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# Probabilistic Evaluation of Liquefaction Potential

by

H.H.M. Hwang and C.S. Lee

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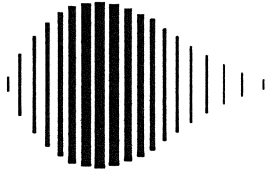
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H.H.M. Hwang<sup>1</sup> and C.S. Lee<sup>2</sup>

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- 1 Professor, Center for Earthquake Research and Information, Memphis State University
- 2 Research Associate, Center for Earthquake Research and Information, Memphis State University

NATIONAL CENTER FOR EARTHQUAKE ENGINEERING RESEARCH  
State University of New York at Buffalo  
Red Jacket Quadrangle, Buffalo, NY 14261

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## PREFACE

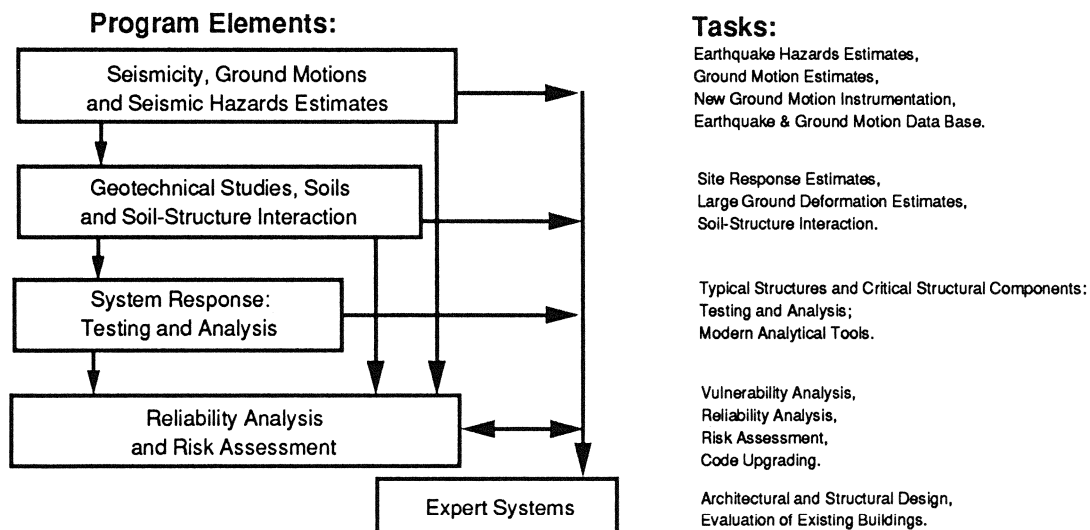
The National Center for Earthquake Engineering Research (NCEER) is devoted to the expansion and dissemination of knowledge about earthquakes, the improvement of earthquake-resistant design, and the implementation of seismic hazard mitigation procedures to minimize loss of lives and property. The emphasis is on structures and lifelines that are found in zones of moderate to high seismicity throughout the United States.

NCEER's research is being carried out in an integrated and coordinated manner following a structured program. The current research program comprises four main areas:

- Existing and New Structures
- Secondary and Protective Systems
- Lifeline Systems
- Disaster Research and Planning

This technical report pertains to Program 1, Existing and New Structures, and more specifically to geotechnical studies.

The long term goal of research in Existing and New Structures is to develop seismic hazard mitigation procedures through rational probabilistic risk assessment for damage or collapse of structures, mainly existing buildings, in regions of moderate to high seismicity. The work relies on improved definitions of seismicity and site response, experimental and analytical evaluations of systems response, and more accurate assessment of risk factors. This technology will be incorporated in expert systems tools and improved code formats for existing and new structures. Methods of retrofit will also be developed. When this work is completed, it should be possible to characterize and quantify societal impact of seismic risk in various geographical regions and large municipalities. Toward this goal, the program has been divided into five components, as shown in the figure below:



Geotechnical studies constitute one of the important areas of research in Existing and New Structures. Current research activities include the following:

1. Development of linear and nonlinear site response estimates.
2. Development of liquefaction and large ground deformation estimates.
3. Investigation of soil-structure interaction phenomena.
4. Development of computational methods.
5. Incorporation of local soil effects and soil-structure interaction into existing codes.

The ultimate goal of projects concerned with geotechnical studies is to develop methods of engineering estimation of large soil deformations, soil-structure interaction, and site response.

*The purpose of this report is to develop a probabilistic method for evaluating the liquefaction potential of a saturated sand site. The method is applied to a site in Memphis, which is close to the New Madrid seismic zone. The procedure is based on an evaluation of the liquefaction potential index of a site  $P_L$  as proposed by Iwasaki. Regional seismicity and local site conditions are incorporated through relevant models. Liquefaction potential probability matrix and fragility curves are constructed by including uncertainties in the site parameters (relative density and shear modulus) as well as in various seismic parameters.*

## ABSTRACT

A probabilistic method for evaluating liquefaction potential of a site is presented and illustrated by using a site at President Island, Memphis, Tennessee, which is close to the New Madrid seismic zone. In this method, the liquefaction potential of a soil layer is estimated by using the factor of safety  $F_L = R/L$ . The earthquake-induced shear stress ratio  $L$  is determined from nonlinear site response analysis. On the other hand, the resistance shear stress ratio (or cyclic shear strength)  $R$  is determined from cyclic test data based on the equivalent uniform cycles  $N_{eq}$  and relative density  $D_r$ . The  $F_L$  value together with depth and thickness of each liquefied layer is used to calculate the liquefaction potential index of a site  $P_L$  as proposed by Iwasaki et al. (1982). The  $P_L$  value indicates the liquefaction severity of a site: no or little liquefaction ( $P_L = 0$ ), minor liquefaction ( $0 < P_L \leq 5$ ), moderate liquefaction ( $5 < P_L \leq 15$ ), and major liquefaction ( $P_L > 15$ ).

By including uncertainties in site parameters (relative density and shear modulus) and seismic parameters (stress drop, strong-motion duration, and random phase angles), 81 earthquake-site models are established. Given a moment magnitude, the probabilities of no, minor, moderate, and major liquefaction can be determined from the analyses of these earthquake-site samples. By repeating the same procedure for other moment magnitudes, the liquefaction potential probability matrix and the fragility curves can be constructed. The proposed method incorporates the local site conditions and regional seismicity in the evaluation of liquefaction potential of a site. In addition, uncertainties in seismic and site parameters can be easily included in the analysis.



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## SECTION 1

### INTRODUCTION

The catastrophic failures of structures and consequent loss of human lives due to soil liquefaction in the 1964 Niigata earthquake [1,2] have created an awareness of the danger posed by earthquake-induced liquefaction. The threat is especially imminent for sites with loose sandy soil conditions and for inadequately-compacted hydraulic fills.

The liquefaction potential of a saturated sand site is affected by site parameters such as relative density, percentage of clay, and effective confining pressure. In addition, it is also affected by seismic parameters such as the magnitude, frequency content, and duration of an earthquake. Hence, an analytical approach that incorporates the local site conditions and regional seismicity to evaluate the liquefaction potential of a site is desirable. By using the analytical method, uncertainties in seismic and site parameters can be easily included in the analysis. In this study, a probabilistic method for evaluating liquefaction potential of a site is presented and illustrated by using a site at President Island, Memphis, Tennessee, which is close to the New Madrid seismic zone (NMSZ).

The dynamic soil model for nonlinear site response analysis is established based on actual boring logs. Because of the uncertainties in relative density and shear modulus, nine site models are established. A seismologically based model that takes into account source mechanism, path attenuation, and soft-rock effects is used to generate the horizontal earthquake time

histories at the base of the soil column. The uncertainties in seismic parameters, stress drop, strong-motion duration, and random phase angles are considered in this study. From the combinations of representative values of seismic and site parameters, 81 earthquake-site samples are established for nonlinear site response analysis.

The liquefaction potential of a soil layer is estimated by using the factor of safety  $F_L = R/L$ . The earthquake-induced shear stress ratio  $L$  is determined from nonlinear site response analysis and is taken as the average shear stress ratio. The irregular shear stress time history for each liquefiable layer is converted into equivalent uniform cycles  $N_{eq}$  at the average shear stress ratio based on the procedure proposed by Seed et al. [3]. By using the equivalent uniform cycles  $N_{eq}$  and relative density  $D_r$ , the resistance shear stress ratio  $R$  is determined from cyclic test data. The  $F_L$  value together with depth and thickness of each liquefied layer is used to evaluate the liquefaction potential index of a site  $P_L$  proposed by Iwasaki et al. [4]. The  $P_L$  value indicates the liquefaction severity of a site: no or little liquefaction ( $P_L = 0$ ), minor liquefaction ( $0 < P_L \leq 5$ ), moderate liquefaction ( $5 < P_L \leq 15$ ), and major liquefaction ( $P_L > 15$ ).

