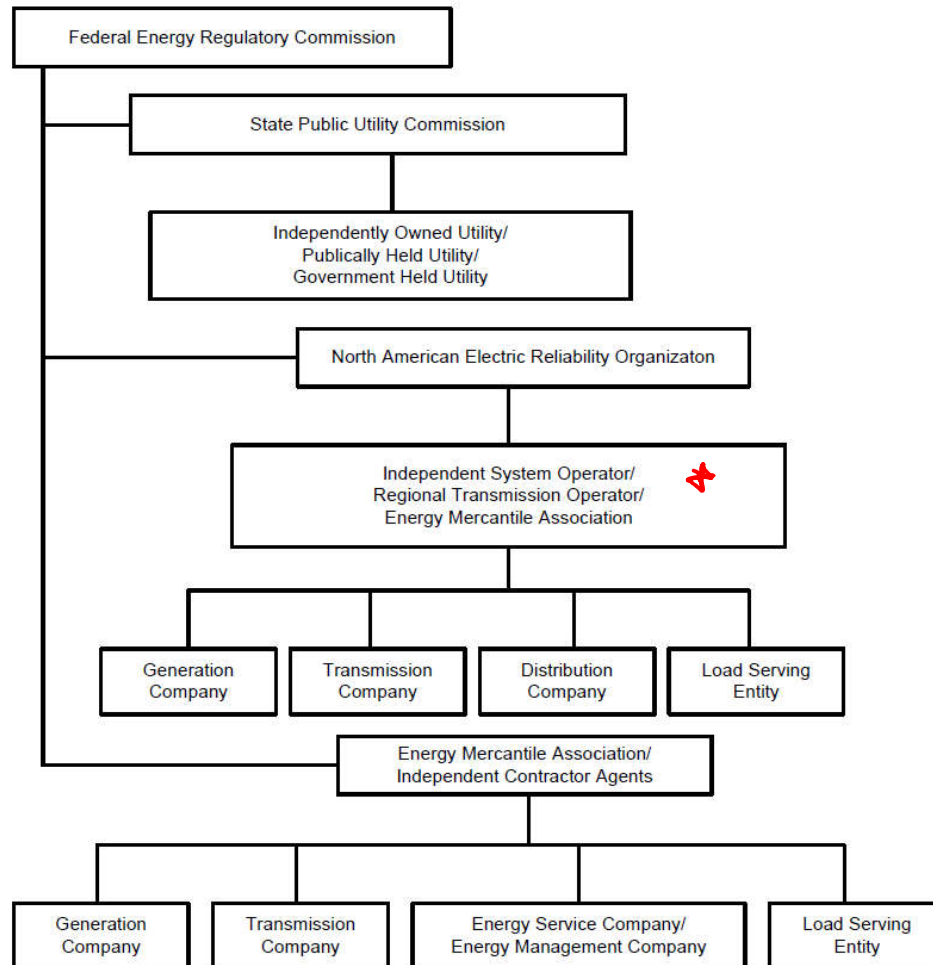
$$C(P) = aP^2 + bP + c$$

a, b, c constants.



Types of Markets

- Nowadays, most markets are **competitive**
- The Independent System Operators (ISO) ensure the grid operation, market administration and **planning**



