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Balancing congestion and security in the presence of strategic applicants with private information

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ABSTRACT

Concerns on security and congestion appear in security screening which is used to identify and deter potential threats (e.g., attackers, terrorists, smugglers, spies) among normal applicants wishing to enter an organization, location, or facility. Generally, in-depth screening reduces the risk of being attacked, but creates delays that may deter normal applicants and thus, decrease the welfare of the approver (authority, manager, screener). In this paper, we develop a model to determine the optimal screening policy to maximize the reward from admitting normal applicants net of the penalty from admitting bad applicants. We use an M/M/1 queueing system to capture the impact of security screening policies on system congestion and use game theory to model strategic behavior, in which potential applicants with private information can decide whether to apply based on the observed approver's screening policy and the submission behavior of other potential applicants. We provide analytical solutions for the optimal non-discriminatory screening policy and numerical illustrations for both the discriminatory and non-discriminatory policies. In addition, we discuss more complex scenarios including imperfect screening, abandonment behavior of normal applicants, and non-zero waiting costs of attackers.

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1. Introduction

Security screenings play an important role in many fields, including visa issuance, cargo inspection, and airport security screening. In-depth examination of applicants reduces security risk, but can entail high congestion which may deter normal applications and in turn may conflict with the approver's interests. Since September 11, 2001, the security levels for the United States visa issuance have been greatly tightened, significantly affecting regular academic exchanges, and the interactions that go along with these exchanges such as work obligations, collaboration networking, and family reunions (Seife and Ding, 2003; Bhattacharjee, 2004a,b; Bagla, 2006; Stone, 2008). For example, the US Government Accountability Office (2004) states that the average waiting period for a visa security clearance is 67 days, indicating that "students and scholars with science backgrounds might decide not to come to the US, and technological advancements that serve the US and global interests could be jeopardized".

Concerns on security and congestion also appear in the setting of container security at ports of entry. To prevent terrorists from smuggling weapons into the US, US law mandates non-intrusive

imaging and radiation detection for 100% of US-bound containers at international ports. This 100% inspection has raised concerns that resulting congestion will substantially increase the cost of doing business and hurt commerce (Bakshi et al., 2009). Using discrete-event simulation based on actual data, Bakshi et al. (2009) empirically show that the current screening regime is not effective, and a two-step screening process (with a rapid primary screening of all cargo, followed by a more detailed screening of those containers that failed the first test) might be better.

In airport security, as early as the 1970's, researchers have applied queueing models to study airport congestion resulting from security screenings (Gilliam, 1979). Since September 11, 2001, many researchers have studied airport congestion due to the enhanced screening. Blalock et al. (2007) find that the tightened post-9/11 baggage-screening policy has reduced passenger volume by eight percent. Following the attempted terrorist attack to Northwest Airlines Flight 253 on December 25, 2009, the US started a new screening policy requiring citizens of 14 nations (including Pakistan, Saudi Arabia and Nigeria), who are flying to the US, to be subject to special screening at airports worldwide (Lipton, 2010). This nationality-based discriminatory screening policy has been widely criticized (Fisher, 2010), while its effectiveness remains unclear.

Motivated by the above examples, we apply game theory and queueing theory in this paper to study the approver's optimal

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screening policy, considering both system congestion and the strategic behavior of potential applicants with private information. Each potential applicant could be either a terrorist (bad type) or not (good type), which is his private information and not directly observable by the approver. The approver's screening policy can be non-discriminatory, or discriminatory based on the applicants' observable attributes (such as age, nationality, gender, and security history). There might exist some correlation between the unobservable information and the observable attributes.

The novelty of this research, compared to previous studies, is that it allows *strategic* decisions by *all* types of potential applicants. In particular, potential applicants could adapt their behavior according to a disclosed security policy (Zhuang and Bier, 2007). For example, smugglers may choose the weakest port to enter; leisure travelers may choose not to travel because of congestion; and foreign students may no longer apply to the US schools because of the long waiting period for visas.

To our knowledge, no research to date has simultaneously considered both the applicant's strategic behavior and congestion in determining the optimal screening policy (with an exception of a recent paper by Bakshi and Gans (2010), which considers congestion and the terrorist's strategic choice but does not consider the normal people's choice); our research aims to fill this important theoretical gap. In particular, we first analytically derive the approver's optimal non-discriminatory screening policy, and then use numerical examples to illustrate the benefit of discriminatory policies based on observable attributes.

We recognize that there exists close work on security screening using game theory and economic modeling. For example, in the setting of container security at ports of entry, Bier and Haphuriwat (in press) study the optimal proportion of containers to inspect using game theory to capture the fact that attackers are simultaneously trying to maximize their expected rewards. In critical infrastructure protection, optimal defense investment in the face of adaptive terrorists has been studied (Golany et al., 2009; Zhuang and Bier, 2007; Zhuang et al., 2010; Golalikhani and Zhuang, forthcoming). In the economics literature, Basuchoudhary and Razzolini (2006) and Yetman (2004) have studied the idea of discriminatory screening. In contrast to our paper, all of these papers fail to consider congestion or normal applicants' decisions.

In recent years, selective screening based on passenger profiling has been proposed to reduce the inconvenience caused to normal passengers and improve the effectiveness of screening devices. McLay et al. (2006) show that using different screening procedures on different passenger types (passenger risk information) can lead to more effective security screening strategies. Babu et al. (2006) study the effects of classifying passengers into different groups and applying different levels of screening to them. Nie et al. (2009) extend the work of Babu et al. (2006) by allowing passengers to have heterogeneous threat levels. Recently, Cavusoglu et al. (2010) study the impacts of profiling on the design of the screening systems and other performance measures, such as the reliability of screening device signals and the inconvenience caused to normal passengers. However, these papers do not consider strategic passengers' behavior. Along the same line, in other application domains which are different from transportation security, Viaene et al. (2007) study the optimal screening policy for detecting fraudulent automobile insurance claims, and Claeys et al. (2010) study group screening policies in a queueing model with dynamic arrivals.

In the service operations management literature, there exists some work using a game-theoretic formulation of a queueing problem to study the interaction between the service provider and the customers who consider congestion when deciding whether or not to queue (for an excellent overview, see Hassin and Haviv, 2003). This formulation proves to be effective in modeling service systems

with customer behaviors and thus, fits for our settings. An example using this formulation is Anand et al. (2011) which studies the similar tradeoff between quality (analogous to security in the above literature) and congestion trade-off in a setting where customers decide whether to use the service based on their evaluations of quality and speed. As in Anand et al. (2011), we endogenize the trade-off between quality and congestion into individual decisions. But in comparison, Anand et al. (2011) assume the service provider directly decides service speed and price to maximize her revenue, while our work assumes that the service provider determines screening probabilities and service speed is a parameter, not a decision. In addition, the quality/time interaction that Anand et al. (2011) outline is modeled explicitly as a monotonic function: as the service speed increases, the quality of the service decreases which depresses demand. In contrast, the quality (security)/time interaction in our paper lies implicitly in the fact that the more applicants are screened, the more bad applicants can be caught while more congestion is created at the approver. Due to the nature of the security context, we address differentiated screening strategies in the presence of heterogeneous customers (potential applicants or travelers) with observable information which is not discussed by Anand et al. (2011).

The remainder of the paper is organized as follows. A description of the model is presented in Section 2. Section 3 provides an analysis of the best responses of potential applicants. Section 4 provides an analytical solution for the approver's optimal non-discriminatory policy. Section 5 then provides numerical analysis of both discriminatory and non-discriminatory policies and indicates under which conditions discriminatory policies are significantly better. Section 6 discusses and analyzes several extensions of our model. Section 7 concludes this paper and provides future research directions. Finally, the appendix provides proofs to the propositions in this paper.

2. The model

We consider a manager, which we refer to as the "approver," facing a population of strategic potential applicants willing to enter a secure organization or facility. Note that in this paper we use "*potential applicant*" to represent the people who have intentions to apply but may or may not submit their applications. In contrast, we use "*applicant*" to represent the people who have already submitted their applications. The approver decides whether to screen each applicant based on observable attributes such as age, nationality, gender, occupation, and security history. The approver can immediately approve an application, in which case the applicant passes. On the other hand, if the approver decides to screen the applicant, the applicant will be placed in a queue to wait for the result of the screening process (either approval or rejection). Fig. 1 shows a flowchart of the process.

The approver's goal is to reduce the risk of admitting bad applicants (attackers), while simultaneously reducing the inconvenience (congestion) to good applicants. Screening numerous applicants decreases the chance of admitting a bad applicant, but increases waiting times, which could decrease the willingness of good potential applicants to apply. All potential applicants are

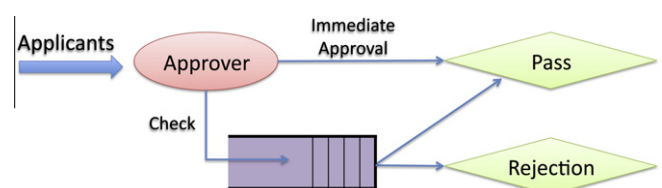


Fig. 1. The approval process with strategic potential applicants and congestion.

assumed to decide whether to submit an application by weighing the costs and benefits, according to the announced screening policy. In the following subsection, we outline our assumptions regarding characteristics of potential applicants, cost structure, screening, and service characteristics, and then formulate the approver's optimization problem (taking into account the potential applicants' decisions).