For an earthquake with a given moment magnitude, the probabilities of no, minor, moderate, and major liquefaction can be determined from the analyses of 81 earthquake-site samples. The earthquake-induced liquefaction potential probability matrix and the fragility curves [5] can be constructed by repeating the same procedure for earthquakes with various moment magnitudes.

In this report, Section 2 describes the nonlinear site response analysis and the uncertainties in seismic and site parameters. Section 3 presents the method for evaluating the factor of safety against liquefaction for a potentially liquefiable layer and the liquefaction potential index of a site, while Section 4 presents the probabilistic method for constructing the liquefaction potential probability matrix and fragility curves. The results from the proposed method and those obtained by using the simplified approach suggested by Seed and Idriss [6,7] are compared in Section 5. Finally, Section 6 presents the conclusions of this study.



## SECTION 2

### NONLINEAR SITE RESPONSE ANALYSIS

It is generally acknowledged that soil liquefaction in saturated cohesionless soils during an earthquake is caused by the buildup of excess pore pressure due to the cyclic shear stress induced by ground shaking [7]. In this study, the cyclic shear stresses in a soil deposit are evaluated by performing nonlinear site response analysis using the MASH computer program [8]. The dynamic soil model in the MASH program consists of a horizontally multi-layered soil profile that extends to a fixed base. The input earthquake acceleration time histories at the base of the soil profile are synthetic earthquakes generated from a seismologically based model, in which the source mechanism, path attenuation, and soft-rock effects are taken into consideration.

#### 2.1 Dynamic Soil Model

The existing boring log of the selected site at President Island is shown in figure 2-1. The water table of the site is about 2.5 m to 3.0 m below the ground level. Because of the capillary action of water and the silt content of the shallow soil, the top layer is considered saturated. The soil at the depth of 60 m is very stiff and thus the base of the soil profile is selected at this level. The actual bedrock (hard-rock) in the Memphis area is about 909 m below the ground level. The material between 60 m and 909 m is denoted as soft-rock and its effects on the earthquake motions are included in the input synthetic earthquake time history. Figure 2-1 also

Depth (m)

0		MEDIUM DENSE SM-SP	
2.9	$\gamma_s = 19.6 \text{ kN/m}^3$	$D_r = 0.502, 0.668, 0.761$	NSPT = 7-16
5.5	$\gamma_s = 19.6 \text{ kN/m}^3$	STIFF ML-CL $PI = 10-20$	$S_u = 89.7 \text{ kN/m}^2$ NSPT = 15
11.6	$\gamma_s = 18.9 \text{ kN/m}^3$	MEDIUM DENSE SM-SC $D_r = 0.423, 0.511, 0.588$	NSPT = 9-17
17.7	$\gamma_s = 19.6 \text{ kN/m}^3$	MEDIUM DENSE SP $D_r = 0.405, 0.521, 0.618$	NSPT = 11-25
19.2	$\gamma_s = 21.2 \text{ kN/m}^3$	DENSE SP-GP $D_r = 0.713, 0.757, 0.786$	NSPT = 40-49
23.2	$\gamma_s = 20.4 \text{ kN/m}^3$	STIFF CL $PI = 20-40$	$S_u = 95.8 \text{ kN/m}^2$ NSPT = 16
27.5	$\gamma_s = 21.2 \text{ kN/m}^3$	DENSE SP $D_r = 0.90$	
29.3	$\gamma_s = 20.4 \text{ kN/m}^3$	VERY STIFF CL $PI = 20-40$	$S_u = 119.7 \text{ kN/m}^2$
36.9	$\gamma_s = 21.2 \text{ kN/m}^3$	DENSE SC $D_r = 0.84$	
46.4	$\gamma_s = 22.0 \text{ kN/m}^3$	VERY DENSE SP $D_r = 0.925$	
53.4	$\gamma_s = 20.4 \text{ kN/m}^3$	VERY STIFF CL $PI = 20-40$	$S_u = 192.0 \text{ kN/m}^2$
60.0	$\gamma_s = 20.4 \text{ kN/m}^3$	VERY STIFF CL $PI = 20-40$	$S_u = 215.4 \text{ kN/m}^2$

FIGURE 2-1 Soil Profile of a Site at President Island

shows the basic soil properties such as total unit weights  $\gamma_s$  of both sand and clay, plasticity index PI of clay, and the range of standard penetration test blowcounts  $N_{SPT}$  obtained from existing boring logs. The relative density for sand  $D_r$ , which has significant effects on the soil liquefaction potential, is estimated from the corrected standard penetration test blowcount  $(N_1)_{60}$  based on the relationship suggested by Tokimatsu and Seed [9] (figure 2-2).  $(N_1)_{60}$  is obtained by normalizing the  $N_{SPT}$  value to an effective overburden pressure of 1 tsf (95.8 kN/m<sup>2</sup>) and an effective energy delivered to the drill rod at 60% of the ideal free-fall energy [10].

$$(N_1)_{60} = C_N \times C_F \times N_{SPT} \quad (2.1)$$

where  $C_F$  is a factor for correcting percentage of energy delivered to the drill rod.  $C_F$  is equal to 1.0 for rope and pulley type and 0.85 for donut type.  $C_N$  is a factor for correcting the overburden pressure.

$$C_N = 1 - 1.25 \log \left( \frac{\sigma'_0}{\sigma_1} \right) \quad (2.2)$$

where  $\sigma_1$  is equal to 1 tsf (95.8 kN/m<sup>2</sup>) and  $\sigma'_0$  is the effective vertical confining (overburden) pressure.

### 2.1.1 Hysteretic Behavior

Soil exhibits pronounced nonlinear behavior under cyclic loadings. The secant shear modulus  $G$  is strain-dependent and decreases with increasing

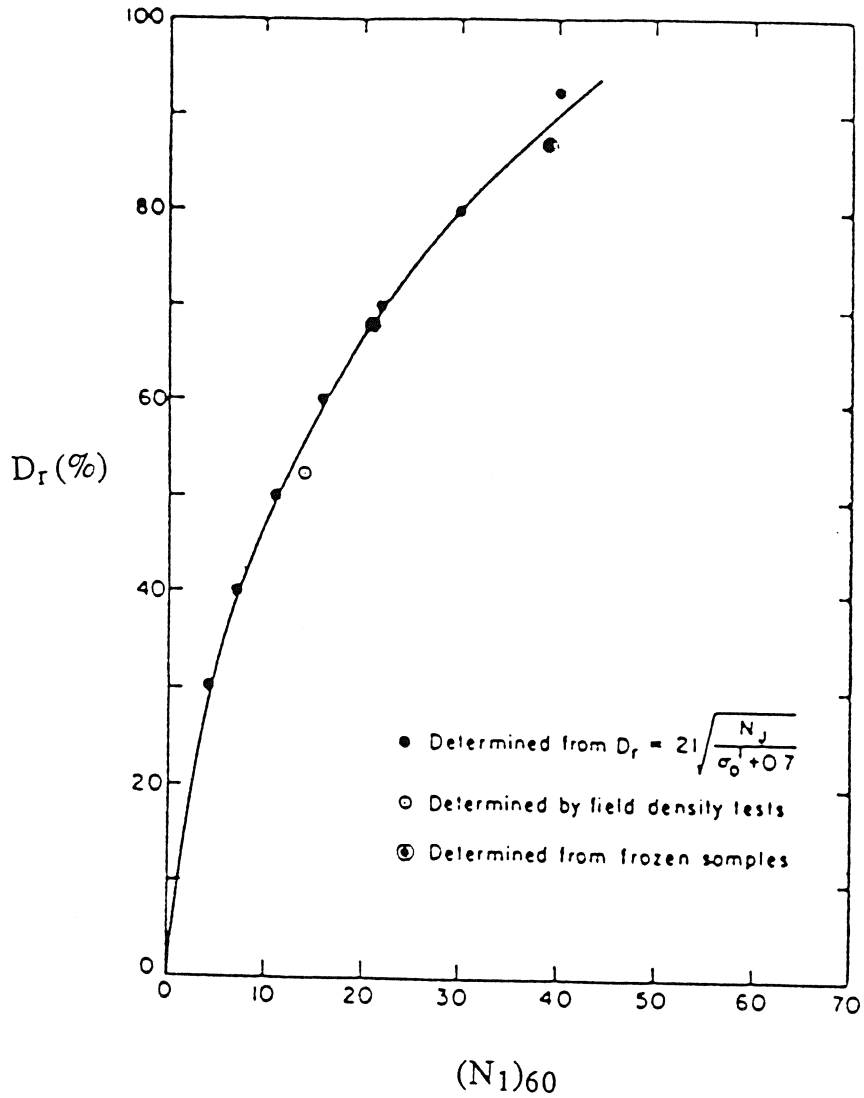


FIGURE 2-2 Relationship Between Relative Density and (N1)60 (after Tokimatsu and Seed 1986)

shear strain  $\gamma$ . In the MASH program, the secant shear modulus is expressed as

$$\frac{G}{G_0} = 1 - \left[ \frac{[\gamma/\gamma_0]^{2B}}{1 + [\gamma/\gamma_0]^{2B}} \right]^A \quad (2.3)$$

where  $G_0$  is the low-strain shear modulus;  $\gamma_0$  is the reference strain; and A and B are two parameters that define the shape of the shear modulus reduction curve.