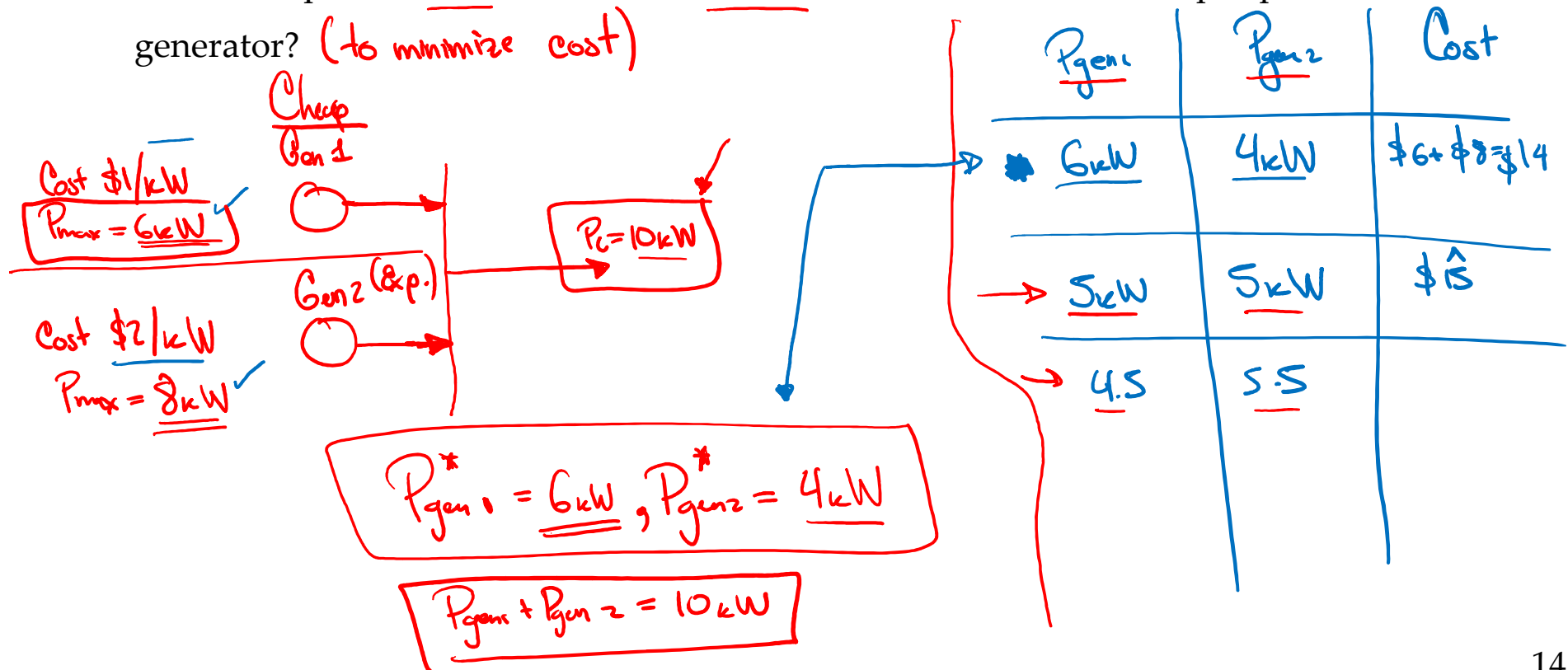
<http://www.isorto.org/about/default>

<https://www.iso-ne.com/isoexpress/>

Economic Dispatch Example

(1 hour)

- **Economic Dispatch** is to find out, for a **single period of time**, the output power of every generation unit so that demands are satisfied at a **minimum costs**
- Example: Two generators must supply a load which is consuming 10 kW. Generator 1 can provide a maximum power of 6 kW at a cost of \$1/kW, Generator 2 can provide a maximum power of 8 kW at a cost of \$2/kW. What should be the output power of each generator? (to minimize cost)



Economic Dispatch Example – Mathematical Formulation

- Example: Two generators must supply a load which is consuming 10 kW. Generator 1 can provide a maximum power of 6 kW at a cost of \$1/kW, Generator 2 can provide a maximum power of 8 kW at a cost of \$2/kW. What should be the output power of each generator?

minimize total Cost

subject to:

$$P_1 + P_2 = 10 \text{ kW}$$

$$0 \leq P_1 \leq 6 \text{ kW}$$

$$0 \leq P_2 \leq 8 \text{ kW}$$

$$\min_{P_1, P_2} \left(\overbrace{1P_1}^{\text{Cost 1}} + \overbrace{2P_2}^{\text{Cost 2}} \right) \quad \left. \vphantom{\min_{P_1, P_2}} \right\} \text{Cost function}$$