2.1. Model setup

We assume: (1) the approver cannot immediately reject applicants; i.e., applicants can be rejected only after screening; (2) when the approver is indifferent between different levels of screening probabilities, she will choose the lowest level due to convenience/cost concerns. In Sections 2–5 we assume perfect screening; i.e., after screening, all of good applicants will pass and all of bad applicants will be caught; in Subsection 6.1, we relax this assumption by allowing non-zero screening errors. The elements of the model are described as follows.

Applicant characteristics. Each potential applicant can be one of two types, $\theta \in \{g, b\}$, representing good and bad types, respectively. The type is known to the potential applicant himself, but unobservable to the approver. Each potential applicant also has an observable attribute that can take on one of two possible values, $t \in \{1, 2\}$. The probability that a potential applicant has attribute $t = 1$ is given by $p \in [0, 1]$. We assume that potential applicants are bad with probability α if $t = 1$ and with probability β if $t = 2$. The joint probability masses are $p(1 - \alpha)$, $p\alpha$, $(1 - p)(1 - \beta)$, and $(1 - p)\beta$, for a potential applicant of types 1g, 1b, 2g, and 2b, respectively.

Cost structure. We assume that the approver gains R for admitting each good applicant, and loses C for admitting each bad applicant. A good applicant receives a reward of r_g if he is approved and incurs a waiting cost of c_w per unit time if he is screened. A bad applicant receives a reward of r_b if he is approved and incurs a penalty of c_b if he is caught. To make analysis tractable, we assume that the reward r_b and the penalty c_b are sufficiently large such that bad potential applicants typically neglect the waiting cost when making submission decisions. In Subsection 6.3, we relax this assumption in numerical experiments.

Service characteristics. Potential applicants are assumed to arrive according to a Poisson process with rate λ . All potential applicants independently decide whether to submit an application. We assume no renegeing; i.e., once an applicant begins screening, he waits for the result of this process without leaving the queue or withdrawing his application. In real applications, good applicants could abandon the queue due to long waiting time. Thus, we relax this assumption in Subsection 6.2 numerically. We model the screening process as an $M/M/1$ queueing system with a service rate of μ . The average time interval between when an applicant submits a request and when he gets an approval or rejection is denoted by W , the average waiting time.

We assume that the applicants cannot observe the actual length of queue. This assumption is reasonable because little evidence exists in the domains of our focus (visa applications, background checks for security jobs and container screening), that the potential applicants know the state of the queue when they make the submission decision. Typically, the potential applicants only know the expected waiting time through their or other people's experiences. This type of model, characterizing customers' equilibrium behavior when the state of the queue is unobservable, has been defined as "an unobservable queue" model in Hassin and Haviv (2003).

Approver's strategy. The approver's strategy is given by $\Phi \doteq (\Phi_1, \Phi_2)$, where $\Phi_t \in [0, 1]$ is the probability of screening an applicant with an attribute value t . Her objective is to maximize

the reward from admitting good applicants net of the penalty from admitting bad applicants¹:

$$\max_{\Phi} J(\Phi) = (\lambda_{1g} + \lambda_{2g})R - [(1 - \Phi_1)\lambda_{1b} + (1 - \Phi_2)\lambda_{2b}]C, \tag{1}$$

where $\lambda_{t\theta}$ are the arrival rates of applicants with $t \in \{1, 2\}$ and $\theta \in \{g, b\}$. Due to the assumption of perfect inspection, the good applicants will pass eventually, regardless of whether they are screened or not, and the bad applicants will pass only when they are not screened. Therefore the approver gets a reward of R from each good applicant and a penalty cost C from each bad applicant who is not screened.

Potential applicants' strategy. Potential applicants behave as rational economic agents who maximize their expected utilities. Their utilities depend not only on their own decisions, but also on the decisions of other potential applicants and the decision of the approver. Each potential applicant has two options: to submit an application or not. Let $p_{t\theta} \in [0, 1]$ denote the potential applicants' submission probability for $t \in \{1, 2\}$ and $\theta \in \{g, b\}$ which is a pure strategy if $p_{t\theta} = 0, 1$, and is a mixed strategy otherwise. The total traffic rate for screening is the summation over all screened applicants: $\sum_{t=1}^2 \Phi_t(p_{tg}A_{tg} + p_{tb}A_{tb})$ where $A_{1g} = p(1 - \alpha)\lambda$, $A_{1b} = p\alpha\lambda$, $A_{2g} = (1 - p)(1 - \beta)\lambda$, and $A_{2b} = (1 - p)\beta\lambda$. We denote the potential applicants' strategies by $\mathbf{p} \doteq (p_{1g}, p_{2g}, p_{1b}, p_{2b})$. Thus, the arrival rates of applicants are $\lambda \doteq (\lambda_{1g}, \lambda_{2g}, \lambda_{1b}, \lambda_{2b})$, where $\lambda_{t\theta} = p_{t\theta}A_{t\theta}$, for $t \in \{1, 2\}$, and $\theta \in \{g, b\}$.

For a good potential applicant, his utility of not submitting an application is zero and his utility of submitting an application is the reward minus the expected waiting cost. Thus, his expected utility is:

$$u_{tg}(\Phi, \mathbf{p}) = p_{tg}[r_g - \Phi_t c_w W(\Phi, \mathbf{p})], \quad \text{for } t \in \{1, 2\}, \tag{2}$$

where, from Ross (2002), the average waiting time for the $M/M/1$ queueing system is given by:

$$W(\Phi, \mathbf{p}) = \frac{1}{\mu - \sum_{t=1}^2 \Phi_t(p_{tg}A_{tg} + p_{tb}A_{tb})}. \tag{3}$$

Similarly, a bad potential applicant's expected utility is:

$$u_{tb}(\Phi, \mathbf{p}) = p_{tb}[\Phi_t(-c_b) + (1 - \Phi_t)r_b], \quad \text{for } t \in \{1, 2\}. \tag{4}$$

2.2. Definition of equilibrium

Combining good and bad potential applicants' utilities in Eqs. (2) and (4), for a given approver's strategy Φ , the objective function of a potential applicant with an observable attribute t and an unobservable type θ is:

$$\max_{p_{t\theta}} u_{t\theta}(\Phi, \mathbf{p}) = \begin{cases} p_{tg}[r_g - \Phi_t c_w W(\Phi, \mathbf{p})] & \text{if } \theta = g, \\ p_{tb}[\Phi_t(-c_b) + (1 - \Phi_t)r_b] & \text{if } \theta = b. \end{cases} \tag{5}$$

Given Φ , we define the potential applicants' best response:

$$\hat{\mathbf{p}}(\Phi) = [\hat{p}_{1g}(\Phi), \hat{p}_{1b}(\Phi), \hat{p}_{2g}(\Phi), \hat{p}_{2b}(\Phi)],$$

where

$$\hat{p}_{t\theta}(\Phi) = \arg \max_{p_{t\theta}} u_{t\theta}(\Phi, \mathbf{p}), \quad \text{for } t \in \{1, 2\} \text{ and } \theta \in \{g, b\}. \tag{6}$$

¹ In order to focus on the tradeoff between the congestion impact and the security impact on good/bad potential applicants, respectively, we ignore the approver's screening cost which is proportional to Φ due to labor, time or financial costs consumed during the screening process.

Definition 1. We call a collection (\mathbf{p}^*, Φ^*) a subgame perfect Nash equilibrium, or equilibrium, if and only if

$$\mathbf{p}^* = \hat{\mathbf{p}}(\Phi) \tag{7}$$

and

$$\Phi^* = \arg \max_{\Phi} J[\Phi; \hat{\mathbf{p}}(\Phi)]. \tag{8}$$

Table 1 summarizes major notations used in this paper. Having established our model, we now proceed to its analysis. In particular, we first derive best responses of potential applicants in Section 3, and then solve for the optimal strategy of the approver in Section 4.

3. Potential applicants' best responses

3.1. Bad potential applicants' best responses

Proposition 1. Bad potential applicants' best responses are given by²:

$$\hat{p}_{tb}(\Phi_t) = \begin{cases} 1, & \Phi_t < s_b = \frac{r_b}{c_b+r_b}, \\ 0, & \Phi_t \geq s_b = \frac{r_b}{c_b+r_b}, \end{cases} \text{ for } t = 1, 2. \tag{9}$$

Remark. Bad potential applicants do not consider congestion in this section, so their strategies do not depend on the strategies of other potential applicants. Their strategies solely depend on a comparison between the probability of being screened and a threshold value s_b ; they apply with probability one if the probability of being screened is sufficiently small (below s_b), and with probability zero otherwise. From the definition of s_b , we see that intuitively a bad potential applicant is more likely to apply when his reward after passing screening is high, or his penalty after being caught is low.

3.2. Good potential applicants' best responses

A good potential applicant's best response is more complex, because it depends on the decisions of other potential applicants through negative externality associated with congestion, as shown in Eqs. (2) and (3). If we fix the approver's strategy Φ and bad potential applicants' best responses \hat{p}_{tb} , $t = 1, 2$, we are left with an equilibrium analysis problem on two classes of customers: good potential applicants with an attribute value of 1, and good potential applicants with an attribute value of 2. This equilibrium analysis problem has been solved in Balachandran and Schaefer (1980). As in Balachandran and Schaefer (1980), we first define the *desired aggregate arrival rate* of screened good potential applicants as follows:

Note that the traffic caused by bad applicants is:

$$\Phi_1 \hat{p}_{1b} p \alpha \lambda + \Phi_2 \hat{p}_{2b} (1-p) \beta \lambda.$$

Assuming there are no good applicants with $t=2$, at the equilibrium, the maximum traffic of screened good applicants should be:

$$\hat{\lambda}_{1g} = \mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1-p) \beta \lambda - \frac{\Phi_1 c_w}{r_g}, \tag{10}$$

which is derived from the fact that the good applicant of attribute 1 has zero utility at the equilibrium; $r_g - \Phi_1 c_w W = r_g - \frac{\Phi_1 c_w}{\mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1-p) \beta \lambda - \hat{\lambda}_{1g}} = 0$.