The secant shear modulus for sand is affected primarily by the confining pressure and relative density [11-14]. The low-strain shear modulus  $G_0$  is usually taken as the shear modulus corresponding to a strain level of  $10^{-6}$  or less. In the MASH program,  $G_0$  in psf is estimated from the following empirical equation [8]:

$$G_0 = 61000 [1 + 0.01 (D_r - 75)] (\bar{\sigma})^{1/2} \quad (2.4)$$

where  $D_r$  is the relative density in percentage and  $\bar{\sigma}$  is the average effective confining pressure in psf.

The reference strain  $\gamma_0$  is expressed as

$$\gamma_0 = \frac{\tau_{\max}}{G_0} \quad (2.5)$$

where  $\tau_{\max}$  is the maximum shear stress under dynamic loadings and is computed using the formula suggested by Hardin and Drnevich [15].

The parameters A and B in equation (2.3) define the shape of the shear modulus reduction curve. Hwang and Lee [16] determined the values of A and B for sand based on experimental data available in the literature (figure 2-3). The parameters A and B corresponding to the mean, mean plus one standard deviation (SD), and mean minus one SD curves are shown in table 2-I. The lower and upper bound values are also included in the table. On the basis of these parameters values, the shear modulus reduction curves for sand are shown in figure 2-3.

Table 2-I Parameter Values of A and B for Sand

Curves	A	B
Lower	0.509	0.480
Mean - SD	0.705	0.445
Mean	0.941	0.441
Mean + SD	1.268	0.446
Upper	1.775	0.489

Several studies [17-19] have indicated that the plasticity index PI is the dominant factor affecting the shape of shear modulus reduction curve for clay. In general, as the plasticity index of clay increases, the shear modulus reduction curve gradually shifts to the right, indicating a small reduction of shear modulus with increasing plasticity index at the same strain level.

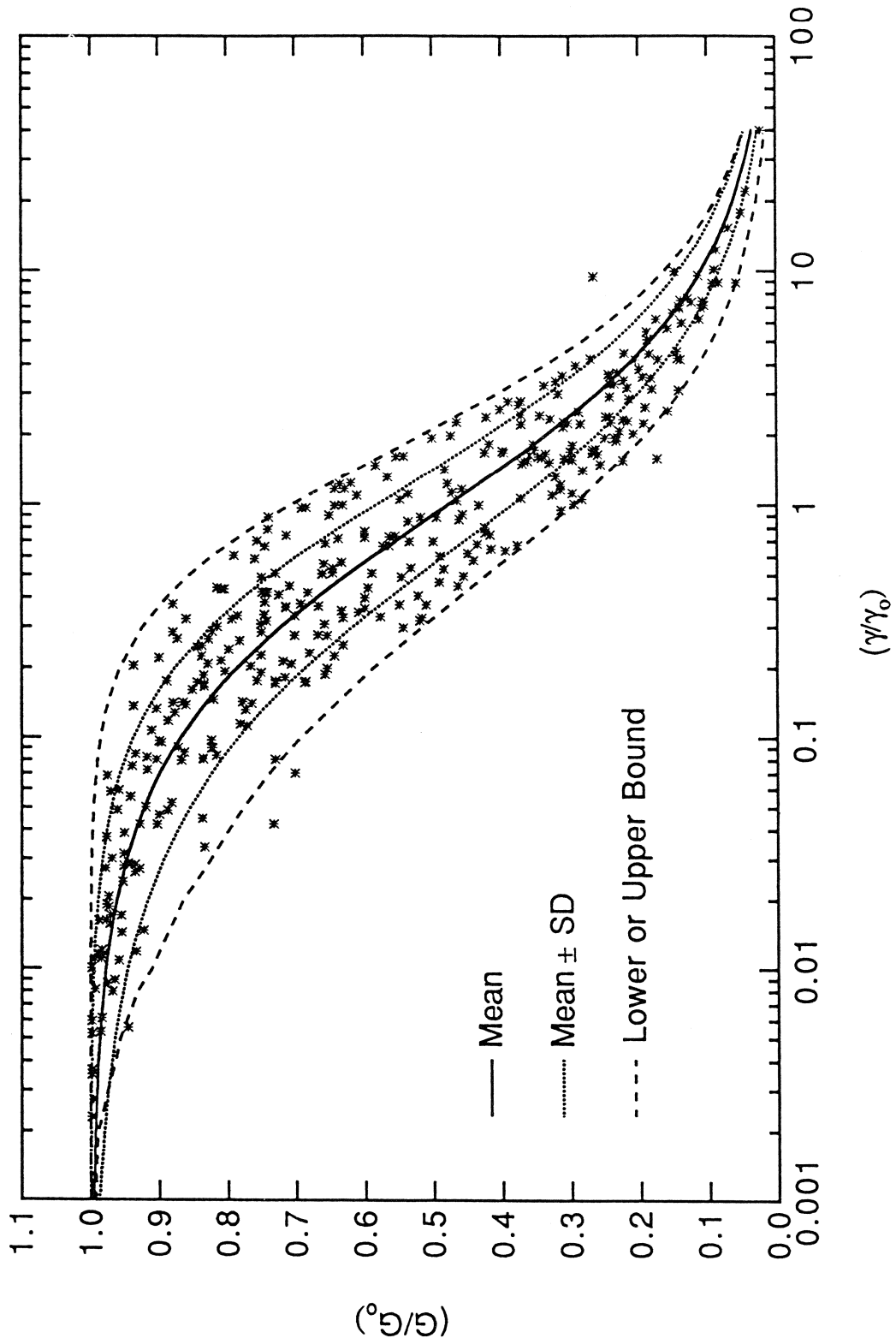


FIGURE 2-3 Shear Modulus Reduction Curves for Sand

The low-strain shear modulus  $G_0$  for clay in the MASH program is computed as [8]

$$G_0 = 2500 S_u \quad (2.6)$$

where  $S_u$  is the undrained shear strength of clay. In this study,  $\tau_{max}$  is taken as  $S_u$  and  $G_0$  is taken as  $2500 S_u$ ; thus, the reference strain  $\gamma_0$  is equal to 0.0004.

Figure 2-4 shows the shear modulus reduction curves for clay corresponding to different ranges of plasticity indices suggested by Sun et al. [19]. The parameters A and B corresponding to these curves determined from nonlinear regression analyses by Hwang and Lee [16] are listed in table 2-II.

Table 2-II Parameter Values of A and B for Clay

PI	Curve	A	B
5-10	Mean	1.026	0.458
10-20	Mean	1.464	0.433
20-40	Mean	1.838	0.376
40-80	Mean	2.197	0.330
> 80	Mean	2.591	0.268