→ s.t.

$$1) P_1 + P_2 = 10 \text{ kW}$$

$$2) 0 \leq P_1 \leq 6 \text{ kW}$$

$$3) 0 \leq P_2 \leq 8 \text{ kW}$$

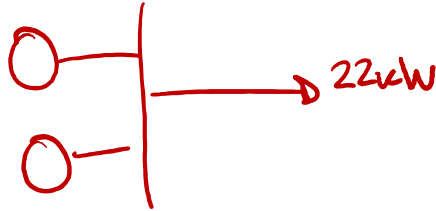
Constraints

- This formulation falls under a **linear programming problem** (optimization)

Economic Dispatch Example 2

- Generator 1 provides power at a cost of $C_1(P_1) = 0.5P_1^2 + 2P_1$ and generator 2 provides power at a cost of $C_2(P_2) = 0.25P_2^2 + 0.2$
- Generators 1 and 2 capacity are at 8 kW and 15 kW respectively
- They must supply a load of 22 kW. What should be the output power of each generator?

(not so trivial)



$$\min_{P_1, P_2} C_1(P_1) + C_2(P_2) = 0.5P_1^2 + 2P_1 + 0.25P_2^2 + 0.2$$

s.t.

$$P_1 + P_2 = 22 \text{ kW}$$

$$0 \leq P_1 \leq 8 \text{ kW}$$

$$0 \leq P_2 \leq 15 \text{ kW}$$

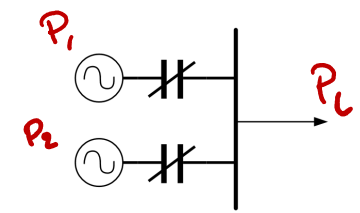
Unit Commitment Example

(Planning)

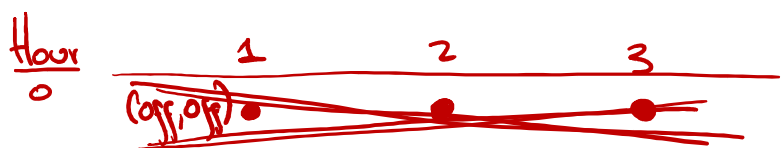
- Unit Commitment problem consists of determining, for a planning horizon (typically 1 day), the start-up and shut-down schedule of all production units so that the electric demand is supplied and total operating costs are minimized

	Gen.	P_{min}	P_{max}	Cost/power	Start-up cost
Cheap	1	1.5	7	7.2	4
Expensive	2	1	6	7.8	4