² We assume when a bad potential applicant is indifferent between submitting or not, he will choose not to submit his application due to cost concerns.

Table 1
Major notations.

Notation	Explanation
$\theta \in \{g, b\}$	Unobservable type of a potential applicant
$t \in \{1, 2\}$	Observable attribute of a potential applicant
p	Probability that a potential applicant has attribute 1
α	Probability that a potential applicant with attribute 1 is bad
β	Probability that a potential applicant with attribute 2 is bad
R	Approver's reward for admitting each good applicant
C	Approver's penalty for admitting each bad applicant
r_g	Good applicant's reward if passed
r_b	Bad applicant's reward if passed
c_w	Good applicant's cost per unit of waiting time
c_b	Bad applicant's penalty if rejected
λ	Poisson arrival rate of all potential applicants
$\lambda_{t\theta}$	Poisson arrival rate of potential applicants with type θ and attribute t
μ	Service rate of the screening process
$W(\Phi, \mathbf{p})$	Expected waiting time
$\Phi \doteq (\Phi_1, \Phi_2)$	Approver's strategy
$\Phi_t \in [0, 1]$	Probability of screening an applicant with attribute t
$J(\Phi)$	Approver's objective function
$\lambda = \{\lambda_{t\theta}\}$	Arrival rates of applicants
$\mathbf{p} = \{p_{t\theta}\}$	Potential applicant's submission probability
$u_{t\theta}$	Potential applicant's expected utility with attribute t and type θ
$\hat{\mathbf{p}}(\Phi)$	Potential applicant's best response for given Φ

Similarly, if assuming there are no good applicants with $t = 1$, then at the equilibrium, the maximum traffic of screened good applicants should be:

$$\hat{\lambda}_{2g} = \mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1-p) \beta \lambda - \frac{\Phi_2 c_w}{r_g}, \tag{11}$$

which is derived from the fact that the good applicant of attribute 2 has zero utility at the equilibrium; $r_g - \Phi_2 c_w W = r_g - \frac{\Phi_2 c_w}{\mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1-p) \beta \lambda - \hat{\lambda}_{2g}} = 0$.

Thus, $\hat{\lambda}_{1g}$ is the maximum demand rate "desired" by the good potential applicants with $t = 1$. That is, when assuming there are no good applicants with $t = 2$, the good potential applicants with $t = 1$ would apply (utility is non-negative) unless their *screened* aggregate demand rate is more than $\hat{\lambda}_{1g}$. When the demand rate reaches $\hat{\lambda}_{1g}$, their utility becomes zero. Similarly, $\hat{\lambda}_{2g}$ is the maximum demand rate "desired" by the good potential applicants with $t = 2$, when assuming there are no good applicants with $t = 1$.

Based on the above definitions of $\hat{\lambda}_{1g}$ and $\hat{\lambda}_{2g}$, Proposition 2 below specifies the best responses of good potential applicants. To simplify notation, we denote the Poisson arrival rate of all good potential applicants as λ_g and the Poisson arrival rate of all bad potential applicants as λ_b . In other words, $\lambda_g = \lambda_{1g} + \lambda_{2g} = [p(1-\alpha) + (1-p)(1-\beta)]\lambda$ and $\lambda_b = \lambda_{1b} + \lambda_{2b} = [p\alpha + (1-p)\beta]\lambda$.

Proposition 2. Given the approver's strategy Φ and bad potential applicants' best responses \hat{p}_{tb} for $t = 1, 2$:

- (i) If $\Phi_1 = 0$, then $\hat{p}_{1g} = 1$; if $\Phi_2 = 0$, then $\hat{p}_{2g} = 1$.
- (ii.a) If the approver uses a discriminatory policy and $0 < \Phi_1 < \Phi_2$, then the good potential applicants' best responses are:

$$\hat{p}_{1g} = \frac{1}{\Phi_1 \lambda_{1g}} \max \left[\min \left(\hat{\lambda}_{1g}, \Phi_1 \lambda_{1g} \right), 0 \right], \text{ and}$$

$$\hat{p}_{2g} = \frac{1}{\Phi_2 \lambda_{2g}} \max \left[\min \left(\hat{\lambda}_{2g} - \hat{p}_{1g} \Phi_1 \lambda_{1g}, \Phi_2 \lambda_{2g} \right), 0 \right].$$

- (ii.b) If the approver uses a discriminatory policy and $0 < \Phi_2 < \Phi_1$, then the good potential applicants' best responses are:

$$\hat{p}_{1g} = \frac{1}{\Phi_1 A_{1g}} \max \left[\min \left(\hat{\Lambda}_{1g} - \hat{p}_{2g} \Phi_2 A_{2g}, \Phi_1 A_{1g} \right), 0 \right], \quad \text{and}$$

$$\hat{p}_{2g} = \frac{1}{\Phi_2 A_{2g}} \max \left[\min \left(\hat{\Lambda}_{2g}, \Phi_2 A_{2g} \right), 0 \right].$$

(iii) If the approver uses a non-discriminatory policy $\Phi_1 = \Phi_2 = \Phi > 0$, then $\hat{p}_{1b} = \hat{p}_{2b} = \hat{p}_b$ and $\hat{\Lambda}_{1g} = \hat{\Lambda}_{2g} = \hat{\Lambda}_g$. The good potential applicants' best responses are:

$$\hat{p}_{1g} = \hat{p}_{2g} = \begin{cases} 1, & \text{if } \hat{\Lambda}_g > \Phi A_g, \\ \frac{\hat{\Lambda}_g}{\Phi A_g}, & \text{if } 0 \leq \hat{\Lambda}_g \leq \Phi A_g, \\ 0, & \text{if } \hat{\Lambda}_g < 0. \end{cases}$$

Remark. First, note that the good potential applicants' submission probabilities tend to increase in their corresponding desired aggregate arrival rates and decrease in screening probabilities and arrival rates of all potential applicants. Second, for the case $\Phi_1 < \Phi_2$, good potential applicants with $t = 1$ are less sensitive to congestion than those with $t = 2$. In other words, facing the same level of congestion, the good potential applicants with $t = 1$ have a higher utility and thus are more likely to apply than those with $t = 2$. Therefore, at the equilibrium, if none or a proportion of good potential applicants with $t = 1$ apply (i.e., $\hat{\Lambda}_{1g} < \Phi_1 A_{1g}$), then none of those with $t = 2$ apply; if all of the good potential applicants with $t = 1$ apply (i.e., $\hat{\Lambda}_{1g} \geq \Phi_1 A_{1g}$), then a proportion or all of the good potential applicants with $t = 2$ may apply. Similarly, if $\Phi_1 > \Phi_2$, good potential applicants with $t = 2$ are more likely to apply. When $\Phi_1 = \Phi_2$, the approver is indifferent between these two attribute values and thus good potential applicants behave the same.

4. Optimal screening policies

Substituting best responses of the potential applicants (as specified in Propositions 1 and 2) into the approver's decision-making problem as specified in Eq. (1), we study the approver's optimal strategy.

4.1. Non-discriminatory screening policy

We start with a non-discriminatory screening policy that uses equal screening probabilities for applicants of two attributes: $\Phi_1 = \Phi_2 = \Phi$.

Proposition 3. The approver's optimal non-discriminatory strategy Φ^* is specified in Table 2:

Remark. As shown in Table 2, the optimal non-discriminatory screening probability can only take one of these two values: $\Phi^* = \frac{\mu}{A_g + A_b + \frac{c_w}{r_g}} < s_b$ (in this case, all bad potential applicants apply, i.e., $\hat{p}_b = 1$) and $\Phi^* = s_b = \frac{r_b}{c_b + r_b}$ (in this case, none of the bad potential applicants apply, i.e., $\hat{p}_b = 0$). In general, the approver uses a screening probability smaller than s_b when the bad potential applicant has a high incentive to apply (high s_b) and when the reward of admitting a good applicant is relatively high compared to the penalty of admitting a bad one (high R and low C). In this case, Φ^* increases in the service rate μ and the ratio of the good applicant's gain r_g to his unit waiting cost c_w ; more applicants should be screened if the screening process is faster or good potential applicants are more tolerant to congestion. In addition, Φ^* decreases in the arrival rate of all potential applicants A ; the approver screens a smaller proportion of applicants when the whole population expands. In contrast, when bad applicants are very dangerous to the approver (high C) and are deterred easily (low s_b), and the

reward of admitting a good applicant is relatively low (low R) compared to the penalty of admitting a bad one (C), the approver should use a screening probability which equals s_b to deter all the bad ones. In this case, Φ^* increases in r_b and decreases in c_b . Proposition 3 also implies that Φ^* cannot be zero unless the bad applicant's reward r_b or the service rate μ equals zero.

4.2. Discriminatory screening policy

Now we study the discriminatory policy. A general result is given in the following proposition.

Proposition 4. The approver's optimal discriminatory policy is always better than any non-discriminatory policy.