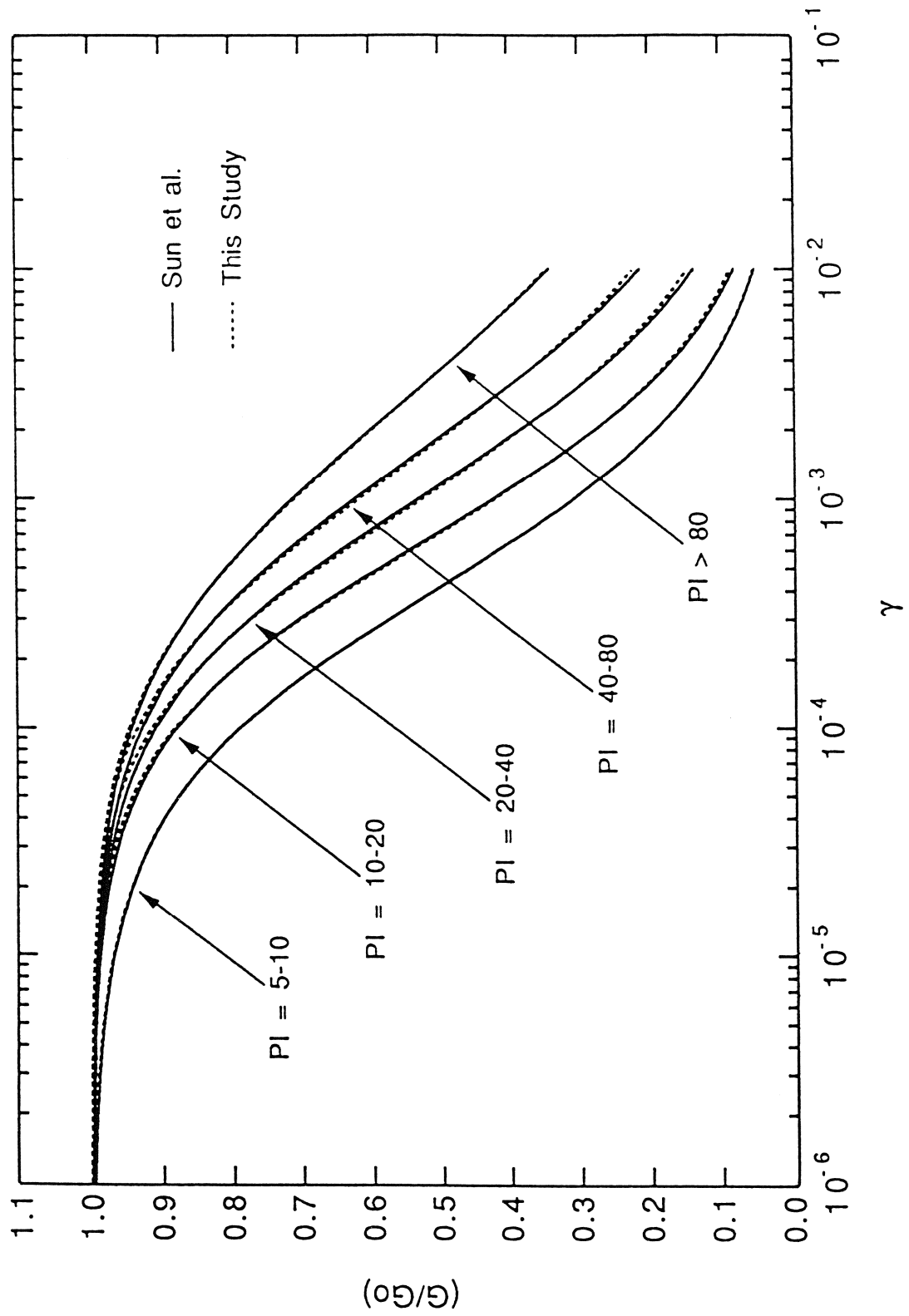


FIGURE 2-4 Shear Modulus Reduction Curves for Clay

### 2.1.2 Uncertainties in Site Parameters

From reviewing existing boring logs of the selected site, the clayey silts and silty clays are found to have a high clay content (>15%). These types of soils are not likely to liquefy in the event of an earthquake [7]. Thus, only sandy soils are considered potentially liquefiable in this study. For each liquefiable soil layer, uncertainties in two site parameters (relative density  $D_r$  and shear modulus  $G$ ) are included in the probabilistic analysis.

The relative density  $D_r$  of a soil layer is estimated based on the corrected standard penetration test blowcount  $(N_1)_{60}$ , which in turn is computed from the  $N_{SPT}$  value. Thus, uncertainty in the  $D_r$  value is determined based on the range of  $N_{SPT}$  values established from the existing boring logs. Three  $D_r$  values (lower, mean, and upper) are estimated as shown in figure 2-1. These  $D_r$  values together with three pairs of parameters A and B (mean - SD, mean, and mean + SD) are used to quantify the uncertainty in shear modulus  $G$ . Thus, nine dynamic soil models are constructed as shown in table 2-III.

Table 2-III Parameters of Site Models

Site Model	Relative Density	Shear Modulus
1	Lower	Lower
2	Mean	Lower
3	Upper	Lower
4	Lower	Mean
5	Mean	Mean
6	Upper	Mean
7	Lower	Upper
8	Mean	Upper
9	Upper	Upper

## 2.2 Input Base Motions

Seismic hazards in Memphis, Tennessee, are entirely dominated by the New Madrid seismic zone (NMSZ) (figure 2-5). In this study, the seismic source of hypothetical New Madrid earthquakes is assumed at Marked Tree, Arkansas, which is near the southern end of the NMSZ. The epicentral distance from the seismic source to the site at President Island is about 57 km. Both seismic source and the site are indicated in figure 2-5. In this study, a seismologically based model is used to generate synthetic acceleration time histories. This model is briefly described below.

Seismicity in the New Madrid Seismic Zone: 1974-1990

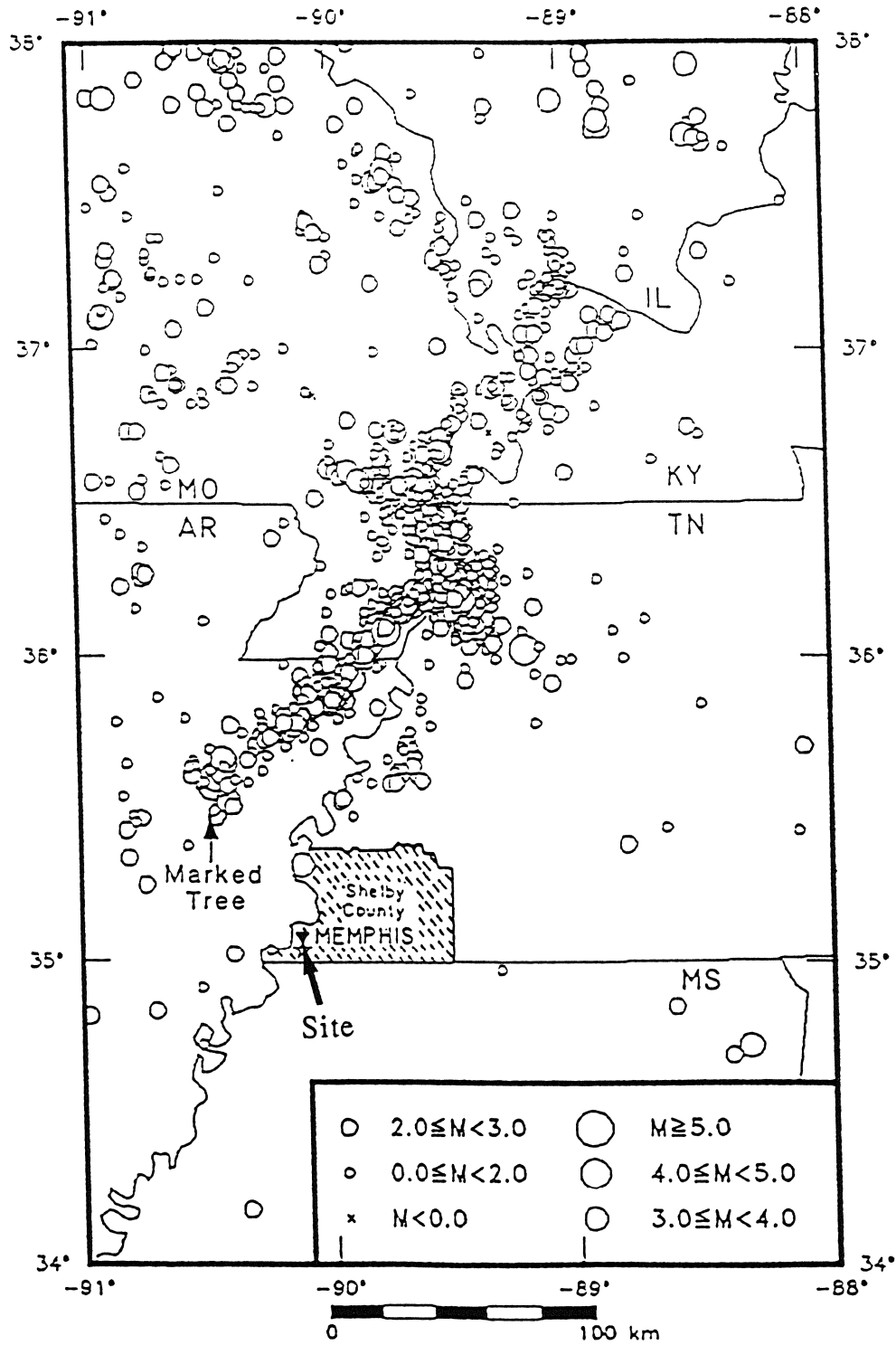


FIGURE 2-5 Locations of Seismic Source and Site

### 2.2.1 Fourier Acceleration Amplitude Spectrum

The Fourier acceleration amplitude spectrum at the base of a soil profile is expressed as follows [20-22]:

$$A(f) = C \times S(f) \times D(f) \times AF(f) \quad (2.7)$$

where  $C$  is a scaling factor;  $S(f)$  is a source spectral function;  $D(f)$  is a diminution function; and  $AF(f)$  is an amplification factor.