Hour	1	2	3
P_L	5.5	8	4

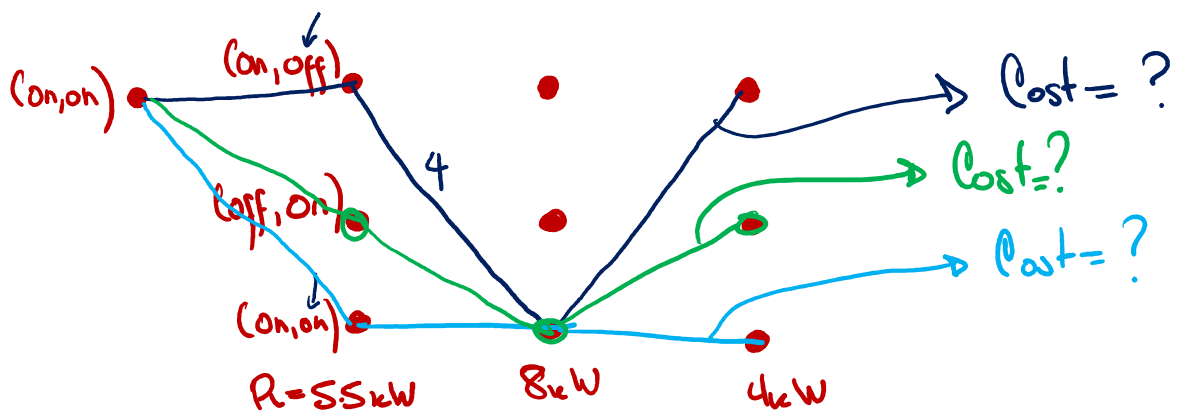


Initial condition (on, on)
1 2



Combinations = $(2^{N_{gen}} - 1)^{N_{hours}}$
 $= (2^2 - 1)^3 = 27$

Shortest Path Problem



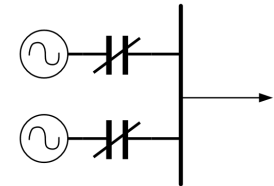
N_{gen}	No. of Combinations for 24 hours
5	6.2×10^{35}
10	1.73×10^{72}
20	3.12×10^{144}
40	* (too big) *

Unit Commitment Example (cont'd)

- What is the best way to operate the generators for the specified 3 hours?

Gen.	P_{\min}	P_{\max}	Cost/power	Start-up cost
1	1.5	7	7.2	4
2	1	6	7.8	4

Hour	1	2	3
P_L	5.5	8	4

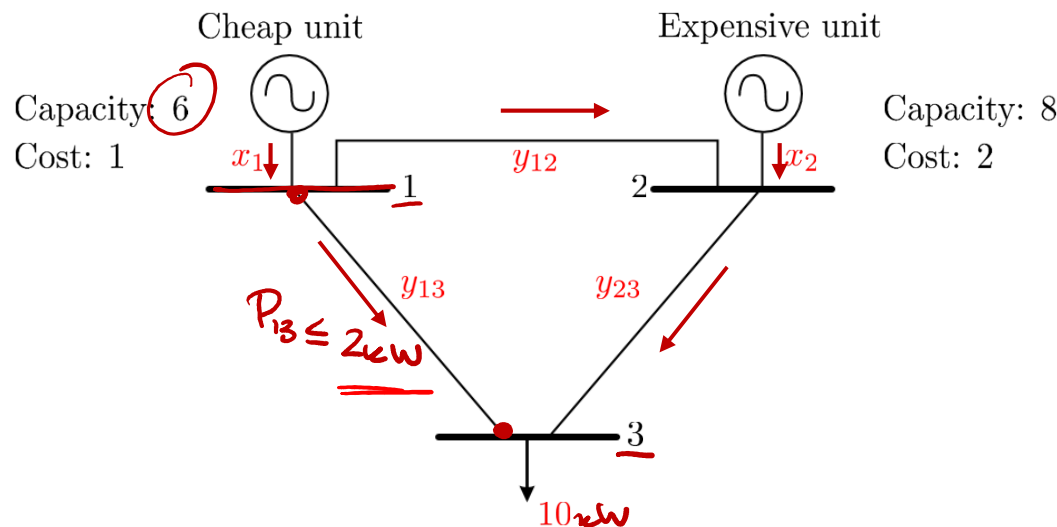


N_{gen}	No. of Combinations for 24 hours
5	6.2×10^{35}
10	1.73×10^{72}
20	3.12×10^{144}
40	(too big)

Optimal Power Flow Example

(for 1 hour)

- The goal of the **Optimal Power Flow (OPF)** problem is to find out the power output of every unit (including active and reactive) so that **all loads are supplied at a minimum costs while satisfying network constraints*** (same as Econ. Dispatch + Network Const.)
- Example:** Same as economic dispatch example, but make sure that the maximum power flowing through line 1-3 is 2 kW!



$\min 1P_1 + 2P_2$
 P_1, P_2
 s.t.