Remark. Proposition 4 indicates that theoretically the approver's optimal payoff under a discriminatory policy is higher than that under a non-discriminatory policy. The reason is that the approver can utilize observable information to disproportionately screen applicants. For example, if knowing applicants of attribute 1 are more likely to be bad, the approver will screen more of them and screen fewer applicants of attribute 2. Thus, on average, under a discriminatory policy, good applicants will experience a shorter waiting time, bad applicants will experience more strict screening, and the approver will get a higher payoff. In practice, however, there exist many reasons to justify a non-discriminatory policy. For example, due to equity/political concerns, the approver might not be allowed to implement a discriminatory policy. In addition, implementing this policy might be difficult due to a high cost of collecting and verifying observable data. Thus, to decide which policy to use, a good benefit/cost balance must be made.

Analysis of the optimal non-discriminatory screening policy in Section 4.1 implies the complexity to analytically derive the optimal discriminatory policy. Thus, we numerically calculate the optimal discriminatory policy (Φ_1^*, Φ_2^*) for a given set of parameter values in the next section.

5. Numerical experiments

In this section, we conduct numerical sensitivity analysis of our model and compare the discriminatory policy with the non-discriminatory policy. To highlight the most interesting cases, we provide sensitivity analysis only for parameters R , r_b , and A . The baseline parameter values used in all numerical experiments in this paper are set as follows: $p = .6$; $\alpha = .2$; $\beta = .02$; $R = 1$; $C = 10$; $r_g = 1$; $r_b = 2$; $c_w = 1$; $c_b = 1$; $A = 100$; and $\mu = 10$. Note that in this baseline case, we have $s_b = \frac{r_b}{c_b + r_b} \approx 0.67$.

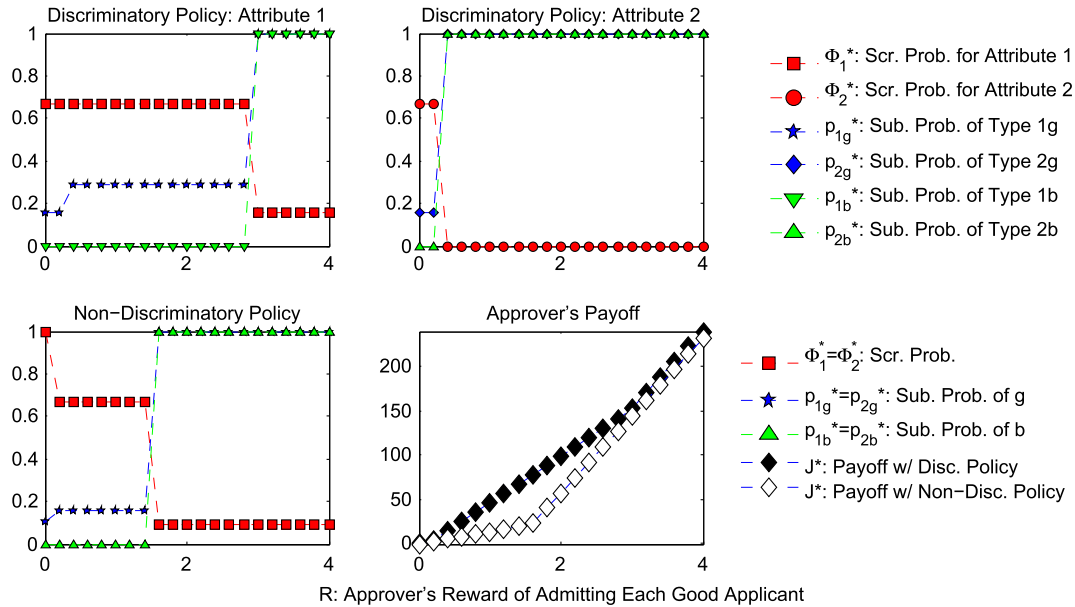
5.1. Changing the approver's reward from admitting a good applicant R

For a discriminatory policy as shown in Fig. 2 (upper panel), when the approver's reward from admitting a good applicant increases, the approver becomes more reluctant to screen applicants. In other words, the screening probabilities Φ_1 and Φ_2 are both non-increasing in R . Thus, potential applicants (including the bad ones) become more likely to apply; i.e., $p_{t\theta}$ (weakly) increases in R for $t = 1, 2, \theta \in \{g, b\}$. The intuition is that when the reward from admitting a good applicant is higher, the approver is willing to reduce screening congestion and take a greater risk of admitting bad applicants.

For a non-discriminatory policy (middle panel in Fig. 2), the screening probability is also non-increasing in R and potential applicants (including the bad ones) become more likely to apply.

Table 2
The optimal non-discriminatory screening policy.

Conditions	Φ^*	Notes
$s_b > \frac{R\mu}{RA_g + CA_b(\mu(A_g + A_b + \frac{\mu}{r_g}) - 1) + R\frac{\mu}{r_g}}$, and $\min\left(1, \sqrt{\frac{R\mu}{CA_b}}\right) > \frac{\mu}{A_g + A_b + \frac{\mu}{r_g}} > 1 - \frac{RA_g}{CA_b}$	$\frac{\mu}{A_g + A_b + \frac{\mu}{r_g}}$	$\hat{p}_b = 1$
Otherwise	s_b	$\hat{p}_b = 0$



R: Approver's Reward of Admitting Each Good Applicant

Fig. 2. Sensitivity analysis for the approver's gain R .

Comparing the approver's payoffs for discriminatory and non-discriminatory policies (lower panel in Fig. 2), the difference is not significant for either large or small values of R , and only significant for medium values of R . The intuition is as follows. Recall that the benefit of a discriminatory policy is due to the reason that it can disproportionately screen applicants: screening fewer less risky ones to reduce congestion while screening more risky ones to lower the loss. When R is sufficiently large (>3 in this example), it is more important to reduce congestion for attracting more good potential applicants than to reduce security risk for deterring bad potential applicants. Thus, the approver screens only a small percentage of applicants no matter under a discriminatory or a non-discriminatory policy. As a result, potential applicants' submission behaviors are similar under these two policies. The benefit from a discriminatory policy is not obvious. When R is sufficiently small (<1 in this example), reducing security risk by deterring bad potential applicants is relatively more important than reducing congestion to have more good potential applicants. Thus the screening probabilities are set high no matter under a discriminatory or a non-discriminatory policy. In summary, a discriminatory policy shows more advantage when the tension between congestion and security risk is more intensive.

5.2. Changing the parameter of bad potential applicants r_b

A high reward when approved (large r_b) motivates bad potential applicants to apply.³ First, look at the optimal discriminatory policy. In the example shown in Fig. 3, the optimal screening probability for applicants of attribute 1 is always $s_b = \frac{r_b}{r_b + c_b}$, which is increasing with r_b . Thus when r_b increases, bad potential applicants of attribute 1 are all deterred. In contrast, the approver's screening probability for

applicants of attribute 2 is relatively small. Especially, when $r_b > 0.2$ in Fig. 3, the approver's screening probability for applicants of attribute 2, Φ_2 is zero, and therefore, both good and bad potential applicants apply with probability 1: $p_{2g} = p_{2b} = 1$. This is because in this numerical example, an optimal discriminatory policy focuses on reducing the security risk from more risky applicants of attribute 1 while ignoring less risky applicants of attribute 2. Such a focus is more important when bad potential applicants are more likely to apply (for example, $r_b > 0.2$). Due to the increased congestion by screening more applicants of attribute 1, the submission probability of good potential applicants p_{1g} is decreasing as r_b increases.

Second, look at the optimal non-discriminatory policy. In the example shown in Fig. 3, the optimal screening probability for all applicants always follows $s_b = \frac{r_b}{r_b + c_b}$. Thus there are no bad applicants and submission probabilities of good potential applicants decrease as the screening probability increases.

Third, the difference in the approver's payoffs under discriminatory and non-discriminatory policies is significant for large values of r_b . This is because when bad potential applicants have a greater incentive to apply, the approver in general screens more applicants, which results in higher congestion. Then it is more beneficial to screen fewer applicants with low risk to reduce congestion and to screen more applicants with high risk for security concern. This again confirms that a discriminatory policy shows more advantage when the tension between congestion and security risk is more intensive.

5.3. Changing the arrival rate of all potential applicants λ

A higher arrival rate of all potential applicants implies more congestion.⁴ First, look at the optimal discriminatory policy. In our

³ Since decreasing c_b has the same impact as increasing r_b , we ignore the numerical results on c_b in this section.

⁴ We have conducted numerical experiments on service capacity μ . Since decreasing μ has the similar impact as increasing λ , we do not report its numerical results in this paper.