The source spectral function  $S(f)$  used in this study is a  $\omega^2$  source acceleration spectrum proposed by Brune [23]. The source spectrum is expressed in terms of the corner frequency  $f_0$  and seismic moment  $M_0$ :

$$S(f) = (2\pi f)^2 \frac{M_0}{1 + \left(\frac{f}{f_0}\right)^2} \quad (2.8)$$

The corner frequency  $f_0$  is related to the seismic moment  $M_0$  through the shear-wave velocity at the source region  $\beta$  and stress parameter  $\Delta\sigma$ :

$$f_0 = 4.9 \times 10^6 \beta \left(\frac{\Delta\sigma}{M_0}\right)^{1/3} \quad (2.9)$$

The scaling factor  $C$  accounts for the shear-wave radiation pattern.

$$C = \frac{\langle R_{\theta\phi} \rangle V}{4 \pi \rho \beta^3} \cdot \frac{1}{r} \quad (2.10)$$

where  $\langle R_{\theta\phi} \rangle$  = radiation pattern;  $V$  = partition of a vector into horizontal components;  $\rho$  = crustal density; and  $r$  = hypocentral distance.  $\langle R_{\theta\phi} \rangle$  is the radiation pattern corresponding to different types of seismic waves over a range of azimuths  $\theta$  and take-off angles  $\phi$ . For  $\phi$  and  $\theta$  averaged over the whole focal sphere, the shear-wave radiation pattern  $\langle R_{\theta\phi} \rangle$  is 0.55 [24].  $V$  is the factor that accounts for the partition of a vector into horizontal components and is chosen as  $1/\sqrt{2}$ . On the basis of the hypocentral locations of instrumentally recorded microearthquakes in the NMSZ, the average focal depth of 10 km is used. The crustal density  $\rho$  of continental crust at this focal depth is taken as 2.7 gm/cm<sup>3</sup> and the shear-wave velocity  $\beta$  is 3.5 km/sec.

The diminution function  $D(f)$  represents the anelastic attenuation that accounts for the damping of the earth's crust and a sharp decrease of acceleration spectra above a cutoff frequency  $f_m$ .

$$D(f) = \exp \left[ \frac{-\pi f r}{Q(f) \beta} \right] P(f, f_m) \quad (2.11)$$

where  $Q(f)$  = frequency-dependent quality factor; and  $P(f, f_m)$  = high-cut filter. The quality factor  $Q(f)$  describes the attenuation of seismic waves and is frequency dependent. Dwyer et al. [25] conducted an attenuation study in the central United States and suggested the quality factor of shear and Lg waves as

$$Q(f) = 1500 f^{0.40} \quad (2.12)$$

The high-cut filter  $P(f, f_m)$  accounts for the observation that the acceleration spectra often show a sharp decrease above a cutoff frequency  $f_m$ , which cannot be attributed to path attenuation. In this study, a Butterworth filter with a cutoff frequency of 30 Hz is used.

The amplification factor  $AF(f)$  accounts for the soft-rock effects resulting from the decreasing shear-wave velocities in the soft-rock layers.  $AF(f)$  can be calculated as [22]

$$AF(f) = \sqrt{\frac{\beta}{\beta_r}} \quad (2.13)$$

where  $\beta$  is the shear-wave velocity at the source and  $\beta_r$  is the effective shear-wave velocity. The cumulative travel time  $T_n$  of the upper  $n$  layers measured from the base of soil profile is computed as

$$T_n = \sum_{i=1}^n \frac{H_i}{\beta_i} \quad (2.14)$$

where  $\beta_i$  and  $H_i$  are the shear-wave velocity and thickness of the  $i$ -th layer, respectively. The wave frequency  $f_n$  of the upper  $n$  layers is calculated as  $f_n = 1/(4T_n)$ . The effective shear-wave velocity  $\beta_r$  corresponding to the wave frequency  $f_n$  is

$$(\beta_r)_n = 4.0 \times f_n \times H_n \quad (2.15)$$

where  $H_n$  is the total depth of the upper  $n$  layers. For each frequency  $f_n$ , the corresponding amplification factor  $AF(f)$  can be computed using equation (2.13). Thus, the amplification factor  $AF(f)$  is frequency-dependent. By using the shear-wave velocity and thickness of soft-rock layers in the Memphis area as suggested by Jacob et al. [26], the amplification factors for the selected site are calculated and shown in table 2-IV.

Table 2-IV Calculation of Amplification Factors

$H_i$ (m)	$\Sigma H_i$ (m)	$\beta_i$ (m/s)	$T_n$ (sec)	$f_n$ (Hz)	$\beta_r$ (m/s)	AF
9	9	400	0.02225	11.11	400.00	2.96
13	22	600	0.04392	5.69	500.95	2.64
17	39	1000	0.06092	4.10	640.22	2.34
100	139	950	0.16618	1.50	836.44	2.04
300	439	1100	0.43891	0.57	1000.89	1.87
200	639	1400	0.58176	0.43	1129.91	1.76
200	839	1700	0.69941	0.36	1197.00	1.71
100	939	2000	0.74941	0.33	1254.98	1.67
2000	2939	3000	1.41607	0.18	2071.00	1.30
7061	10000	3500	3.43350	0.07	2892.60	1.10

### 2.2.2 Power Spectrum

An earthquake accelerogram generally shows a build-up segment followed by a strong-motion segment and then a decay segment. The frequency content of an earthquake accelerogram is found to be approximately

constant during the strong-motion segment. Thus, the strong-motion segment of an acceleration time history is considered as a stationary random process and the one-sided power spectrum  $S_a(f)$  can be derived from the Fourier amplitude spectrum.

$$S_a(f) = \frac{2}{T_e} |A(f)|^2 \quad (2.16)$$

where  $A(f)$  is the Fourier amplitude spectrum (equation 2.7) and  $T_e$  is the strong-motion duration.

### 2.2.3 Synthetic Acceleration Time Histories

In this study, the synthetic time histories are generated using the method proposed by Shinozuka [27]. Given the power spectrum, the stationary acceleration time histories  $a_s(t)$  can be generated as follows:

$$a_s(t) = \sqrt{2} \sum_{k=1}^N \sqrt{S_a(\omega_k)\Delta\omega} \cos(\omega_k t + \phi_k) \quad (2.17)$$

where  $S_a(\omega_k)$  = one-sided earthquake power spectrum;  $N$  = number of frequency intervals;  $\Delta\omega$  = frequency increment;  $\omega_k = k \Delta\omega$ ; and  $\phi_k$  = random phase angles uniformly distributed between 0 and  $2\pi$ . The nonstationary acceleration time histories  $a(t)$  can then be obtained from the multiplication of an envelope function  $w(t)$ .

$$a(t) = a_s(t)w(t) \quad (2.18)$$

The envelope function  $w(t)$  proposed by Hwang et al. [28] is used in this study and is composed of three segments: (1) a parabolically increased segment simulating the initial-rise part of the accelerogram with its duration chosen as one fifth of  $T_e$ , (2) a constant segment representing the strong-motion portion of an earthquake excitation with a duration equal to  $T_e$ , and (3) a linearly decayed segment extending four fifths of  $T_e$ . Thus, the total duration is  $2T_e$ . Real earthquake records are commonly observed with long coda durations; however, the coda durations are considered unimportant in most engineering applications.

#### **2.2.4 Uncertainties in Seismic Parameters**

The seismologically based model for the horizontal accelerations at the base of a soil column is defined by several seismic parameters as summarized in table 2-V. Under a specific moment magnitude, epicentral distance, and quality factor, some parameters such as the crustal density  $\rho$ , shear-wave velocity  $\beta$ , and cut-off frequency  $f_m$  appear to have less influence on the resulting horizontal accelerations. On the other hand, the stress parameter  $\Delta\sigma$  and strong-motion duration  $T_e$  have significant effects on the accelerations. Thus, uncertainties in these two parameters,  $\Delta\sigma$  and  $T_e$ , are included in the analysis.

TABLE 2-V Seismic Parameters

Item	Symbol	Value
Moment magnitude	$M$	varied
Epicentral distance	$R$	57 km
Focal depth	$h$	10 km
Radiation pattern	$\langle R_{\theta\phi} \rangle$	0.55
Horizontal component	$V$	0.71
Shear-wave velocity	$\beta$	3.5 km/sec
Source-rock density	$\rho$	2.7 gm/cm <sup>3</sup>
Quality factor	$Q(f)$	$1500f^{0.4}$
Stress parameter	$\Delta\sigma$	varied
Cutoff frequency	$f_m$	30 Hz
Strong-motion duration	$T_e$	varied

For central and eastern North America, Boore and Atkinson [21] and McGuire et al. [29] suggested an average  $\Delta\sigma$  of 100 bars. From the 1988 Saguenay earthquake, Atkinson and Boore [30] determined a stress parameter of about 200 bars. Thus, three values, 100, 150, and 200 bars, are used to represent the uncertainty in stress parameter.