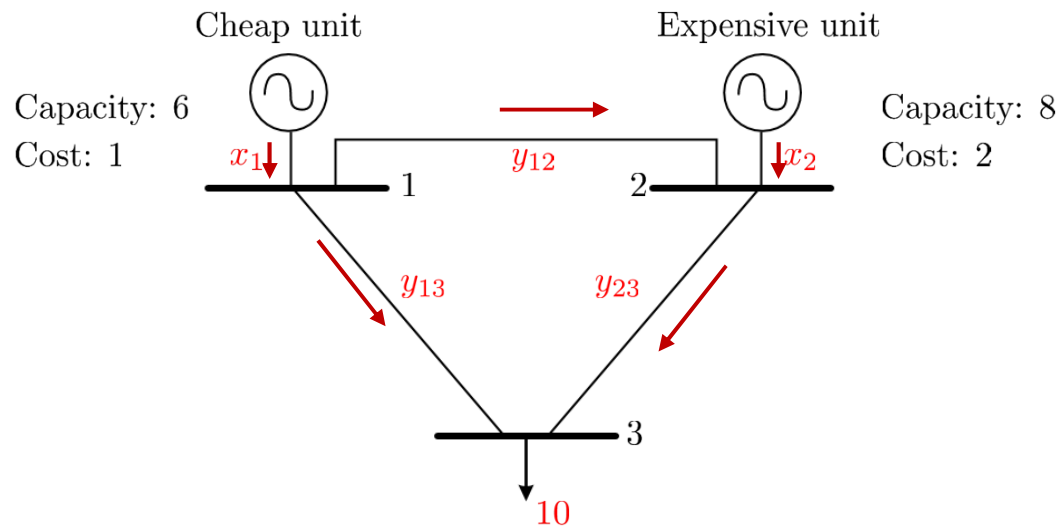
* {Power flow eqns.} nonlinear (sin, cos)

* $0 \leq P_1 \leq 6$
 $0 \leq P_2 \leq 8$

* $P_{13} \leq 2 \text{ kW}$

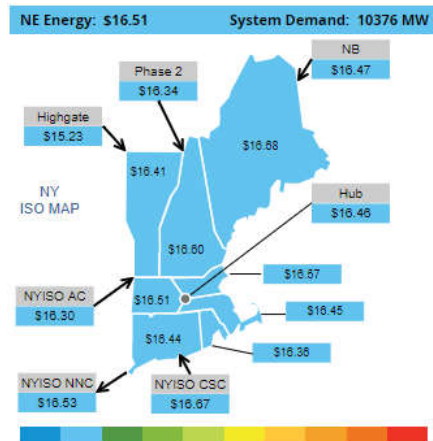
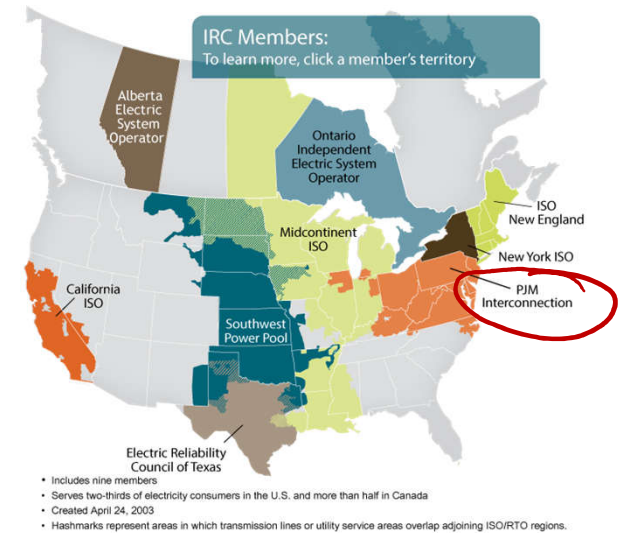
Optimal Power Flow Example

- **Example:** Same as economic dispatch example, but make sure that the maximum power flowing through line 1-3 is 2 kW!