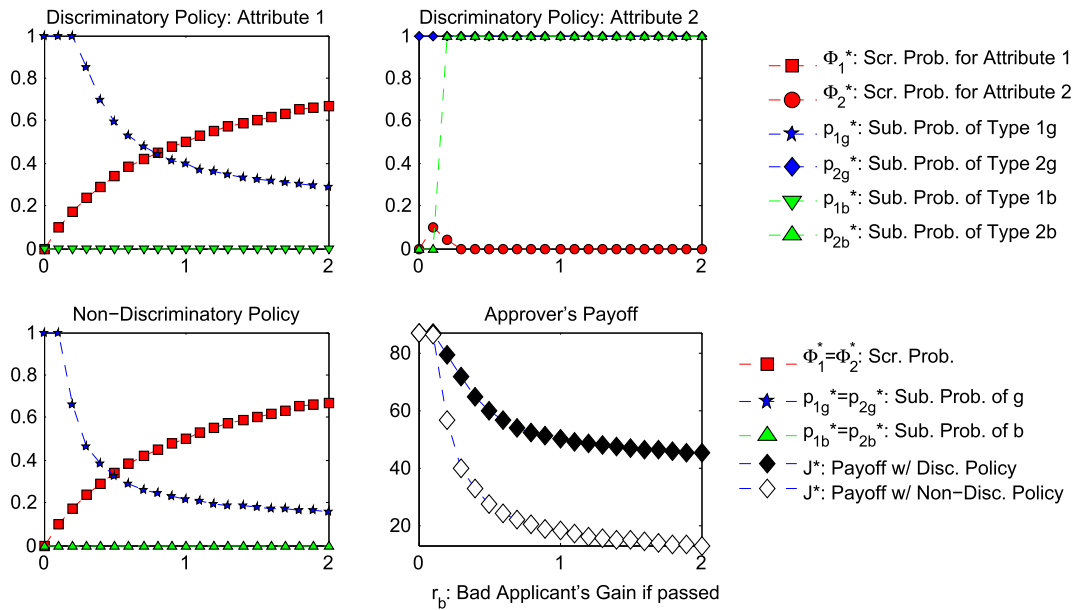
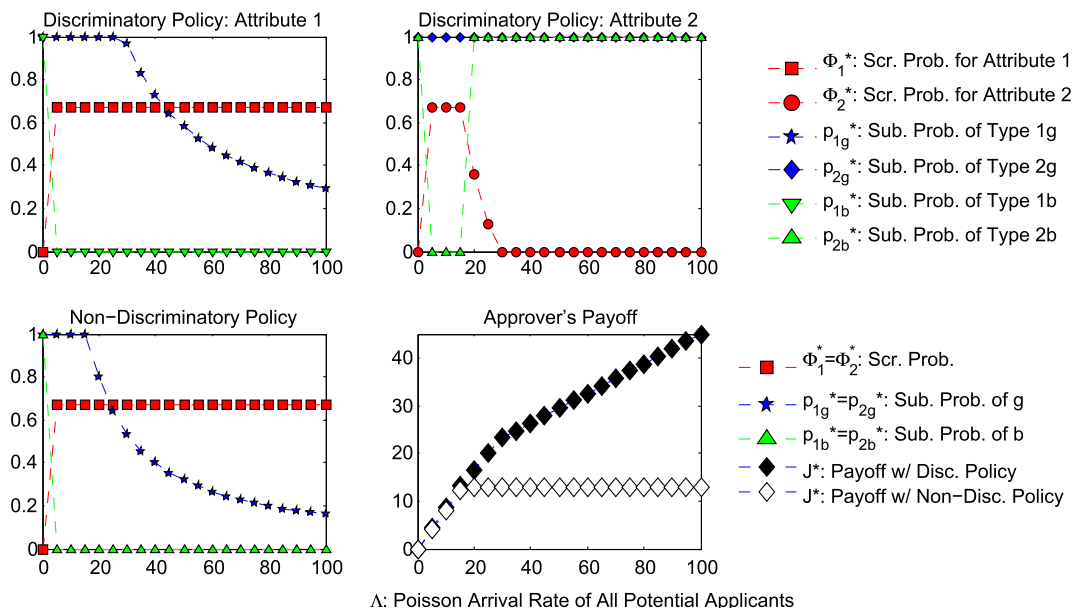


Fig. 3. Sensitivity analysis for r_b .

numerical example, there are proportionally fewer bad applicants of attribute 2 than those of attribute 1. Thus, as shown in Fig. 4, when λ is sufficiently high ($\lambda > 30$ in this example), in order to reduce congestion, the approver tends to ignore less risky applicants of attribute 2 by setting $\Phi_2 = 0$ and focus on screening more risky applicants of attribute 1 by setting screening probability Φ_1 at the threshold level $s_b \approx 0.67$. Thus, at the equilibrium, potential applicants of attribute 2 apply and get approved immediately while bad potential applicants of attribute 1 are all deterred. In addition, good potential applicants of attribute 1 will apply with a positive submission probability which decreases as congestion (λ) increases.

Second, look at the optimal non-discriminatory policy. Screening probabilities are always set high to fully deter all bad potential applicants. Similar with the discriminatory case, there are fewer good applicants as λ increases due to increased congestion.

Third, comparing the optimal discriminatory and non-discriminatory policies, we can see that the difference is small when congestion is low and the difference increases linearly with λ when congestion is high. The intuition is as follows. Under high congestion, the approver's payoff using a non-discriminatory policy stays constant as λ increases; the traffic for screening is composed only by good applicants, and their aggregate demand rate is the *desired aggregate arrival rate* which is determined by service capacity and other parameters excluding λ (see Eq. (10) when $\hat{p}_{1b} = \hat{p}_{2b} = 0$). Using a discriminatory policy, since $\Phi_1 = s_b$ and $\Phi_2 = 0$, bad potential applicants of attribute 1 are all deterred and potential applicants of attribute 2 all submit applications and are admitted without being screened. Then the traffic for screening is composed only by the good applicants of attribute 1, and their aggregate demand rate is determined by parameters excluding λ (see Eq. (10)



lambda: Poisson Arrival Rate of All Potential Applicants

Fig. 4. Sensitivity analysis for λ .

when $\Phi_2 = 0$ and $\hat{p}_{1b} = 0$). Thus using a discriminatory policy, a payoff to the approver is composed by the total reward from admitting good applicants of attribute 1 which is a constant and the total reward net of penalty from admitting applicants of attribute 2 which is linearly increasing with λ . Therefore, as λ increases, a discriminatory policy shows more advantage, which linearly increases.

6. Extensions of our model

In this section, we extend our model to the following situations: (1) screening is imperfect, i.e., there exist errors that good applicants are identified as bad and bad applicants are identified as good (subsection 6.1). (2) The approver considers that some proportion of good applicants may withdraw their applications before the approval/rejection decision, and this proportion depends on the waiting time (subsection 6.2). (3) Bad potential applicants may factor waiting costs into their submission decisions (subsection 6.3).

6.1. Imperfect screening

In this subsection we study imperfect screening. In particular, we let e_g denote the error probability that good applicants are identified as bad and let e_b denote the error probability that bad applicants are identified as good. Then the approver's objective function (1) becomes:

$$\max_{\Phi} J(\Phi) = [\lambda_{1g}(1 - e_g \Phi_1) + \lambda_{2g}(1 - e_g \Phi_2)]R - [(1 - (1 - e_b)\Phi_1)\lambda_{1b} + (1 - (1 - e_b)\Phi_2)\lambda_{2b}]C, \tag{12}$$

where the approver gets the reward R from each approved good applicant and gets the penalty C from each approved bad applicant. The potential applicant's objective function (5) becomes:

$$\max_{p_{t\theta}} u_{t\theta}(\Phi, \mathbf{p}) = \begin{cases} p_{tg}[(1 - e_g \Phi_t)r_g - \Phi_t c_w W(\Phi, \mathbf{p})] & \text{if } \theta = g, \\ p_{tb}[(1 - (1 - e_b)\Phi_t)r_b + (1 - e_b)\Phi_t(-c_b)] & \text{if } \theta = b. \end{cases} \tag{13}$$

6.1.1. Bad potential applicants' best responses

With imperfect screening, Proposition 1 becomes:

Proposition 5. Bad potential applicants' best responses are given by:

$$\hat{p}_{tb}(\Phi_t) = \begin{cases} 1, & \Phi_t < S'_b = \frac{r_b}{(1-e_b)(c_b+r_b)} \\ 0, & \Phi_t \geq S'_b = \frac{r_b}{(1-e_b)(c_b+r_b)} \end{cases} \text{ for } t = 1, 2. \tag{14}$$

Remark. Note that the error probability e_b plays an important role in imperfect screening. Compared to the perfect screening model, with imperfect screening bad potential applicants are more likely to submit their applications as the threshold probability $S'_b = \frac{r_b}{(1-e_b)(c_b+r_b)}$ is higher than that of perfect screening, $S_b = \frac{r_b}{c_b+r_b}$. When screening precision is low ($e_b > \frac{c_b}{c_b+r_b}$), $\frac{r_b}{(1-e_b)(c_b+r_b)} > 1$ and then

all bad potential applicants submit their applications no matter what the screening probability is. So in order to deter some bad potential applicants, the error probability e_b must be controlled within $[0, \frac{c_b}{c_b+r_b}]$.

6.1.2. Good potential applicants' best responses

According to the updated utility functions defined in (13), similarly as the perfect screening case, we derive the desired aggregate arrival rate of screened good potential applicants:

$$\hat{\lambda}_{1g} = \mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1 - p) \beta \lambda - \frac{\Phi_1 c_w}{(1 - e_g \Phi_1) r_g} \tag{15}$$

and

$$\hat{\lambda}_{2g} = \mu - \Phi_1 \hat{p}_{1b} p \alpha \lambda - \Phi_2 \hat{p}_{2b} (1 - p) \beta \lambda - \frac{\Phi_2 c_w}{(1 - e_g \Phi_2) r_g}. \tag{16}$$

Then we obtain the following proposition about the good potential applicants' best responses.

Proposition 6. Based on the updated expression for $\hat{\lambda}_{1g}$ and $\hat{\lambda}_{2g}$ specified in Eqs. (15) and (16), Proposition 2 still holds for the model of imperfect screening.