In this study, the strong-motion duration  $T_e$  is equal to the source duration, which is the reciprocal of the corner frequency  $f_0$  [31].

$$T_e = 1 / f_0 \quad (2.19)$$

Using this equation, the strong-motion duration  $T_e$  for an  $M = 7.5$  earthquake with  $\Delta\sigma = 150$  bars is about 14 seconds. According to the studies conducted by Johnston [32], Krinitzsky et al. [33], and Lai [34], the strong-motion duration has significant variation. Thus, the coefficient of variation is selected as 50% and the three values of 7, 14, and 21 seconds are chosen as representative values. For  $M = 6.5, 7.0, 7.5,$  and  $8.0$  New Madrid earthquakes, three representative values of  $T_e$  are shown in table 2-VI.

Table 2-VI Representative Values of Strong-Motion Duration

$M$	$T_e$ (sec)
6.5	2.5, 5.0, 7.5
7.0	4.0, 8.0, 12.0
7.5	7.0, 14.0, 21.0
8.0	12.0, 24.0, 36.0

From the combination of three representative values of two seismic parameters,  $\Delta\sigma$  and  $T_e$ , nine earthquake models are established. As an example, the nine models for an  $M = 7.5$  earthquake are shown in table 2-VII. From each model, nine earthquake time histories are generated by using different random phase angles. Thus, a total of 81 earthquake time histories is generated for each moment magnitude. For an  $M = 7.5$

earthquake, the peak base acceleration (PBA) of these 81 time histories are also listed in table 2-VII. The values of PBA vary significantly for each combination of stress drop  $\Delta\sigma$  and strong-motion duration  $T_e$ .

Table 2-VII Parameters of Earthquake Models ( $M = 7.5$ )

EQ. Model	$\Delta\sigma$ (bars)	$T_e$ (sec)	PBA (g)
1	100	7	0.362 - 0.474
2	100	14	0.241 - 0.321
3	100	21	0.228 - 0.261
4	150	7	0.441 - 0.540
5	150	14	0.325 - 0.404
6	150	21	0.264 - 0.360
7	200	7	0.500 - 0.733
8	200	14	0.408 - 0.549
9	200	21	0.329 - 0.414

### 2.3 Earthquake-Site Samples

From the combination of nine site models and nine earthquake models (81 synthetic horizontal acceleration time histories), 81 earthquake-site samples are established. As an example, the 81 earthquake-site samples for an  $M = 7.5$  earthquake is shown in table 2-VIII.

Table 2-VIII Earthquake-Site Samples

Sample	EQ. Model	$\Delta\sigma$ (bars)	$T_e$ (sec)	Site Model	$(N_1)_{60}$ or $D_r$	A and B
1	1	100	7	1	Lower	Lower
2	1	100	7	2	Mean	Lower
3	1	100	7	3	Upper	Lower
4	1	100	7	4	Lower	Mean
5	1	100	7	5	Mean	Mean
6	1	100	7	6	Upper	Mean
7	1	100	7	7	Lower	Upper
8	1	100	7	8	Mean	Upper
9	1	100	7	9	Upper	Upper
10	2	100	14	1	Lower	Lower
11	2	100	14	2	Mean	Lower
12	2	100	14	3	Upper	Lower
13	2	100	14	4	Lower	Mean
14	2	100	14	5	Mean	Mean
15	2	100	14	6	Upper	Mean
16	2	100	14	7	Lower	Upper
17	2	100	14	8	Mean	Upper
18	2	100	14	9	Upper	Upper
19	3	100	21	1	Lower	Lower
20	3	100	21	2	Mean	Lower
21	3	100	21	3	Upper	Lower
22	3	100	21	4	Lower	Mean
23	3	100	21	5	Mean	Mean
24	3	100	21	6	Upper	Mean
25	3	100	21	7	Lower	Upper
26	3	100	21	8	Mean	Upper
27	3	100	21	9	Upper	Upper

Table 2-VIII Earthquake-Site Samples (Continued)

Sample	EQ. Model	$\Delta\sigma$ (bars)	$T_e$ (sec)	Site Model	$(N_1)_{60}$ or $D_r$	A and B
28	4	150	7	1	Lower	Lower
29	4	150	7	2	Mean	Lower
30	4	150	7	3	Upper	Lower
31	4	150	7	4	Lower	Mean
32	4	150	7	5	Mean	Mean
33	4	150	7	6	Upper	Mean
34	4	150	7	7	Lower	Upper
35	4	150	7	8	Mean	Upper
36	4	150	7	9	Upper	Upper
37	5	150	14	1	Lower	Lower
38	5	150	14	2	Mean	Lower
39	5	150	14	3	Upper	Lower
40	5	150	14	4	Lower	Mean
41	5	150	14	5	Mean	Mean
42	5	150	14	6	Upper	Mean
43	5	150	14	7	Lower	Upper
44	5	150	14	8	Mean	Upper
45	5	150	14	9	Upper	Upper
46	6	150	21	1	Lower	Lower
47	6	150	21	2	Mean	Lower
48	6	150	21	3	Upper	Lower
49	6	150	21	4	Lower	Mean
50	6	150	21	5	Mean	Mean
51	6	150	21	6	Upper	Mean
52	6	150	21	7	Lower	Upper
53	6	150	21	8	Mean	Upper
54	6	150	21	9	Upper	Upper

Table 2-VIII Earthquake-Site Samples (Continued)

Sample	EQ. Model	$\Delta\sigma$ (bars)	$T_e$ (sec)	Site Model	( $N_1$ ) <sub>60</sub> or $D_r$	A and B
55	7	200	7	1	Lower	Lower
56	7	200	7	2	Mean	Lower
57	7	200	7	3	Upper	Lower
58	7	200	7	4	Lower	Mean
59	7	200	7	5	Mean	Mean
60	7	200	7	6	Upper	Mean
61	7	200	7	7	Lower	Upper
62	7	200	7	8	Mean	Upper
63	7	200	7	9	Upper	Upper
64	8	200	14	1	Lower	Lower
65	8	200	14	2	Mean	Lower
66	8	200	14	3	Upper	Lower
67	8	200	14	4	Lower	Mean
68	8	200	14	5	Mean	Mean
69	8	200	14	6	Upper	Mean
70	8	200	14	7	Lower	Upper
71	8	200	14	8	Mean	Upper
72	8	200	14	9	Upper	Upper
73	9	200	21	1	Lower	Lower
74	9	200	21	2	Mean	Lower
75	9	200	21	3	Upper	Lower
76	9	200	21	4	Lower	Mean
77	9	200	21	5	Mean	Mean
78	9	200	21	6	Upper	Mean
79	9	200	21	7	Lower	Upper
80	9	200	21	8	Mean	Upper
81	9	200	21	9	Upper	Upper

## SECTION 3

### SITE LIQUEFACTION POTENTIAL

The liquefaction potential of a soil layer is affected by site parameters such as relative density, shear modulus, percentage of clay, effective confining pressure, grain-size distribution, depth of water table, and age of deposition [7]. In addition, it is also affected by seismic parameters such as the amplitude, frequency content, and duration of an earthquake.

#### 3.1 Factor of Safety against Liquefaction

The factor of safety against liquefaction  $F_L$  of a soil layer is defined as

$$F_L = R/L \quad (3.1)$$

in which  $R$  is the resistance shear stress ratio and  $L$  is the shear stress ratio induced by an earthquake. For each potentially liquefiable layer, the earthquake-induced shear stress ratio  $L$  is evaluated from nonlinear site response analysis. The average shear stress  $\tau_{av}$  is defined as [7]:

$$\tau_{av} = 0.65 \tau_{max} \quad (3.2)$$

and then the shear stress ratio  $L$  is determined as

$$L = \tau_{av}/\sigma'_0 \quad (3.3)$$

where  $\sigma'_0$  is the effective vertical confining (overburden) pressure. The irregular shear stress time history of each potentially liquefiable layer obtained from nonlinear site response analysis is converted into equivalent uniform cycles  $N_{eq}$  at the average shear stress ratio  $\tau_{av}/\sigma'_0$  based on the procedure proposed by Seed et al. [3]. The equivalent uniform cycles  $N_{eq}$  is computed as follows:

$$N_{eq} = \sum_{i=1}^n (N_i/N_{Li}) N_{ref} \quad (3.4)$$

where  $N_i$  is the number of induced shear stress cycles at the shear stress ratio of  $\tau_i/\sigma'_0$  and  $N_{Li}$  is the number of equivalent uniform cycles required to cause liquefaction at the same shear stress ratio.  $N_{ref}$  is the number of equivalent uniform shear stress cycles required to cause liquefaction at the average shear stress ratio. The values of  $N_{Li}$  and  $N_{ref}$  can be determined from laboratory cyclic test data as shown in figure 3-1. The cyclic test data for sand (SP), silty sand (SM), and clayey sand (SC) used in this study are shown in figures 3-2 through 3-4, respectively [35-37]. By using the equivalent uniform cycles  $N_{eq}$  and relative density  $D_r$ , the resistance shear stress ratio  $R$  for either sand, silty sand, or clayey sand can be determined from these figures. Then, the factor of safety against liquefaction  $F_L$  of a soil layer can be calculated from the  $L$  and  $R$  values.