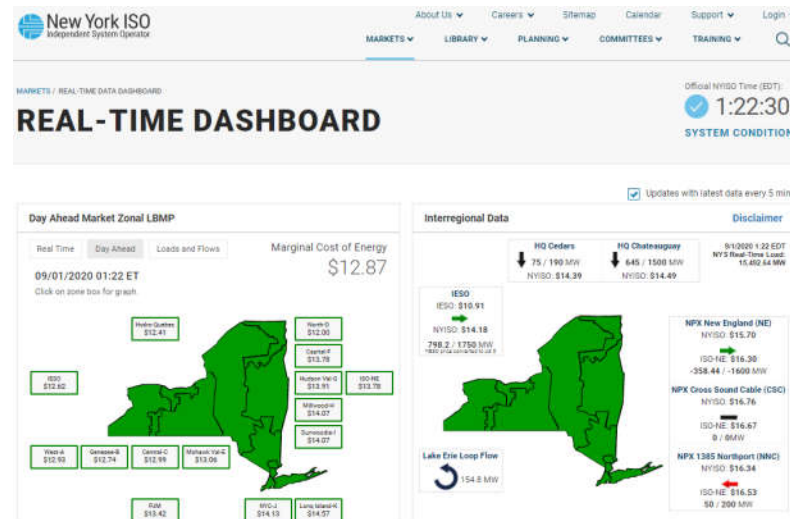


RTO / ISO

- **Regional Transmission Operators:** coordinates, controls, and monitors a **multi-state** electric grid
- **Independent System Operators:** Similar as an RTO but typically within a single state
- The previous optimization problems are utilized by these entities to **control** and optimally* **plan** the operation of generators



<https://www.iso-ne.com/isoexpress/>



<https://www.nyiso.com/real-time-dashboard>

Other Applications in Power

1. What is the best way to coordinate PV + Energy Storage?

optimization problem (Final Project)

2. For a Hybrid Electric Vehicle, what is the best way to operate engine vs. electrical motor?

$$\min_{\mathbf{u}} \left(\sum_{i \in T \setminus \{N_1\}} \pi_i (x_i - x_{ref})' Q (x_i - x_{ref}) + \sum_{i \in T \setminus S} \pi_i u_i' R u_i \right) \quad \text{Cost function} \quad (13a)$$

$$\text{s.t. } x_1 = x(k) \quad (13b)$$

$$x_i = Ax_{pre(i)} + B_1 u_{pre(i)} + B_2 w_i, \quad i \in T \setminus \{N_1\} \quad (13c)$$

$$y_i = Cx_{pre(i)} + D_1 u_{pre(i)} + D_2 w_i, \quad i \in T \setminus \{N_1\} \quad (13d)$$

$$x_i \in \mathcal{X}, \quad y_i \in \mathcal{Y}, \quad i \in T \setminus \{N_1\} \quad (13e)$$

$$u_i \in \mathcal{U}, \quad i \in T \setminus S \quad (13f)$$

Constraints

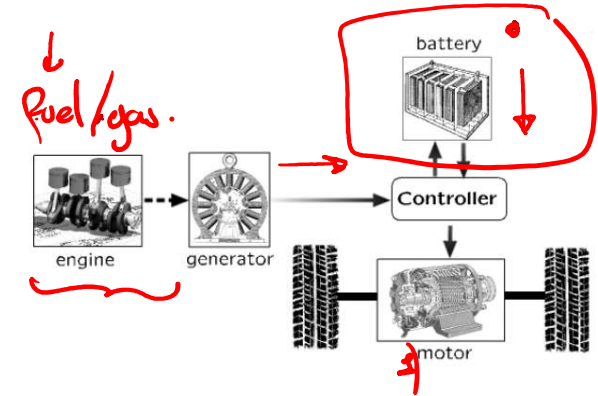
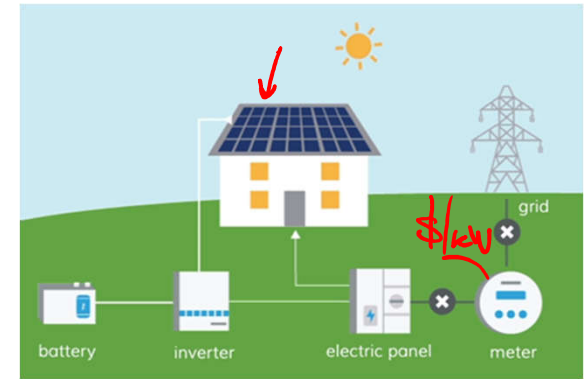
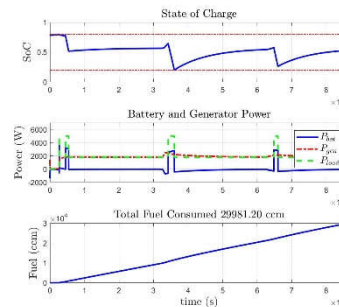
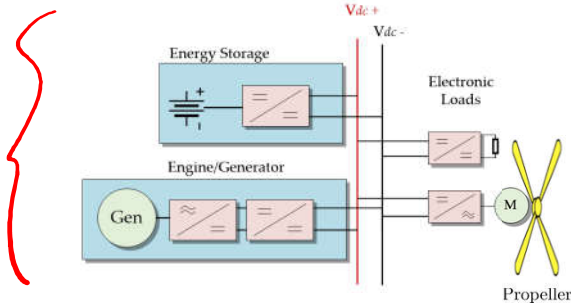