Remark. Note that although under perfect screening and imperfect screening, the good potential applicants' best responses have the same structure, the screened aggregate demand rates $\hat{\lambda}_{1g}$ and $\hat{\lambda}_{2g}$ are different. Due to the screening error, bad potential applicants are more likely to apply while good potential applicants are less likely to apply. So good potential applicants' submission probabilities are smaller than those under perfect screening.

6.1.3. The non-discriminatory screening policy

In the case of imperfect screening, the structure of the optimal non-discriminatory screening policy is more complex due to the impact of screening errors. To be concise, we denote $A \triangleq \mu e_g > 0$, $B \triangleq \frac{c_w}{r_g} > 0$ and define $f_-(y) \triangleq \frac{(y+A+B)\sqrt{(y+A+B)^2-4Ay}}{2e_g y}$.

Proposition 7. The approver's optimal non-discriminatory screening strategy Φ^* when screening precision is low ($e_b > \frac{c_b}{c_b+r_b}$) is specified in Table 3, in which case all bad potential applicants submit their applications ($\hat{p}_b = 1$). The approver's optimal non-discriminatory screening strategy Φ^* when screening precision is high ($e_b \leq \frac{c_b}{c_b+r_b}$) is specified in Table 4, where under certain conditions, bad potential applicants may choose not to submit their applications ($\hat{p}_b = 0$).

Remark. When $e_b > \frac{c_b}{c_b+r_b}$ (Table 3), the optimal non-discriminatory screening probability can only take one of these three values: 0, $f_-(A_b + A_g) \in (0, 1)$, or 1. Different from perfect screening, Φ^* can be zero if errors are high (small $\frac{1-e_b}{e_g}$), or the potential reward from good applicants is large relative to the potential penalty from bad applicants (high $\frac{R A_g}{C A_b}$). All bad potential applicants submit their applications, i.e., $\hat{p}_b = 1$, because they believe they are very likely to pass screening by error.

Table 3 The optimal non-discriminatory (imperfect) screening policy ($e_b > \frac{c_b}{c_b+r_b}$ and $\hat{p}_b = 1$).

Conditions	Φ^*
$f_-(A_b + A_g) > 1$ and $\frac{R A_g}{C A_b} \geq \frac{1-e_b}{e_g}$, or $f_-(A_b + A_g) \leq 1 \leq f_-(A_b)$ and $\frac{R A_g}{C A_b} \geq \max \left\{ \frac{1-e_b}{e_g}, \frac{1-e_b}{1-(1-e_g)(\mu-A_b)/A_g + \frac{c_w}{r_g}} \right\}$, or $f_-(A_b) < 1$ and $\frac{R A_g}{C A_b} \geq \frac{1-e_b}{e_g}$	0
$f_-(A_b + A_g) \leq 1 \leq f_-(A_b)$ and $\frac{R A_g}{C A_b} < \frac{1-e_b}{e_g}$ and $f_-(A_b + A_g) \geq \frac{[(1-e_g)(\mu-A_b)-A_g-\frac{c_w}{r_g}]R+(1-e_b)C A_b}{(1-e_b)C A_b - e_g R A_g}$, or $f_-(A_b) < 1$ and $f_-(A_b + A_g) \geq \frac{(1-e_b)C A_b - R A_g}{(1-e_b)C A_b - e_g R A_g}$	$f_-(A_b + A_g)$
Otherwise	1

Table 4
The optimal non-discriminatory (imperfect) screening policy ($e_b \leq \frac{c_b}{c_b+r_b}$).

Conditions	Φ^*	Notes
$0 < s'_b \leq f_-(A_b + A_g)$ and $\frac{RA_g}{CA_b} \geq \frac{1}{e_g s'_b}$, or $f_-(A_b + A_g) < s'_b \leq f_-(A_g)$ and $\frac{RA_g}{CA_b} \geq \max\{\frac{1-e_b}{e_g}, \frac{1}{e_g s'_b}\}$, or $f_-(A_g) < s'_b \leq \frac{\mu}{\mu e_g + \frac{\mu}{r_g}}$	0	$\hat{p}_b = 1$
and $\frac{RA_g}{CA_b} \geq \max\left\{\frac{1-e_b}{e_g}, \frac{A_g}{A_b - \frac{\mu}{r_b} + \mu e_g + \frac{\mu}{r_g}}\right\}$, or $\frac{\mu}{\mu e_g + \frac{\mu}{r_g}} < s'_b \leq 1$ and $\frac{RA_g}{CA_b} \geq \max\{\frac{1-e_b}{e_g}, 1\}$		
$f_-(A_g) < s'_b \leq \frac{\mu}{\mu e_g + \frac{\mu}{r_g}}$ and $\frac{RA_g}{CA_b} < \frac{1-e_b}{e_g}$ and $f_-(A_b + A_g) \geq \frac{CA_b + (\frac{\mu}{r_b} - \mu e_g - \frac{\mu}{r_g} - A_g)R}{(1-e_b)CA_b - e_g RA_g}$, or $\frac{\mu}{\mu e_g + \frac{\mu}{r_g}} < s'_b \leq 1$ and $f_-(A_b + A_g) \geq \frac{CA_b - RA_g}{(1-e_b)CA_b - e_g RA_g}$	$f_-(A_b + A_g)$	$\hat{p}_b = 1$
Otherwise	s'_b	$\hat{p}_b = 0$

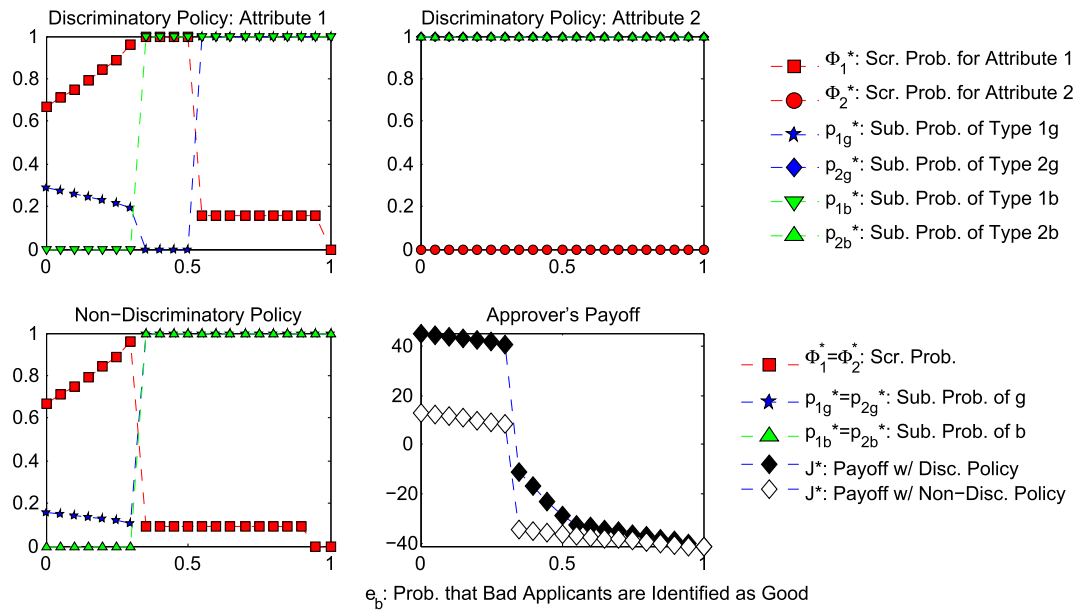


Fig. 5. Sensitivity analysis for e_b .

When $e_b \leq \frac{c_b}{c_b+r_b}$ (Table 4), the optimal non-discriminatory screening probability can only take one of these three values: 0, $f_-(A_b + A_g) \in (0, s'_b)$, or s'_b . Again, different from perfect screening, Φ^* can be zero if errors are high (small $\frac{1-e_b}{e_g}$, large $e_g s'_b$), or the potential reward from good applicants is large relative to the potential penalty from bad applicants (high $\frac{RA_g}{CA_b}$). Note that s'_b is the threshold screening probability that can deter all bad applicants. Thus when $\Phi^* = s'_b = \frac{r_b}{(1-e_b)(c_b+r_b)}$, none of the bad potential applicants submit their applications, i.e., $\hat{p}_b = 0$.

As a special case of this proposition, $RA_g < CA_b$, i.e., the loss from admitting all the bad applicants is higher than the benefit of admitting all the good applicants, and $e_g + e_b < 1$, i.e., the screening is above a certain precision level. Then $\frac{RA_g}{CA_b} < \frac{1-e_b}{e_g}$ and thus, the optimal screening probability is always above zero. This result implies that screening becomes necessary if the aggregate risk from attackers is higher than the aggregate benefit from good applicants and the overall screening error is limited within a certain range.

6.1.4. Changing error probabilities

In this subsection, we illustrate the impact of screening precision numerically. Fig. 5 shows the impact of changing e_b , the probability that bad applicants are identified as good.⁵ Interestingly, we observe non-monotonicity in this case. In particular, for

the discriminatory policy, when $0 < e_b \leq \frac{c_b}{c_b+r_b} \approx 0.33$, as e_b increases, the approver increases screening probabilities in order to make up for the losses due to wrong classification. When $0.33 < e_b \leq 0.5$, the approver already screens all applicants and high congestion has deterred all the good potential applicants. However, bad potential applicants still submit their applications because they hope to be misclassified as good applicants. When $0.5 < e_b \leq 0.95$, screening cannot function well to deter or detect bad applicants, and it can only increase congestion. So the approver decreases the screening probabilities in order to lower congestion and attract good applicants. When e_b approaches 1, the screening probabilities approaches 0, because screening becomes useless. We observe similar patterns in the case of the non-discriminatory policy. Intuitively, the approver's payoff using either a discriminatory policy or a non-discriminatory policy decreases in e_b . In addition, a discriminatory policy shows more advantage when e_b is low. As e_b increases, screening in general becomes ineffective and thus the benefit of using a discriminatory policy decreases.