Cyclic Stress Ratio

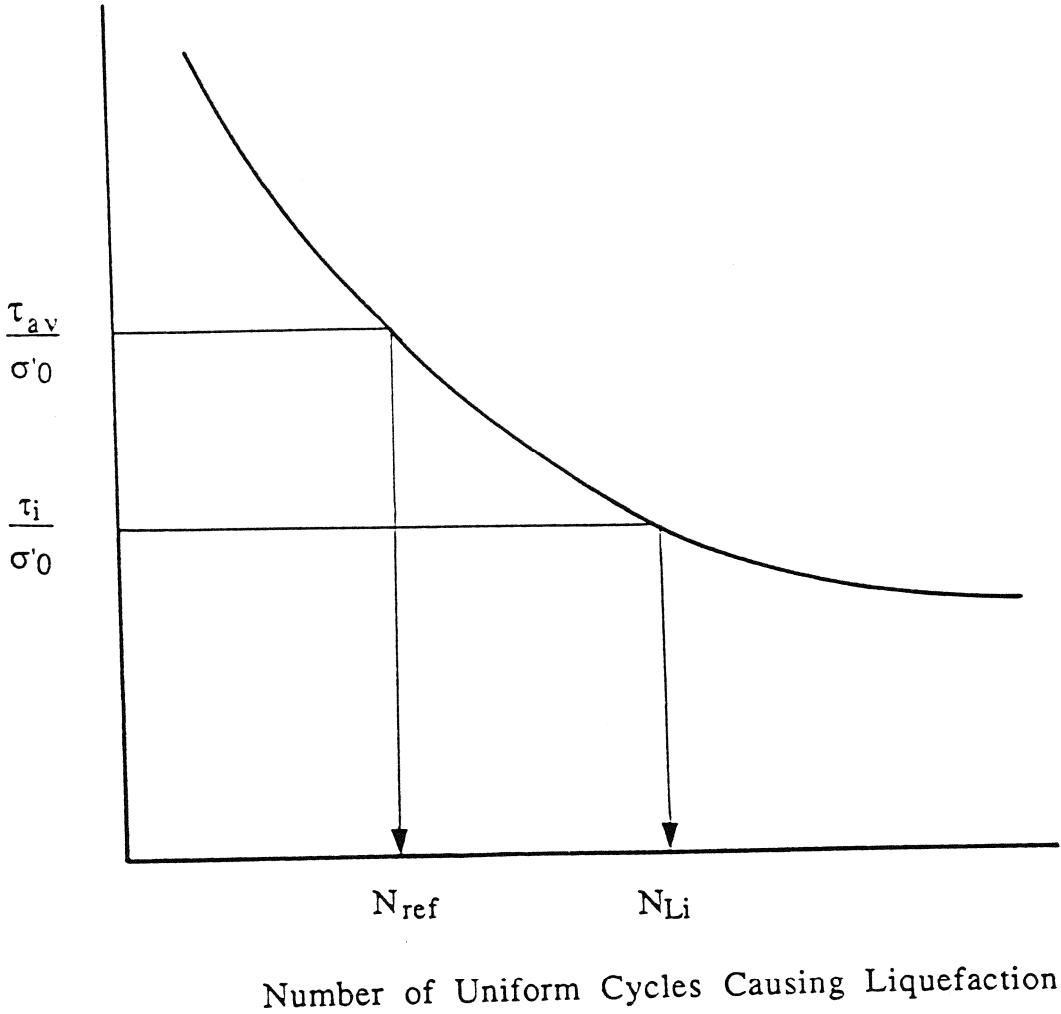


FIGURE 3-1 Determination of  $N_{ref}$  and  $N_{Li}$  Values

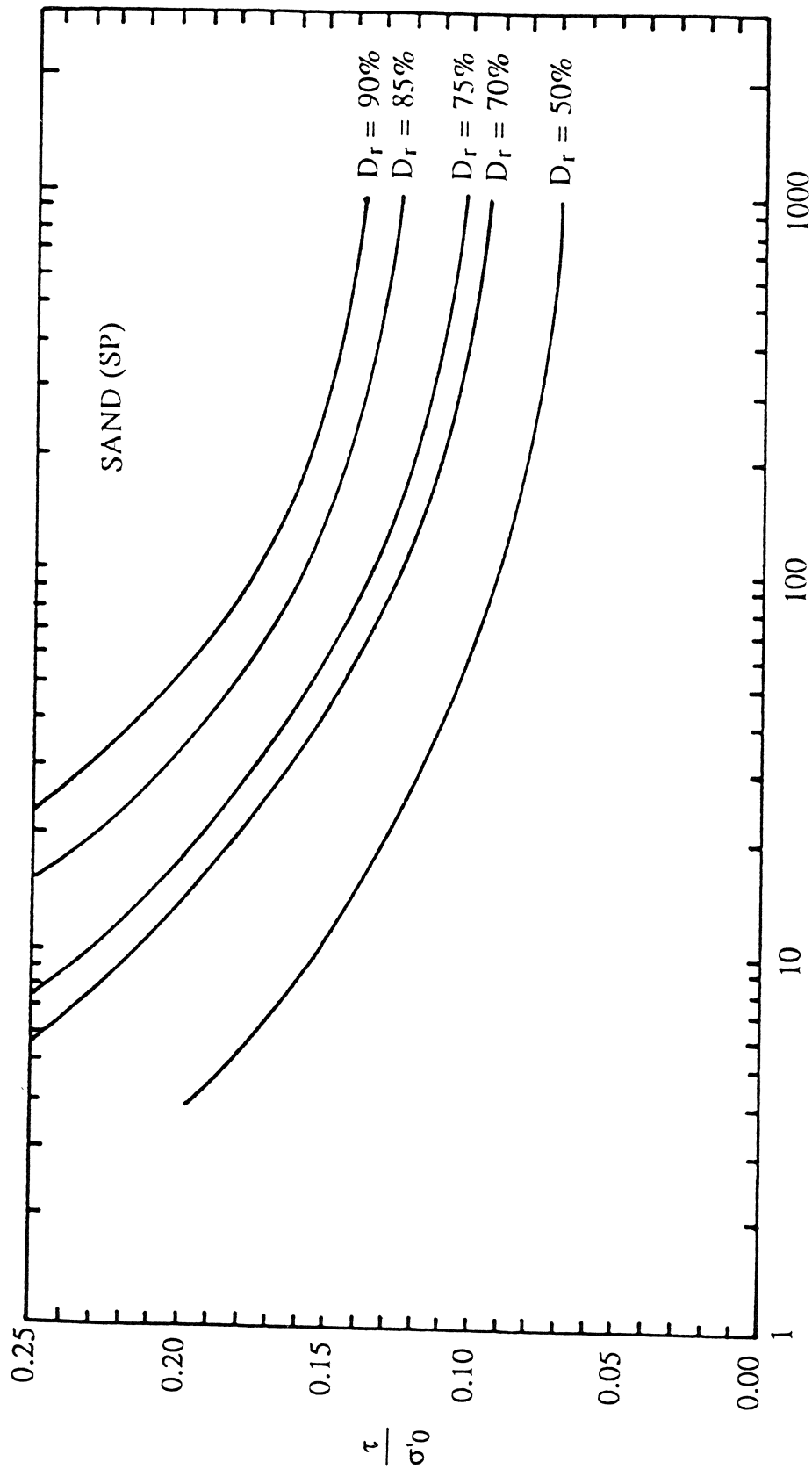


FIGURE 3 - 2 Cyclic Test Data for Sand (after Chang et al. 1990)