Fig. 3. Schematics of a series hybrid electric powertrain.

3. How to operate a Hybrid UAV to maximize flight time?



4. Many others

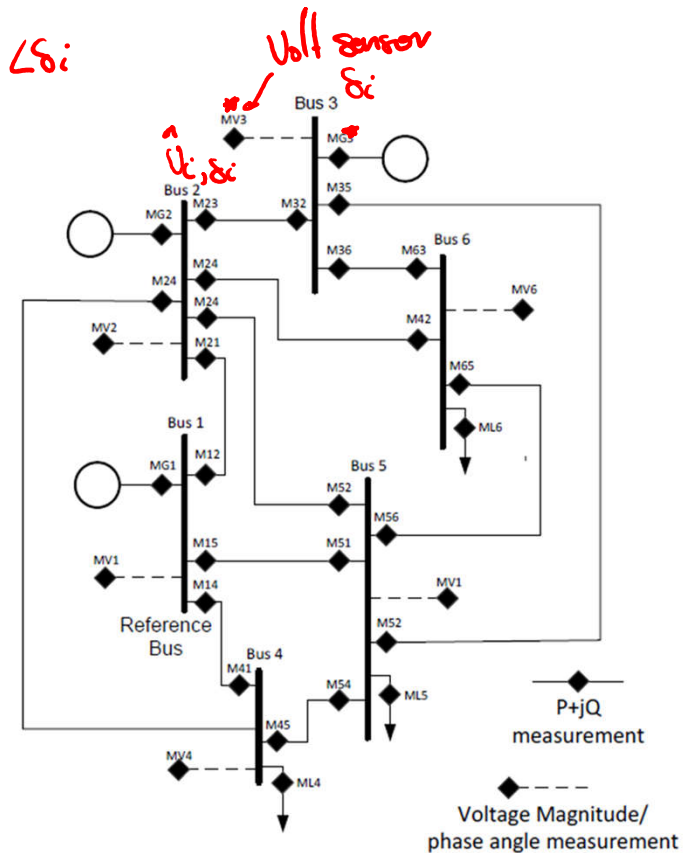
State Estimation Example

- **Why do we need measurements?** To estimate the state of the power grid in real time for both system security and verify constraints are met
 - Are any lines overloaded? ✓
 - Are any voltages above/under limits? ✓
- If there are any problems with the power systems, the control center can take corrective action