Fig. 6 shows the impact of changing e_g , the error probability that good applicants are identified as bad.⁶ Since the approver's strategy, either discriminatory or non-discriminatory, does not change with e_g , the submission probabilities of bad potential applicants do not change in e_g . Then e_g only influences the submission intention of the good potential applicants; their submission probability decreases slowly as e_g increases. As a result, the benefit of using a discriminatory policy does not vary much as e_g increases.

⁵ To separate the impacts of e_g and e_b , we assume $e_g = 0$ in this case.

⁶ To separate the impacts of e_g and e_b , we assume $e_b = 0$ in this case.

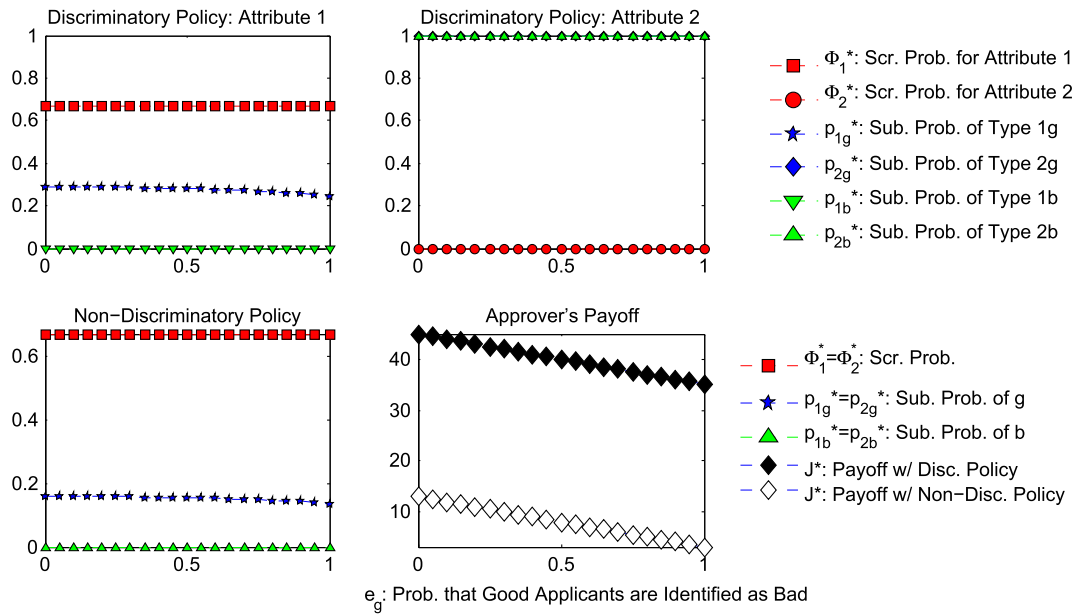


Fig. 6. Sensitivity analysis for e_g .

6.2. Non-zero abandon rate for good applicants

Now we study the scenario that good applicants could abandon the queue due to long waiting time. For example, in the visa context, after months of waiting, good applicants could give up and go elsewhere. This will change the objective function of the approver as the approver would optimally invest the screening effort expecting some approved applicants might not be available to come. To model this scenario, we define the abandon rate, $A(W)$, as the percentage of good applicants who abandon the queue before the screening process ends. $A(W) \in (0, 1]$ is a non-decreasing function of the expected waiting time W . Thus, the approver's objective function (1) becomes:

$$J(\Phi) = [1 - A(W)](\lambda_{1g} + \lambda_{2g})R - [(1 - \Phi_1)\lambda_{1b} + (1 - \Phi_2)\lambda_{2b}]C. \tag{17}$$

In our numerical experiments, we use a specific functional form, $A(W) = 1 - \exp(-\gamma * W)$, where $\gamma \geq 0$ measures the good applicants' intention to abandon the queue. When $\gamma = 0$, we have the same results as presented in previous sections. As shown in Fig. 7, for both discriminatory and non-discriminatory policies, when γ increases, good applicants are more sensitive to congestion and thus the approver gets a lower reward from the good applicants who stay until screening ends. To alleviate congestion, the approver increases screening probabilities to deter all of the bad potential applicants and some of the good

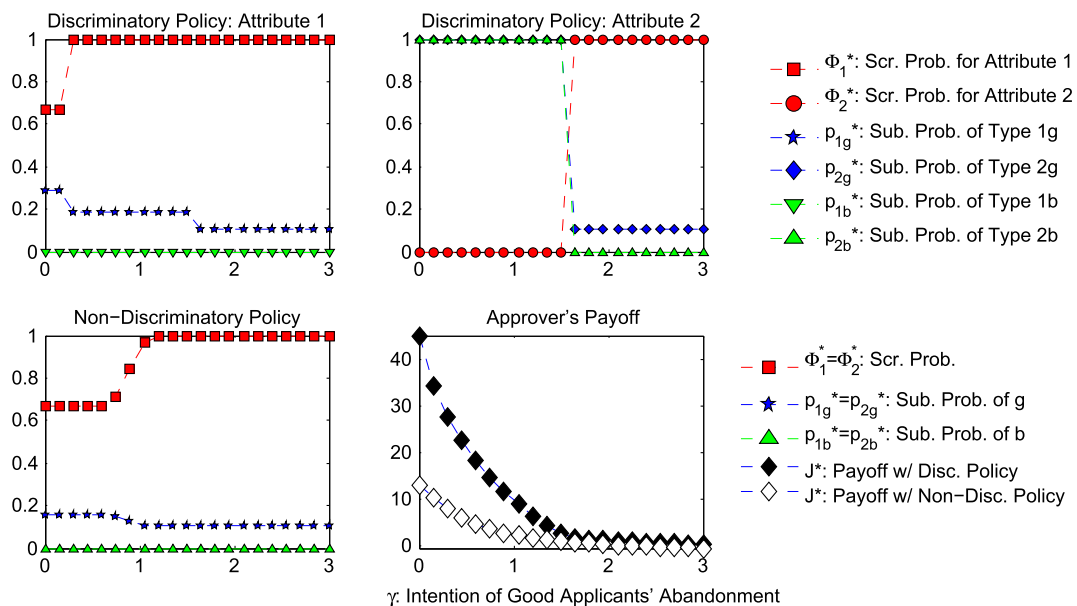


Fig. 7. Sensitivity analysis for γ .

potential applicants. As a result, the benefit of using a discriminatory policy decreases in γ until it approaches zero when γ approaches infinity.

6.3. Non-zero waiting costs for bad applicants

In this subsection, we assume bad applicants have non-zero waiting costs in the screening process. In particular, the bad potential applicant's expected utility in Eq. (4) becomes:

$$u_{tb}(\Phi, \mathbf{p}) = p_{tb}[\Phi_t(-c_b) + (1 - \Phi_t)r_b - \Phi_t b_w W(\Phi, \mathbf{p})],$$

for $t \in \{1, 2\}$, (18)

where b_w is the bad applicant's cost per unit of waiting time and when $b_w = 0$, we have the baseline results same as presented in previous sections. From Fig. 8, we have the following observations. The impact of increasing b_w is similar to that of decreasing the threshold screening probability s_b , because the more sensitive to congestion, the less likely bad potential applicants submit their applications. For example, in the case of the discriminatory policy, when $0 < b_w < 1$, although the screening probability Φ_1 is very low, bad potential applicants of attribute 1 are deterred due to their sensitivity to congestion. When $1 \leq b_w < 2.5$, as b_w increases, although the screening probability Φ_2 decreases, bad potential applicants of attribute 2 are deterred because a higher b_w implies a lower threshold deterring all bad applicants. When $b_w \geq 2.5$, bad potential applicants of both attributes are deterred due to high waiting costs. In the case of the non-discriminatory policy, the optimal screening probability is always set at the threshold to deter bad applicants and thus we see clearly this threshold (the optimal screening probability) is non-increasing in b_w . Note that when $b_w \geq 1.8$, the optimal screening probability is constantly at a low value. This is because all good applicants submit their applications, all bad one are deterred, and the approver's payoff already reaches its upper bound. So the approver has no incentive to further decrease the screening probability. Finally, comparing the discriminatory and non-discriminatory policies, we observe that the benefit of using a discriminatory policy is large when b_w is small, and it is very small when b_w is large. This again indicates that a discriminatory policy shows more advantage when the approver has more difficulties in balancing congestion and security risk.

7. Conclusion and future research directions

In this paper we study the approver's optimal screening policies facing strategic potential applicants with private information. We provide analytical solutions for the optimal non-discriminatory screening policy and numerical illustrations for both the discriminatory and non-discriminatory policies. We find that although the optimal discriminatory screening policy is always better than the optimal non-discriminatory policy, the benefit of using a discriminatory screening policy is not significant when the tension between congestion and security risk is not intensive. These situations include: congestion is low (total potential arrival rate is low, or the service rate is high), or the approver's reward from admitting a good applicant (or penalty from admitting a bad applicant) is very high or very low, or the bad potential applicant has a low incentive to apply (low reward if passed, or high penalty if caught, or high cost per unit of waiting time), or the screening error is high. In those cases, a non-discriminatory policy might be more appropriate in practice.

For future research, more elaborate decision models could be developed. First, this paper assumes that the parameters of the models are common knowledge, as most game-theoretic models do (Mas-Colel et al., 1995). However, in practice the approver and potential applicants may not know the system parameters, and thus a model with information would be an interesting direction. Second, this paper assumes that different types of screened applicants join a single queue, while alternatively, in the screening process different resources (multiple servers) could be used for different applicants with different observable characteristics; and as a result the waiting time performance could be different for applicants with different characteristics. Third, the service rate could be increased at a cost and thus optimization could be introduced to minimize the total costs. Finally, in our model we do not consider the fact that in some cases bad applicants of one attribute could pretend to be of the other attribute, in order to receive lower screening probabilities. For example, the bad applicants of attribute 1 could in principle pretend to be of attribute 2 to receive zero screening probabilities in the baseline scenario, as long as such deception is not too costly; (see Zhuang and Bier, 2011; Zhuang et al., 2010; Zhuang and Bier, 2010 for the role deception in

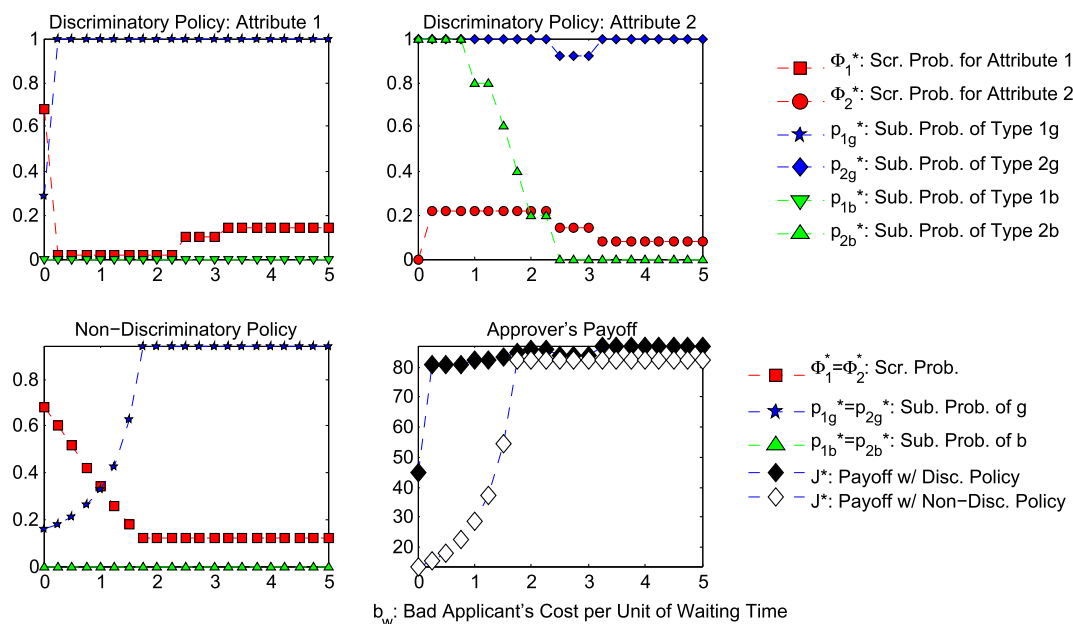


Fig. 8. Sensitivity analysis for b_w .

sequential games). In this situation, we expect that the discriminatory screening policy would become less effective, which again justifies the non-discriminatory policy.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.ejor.2011.01.019.

References

- Anand, Krishnan, Fazil Pac, M., Veeraraghavan, Senthil K., 2011. Quality-speed conundrum: Trade-offs in customer-intensive services. *Management Science* 57 (1), 40–56.
- Babu, V.L.L., Batta, R., Lin, L., 2006. Passenger grouping under constant threat probability in an airport security system. *European Journal of Operational Research* 168 (2), 633–644.
- Bagla, P., 2006. Science and diplomacy – Indian chemist receives a visa and an apology. *Science* 311 (5765), 1229.
- Bakshi, N., Gans, N., 2010. Securing the containerized supply chain: Analysis of government incentives for private investment. *Management Science* 56 (2), 219–233.
- Bakshi, N., Flynn, S.E., Gans, N., 2009. Estimating the Operational Impact of Container Inspections at International Ports. University of Pennsylvania.
- Balachandran, K.R., Schaefer, M.E., 1980. Public and private optimization at a service facility with approximate information on congestion. *European Journal of Operational Research* 4 (3), 195–202.
- Basuchoudhary, A., Razzolini, L., 2006. Hiding in plain sight – Using signals to detect terrorists. *Public Choice* 128 (1–2), 245–255.
- Bhattacharjee, Y., 2004a. US immigration – Groups urge easing of restrictions on visa policies affecting scientists. *Science* 304 (5673), 943.
- Bhattacharjee, Y., 2004b. U.S. visa policy – Foreign scholars to get longer clearance. *Science* 305 (5688), 1222.
- Bier, V.M., Haphuriwat, N., in press. Analytical method to identify the number of containers to inspect at U.S. ports to deter terrorist attacks. *Annals of Operations Research*. <<http://www.springerlink.com/content/817ju81220214027/>>. doi:10.1007/s10479-009-0665-6.
- Blalock, G., Kadiyali, V., Simon, D.H., 2007. The impact of post-9/11 airport security measures on the demand for air travel. *Journal of Law & Economics* 50 (4), 731–755.
- Cavusoglu, Huseyin, Koh, Byungwan, Raghunathan, Srinivasan, 2010. An analysis of the impact of passenger profiling for transportation security. *Operations Research* 58 (5), 1287–1302.
- Claeys, D., Walraevens, J., Laevens, K., Bruneel, H., 2010. A queueing model for general group screening policies and dynamic item arrivals. *European Journal of Operational Research* 207 (2), 827–835.
- Fisher, W., 2010. Civil liberties groups say new TSA screening measures are discriminatory. *The Public Record*. <<http://pubrecord.org/nation/6514/civil-liberties-groups-screening/>> (accessed on 19.11.10).
- Gilliam, R.R., 1979. Application of queuing theory to airport passenger security screening. *Interfaces* 9 (4), 117–123.
- Golalikhani, M., Zhuang, J., forthcoming. Modeling arbitrary layers of continuous level defenses in facing with a strategic attackers. *Risk Analysis*. <<http://onlinelibrary.wiley.com/doi/10.1111/j.1539-6924.2010.01531.x/abstract>>. doi:10.1111/j.1539-6924.2010.01531.x.
- Golany, B., Kaplan, E.H., Marmur, A., Rothblum, U.G., 2009. Nature plays with dice? terrorists do not: Allocating resources to counter strategic versus probabilistic risks. *European Journal of Operational Research* 192 (1), 198–208.
- Hassin, R., Haviv, M., 2003. To Queue or not to Queue: Equilibrium Behavior in Queueing Systems. Kluwer Academic Publishers, Boston/Dordrecht/London.
- Lipton, E., 2010. U.S. intensifies air screening for fliers from 14 nations. *The New York Times*. <<http://www.nytimes.com/2010/01/04/us/04webtsa.html>> (accessed on 19.11.10).
- Mas-Colel, A., Whinston, M.D., Green, J.R., 1995. *Microeconomic Theory*. Oxford University Press, New York.
- McLay, Laura A., Jacobson, Sheldon H., Kobza, John E., 2006. A multilevel passenger screening problem for aviation security. *Naval Research Logistics* 53 (3), 183–197.
- Nie, X., Batta, R., Drury, C.G., Lin, L., 2009. Passenger grouping with risk levels in an airport security system. *European Journal of Operational Research* 194 (2), 574–584.
- Ross, S.M., 2002. *Introduction to Probability Models*. Academic Press, San Diego, CA.
- Seife, C., Ding, Y.M., 2003. High-energy physics: Visa delay foils Chinese delegation. *Science* 301 (5636), 1026.
- Stone, R., 2008. Technical exchanges: U.S. visa delays on the rise, scientists abroad report. *Science* 322 (5905), 1172–1173.
- US Government Accountability Office., 2004. Border security: Improvements needed to reduce time taken to adjudicate visas for science students and scholars. GAO-04-371.
- Viaene, S., Ayuso, M., Guillen, M., Van Gheel, D., Dedene, G., 2007. Strategies for detecting fraudulent claims in the automobile insurance industry. *European Journal of Operational Research* 176 (1), 565–583.
- Yetman, J., 2004. Suicidal terrorism and discriminatory screening: An efficiency-equity trade-off. *Defence and Peace Economics* 15 (3), 221–230.
- Zhuang, J., Bier, V.M., 2007. Balancing terrorism and natural disasters – Defensive strategy with endogenous attacker effort. *Operations Research* 55 (5), 976–991.
- Zhuang, J., Bier, V.M., 2010. Reasons for secrecy and deception in homeland-security resource allocation. *Risk Analysis* 30 (12), 1737–1743.
- Zhuang, J., Bier, V.M., 2011. Secrecy and deception at equilibrium, with applications to anti-terrorism resource allocation. *Defence and Peace Economics* 22 (1), 43–61.
- Zhuang, J., Bier, V.M., Alagoz, O., 2010. Modeling secrecy and deception in a multiple-period attacker-defender signaling game. *European Journal of Operational Research* 203 (2), 409–418.