$$\tilde{V}_i \approx \hat{V}_i \angle \delta_i$$



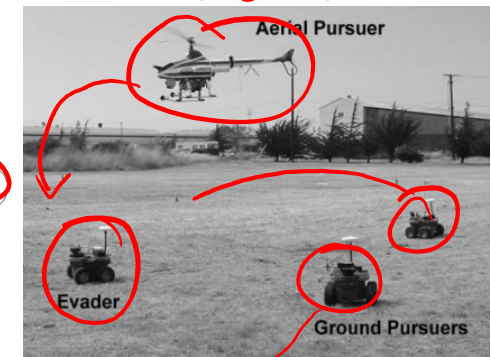
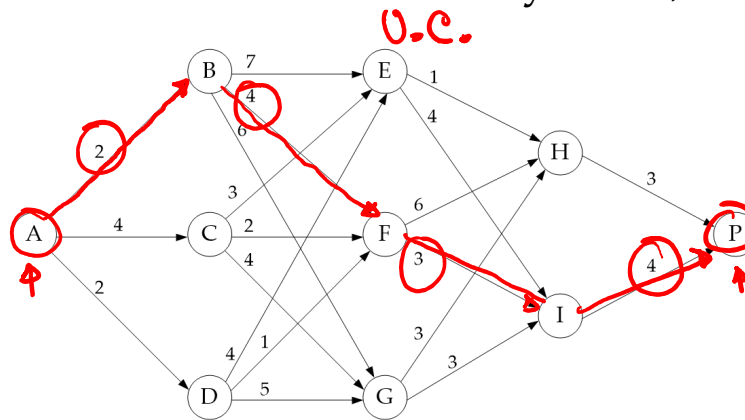
NY ISO control center



Other Applications of Optimization Theory

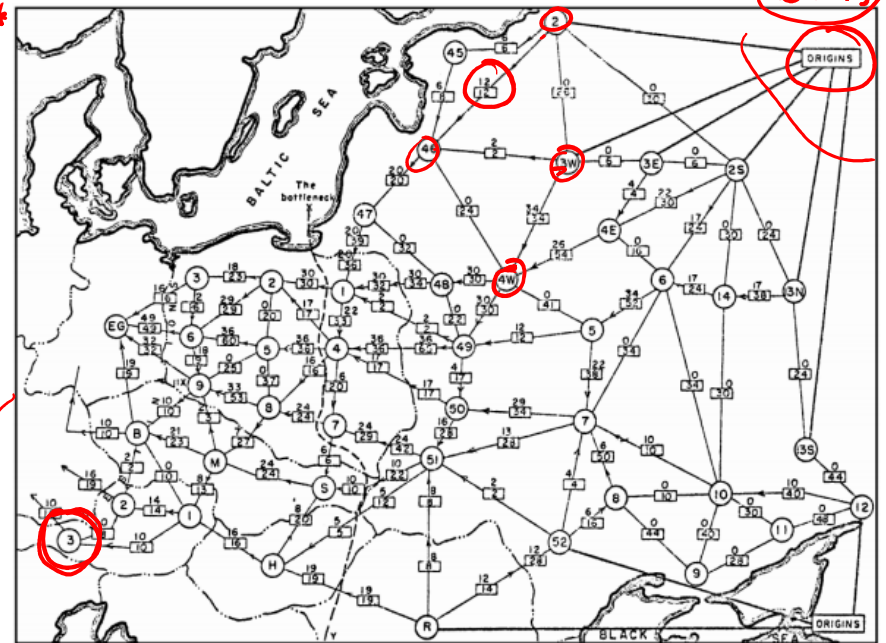
- Optimization techniques are used in other many areas, ranging from:

- Artificial intelligence*
- Control theory
- Economics ✓
- Geophysics
- Chemistry
-



- Example of finding the best path and maximum flow problems

- Harris and Ross (Air Force - 1955)
- Railway network of Western Soviet Union going to Eastern Europe
- Maximum flow is 163k
- Same problem can be used to solve airline scheduling, image segmentation, etc.



Tentative Topics

- **Power System Economics** ⁴
- **Economic Dispatch**
- **Unit Commitment**
- **Optimal Power Flow**
- **State Estimation**
- **Other Topics**
 - Transient analysis
 - Forecasting
- **We will focus more on the application of optimization theory in power systems**
- **Nevertheless, there will be mathematical theory/techniques that are necessary for this course**