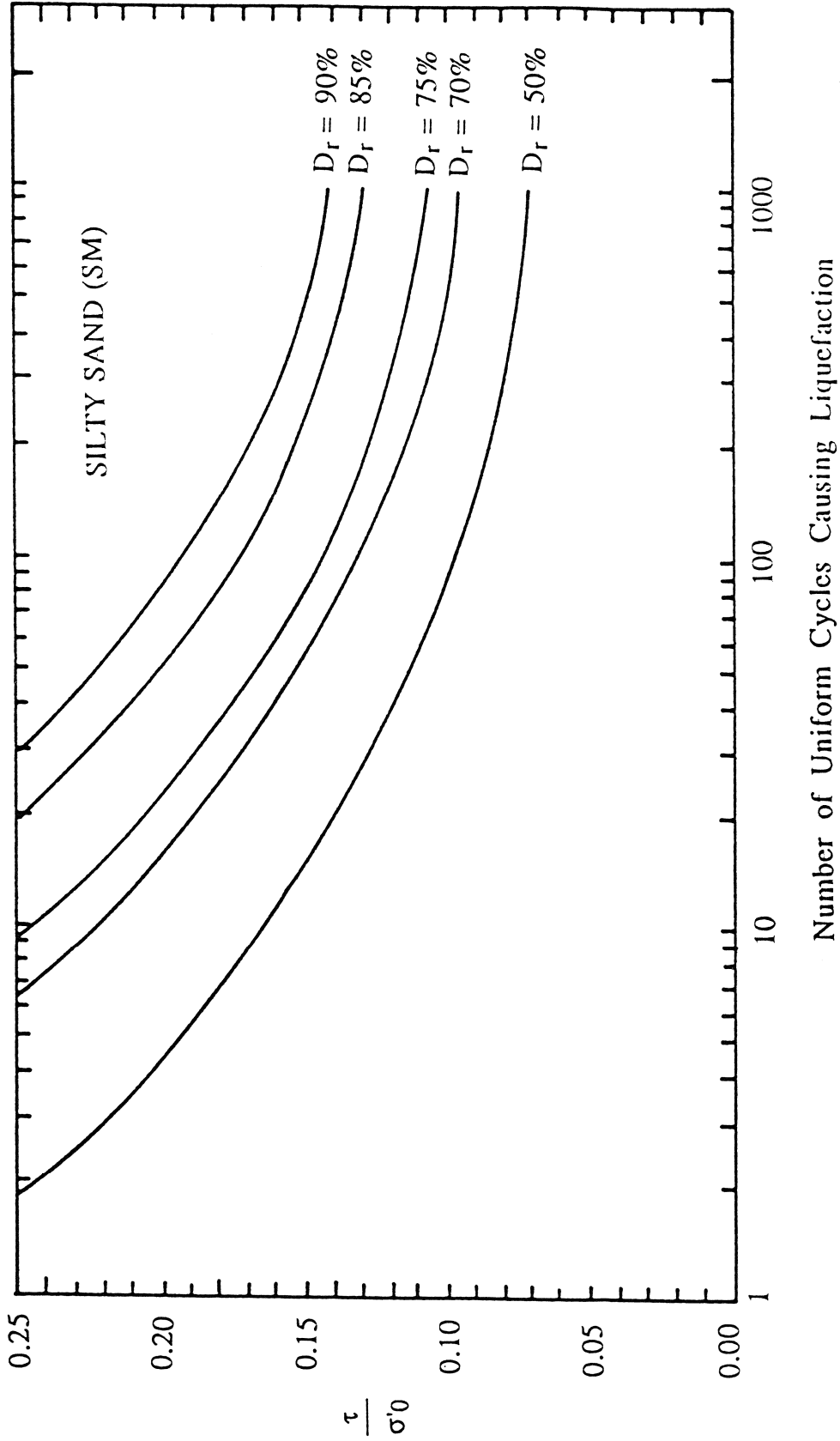


FIGURE 3 - 3 Cyclic Test Data for Silty Sand (after Chang et al. 1990)

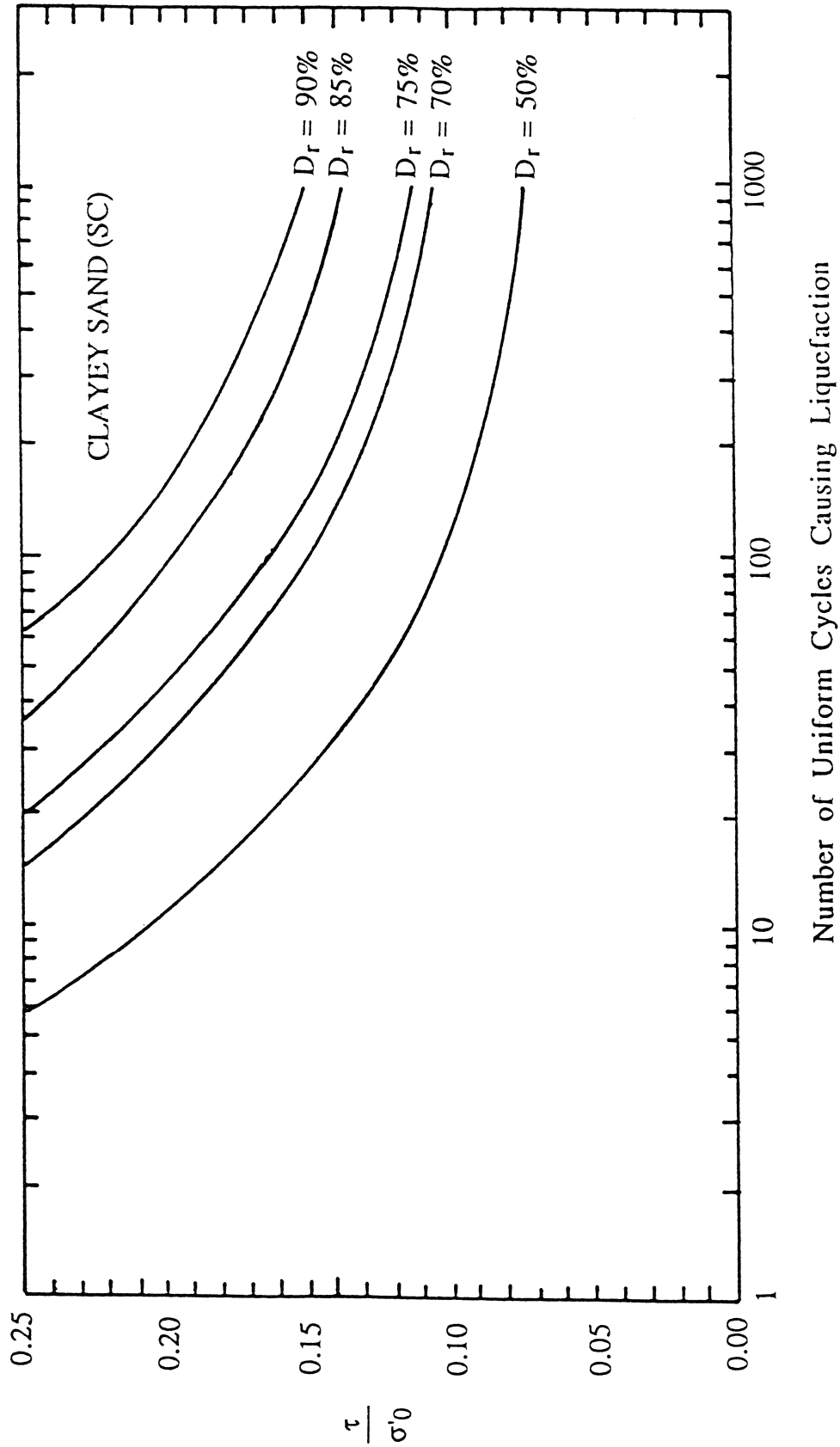


FIGURE 3-4 Cyclic Test Data for Clayey Sand (after Chang et al. 1990)

### 3.2 Liquefaction Potential Index

The  $F_L$  value only indicates the occurrence of liquefaction in a soil layer on a yes or no basis and does not reflect the liquefaction severity of a site. The liquefaction potential of a site is affected by the  $F_L$  value, thickness, and depth of liquefied layers in a soil profile. In this study, the liquefaction potential index  $P_L$  proposed by Iwasaki et al. [4] is used to quantify the liquefaction severity of a site.

$$P_L = \sum_{i=1}^n Q_i \times W_i \times H_i \quad (3.5)$$

where  $H_i$  is the thickness of the  $i$ -th layer in meter and  $Q_i$  accounts for the severity of the  $i$ -th liquefied layer.

$$Q_i = 1 - F_{Li} \quad \text{for } F_{Li} \leq 1.0 \text{ (liquefied)} \quad (3.6)$$

$$Q_i = 0 \quad \text{for } F_{Li} > 1.0 \text{ (non-liquefied)}$$

$W_i$  accounts for the influence of depth of the  $i$ -th liquefied layer on the liquefaction severity of a site.

$$W_i = 10 - 0.5 z \quad (3.7)$$

where  $z$  is the depth measured from the ground level in meter. The maximum depth considered in this study is 20 m. On the basis of the  $P_L$

value, the liquefaction potential of a site is classified as no, minor, moderate, or major liquefaction as shown in table 3-I.

Table 3-I Liquefaction Potential Index  $P_L$

$P_L$	Liquefaction Potential
0	No or little
$0 < P_L \leq 5$	Minor
$5 < P_L \leq 15$	Moderate
$15 < P_L$	Major

### 3.3 Illustration

The soil profile of sample 17 (table 2-VIII) is shown in table 3-II. Layers 1, 3, 4, and 5 (sandy soils) in the soil profile are identified as the potentially liquefiable layers. The shear-wave velocity of the soil layers is shown in figure 3-5. Figure 3-6 shows the horizontal acceleration time history at the base of the soil column from a moment magnitude 7.5 New Madrid earthquake. The time history is generated by using a stress drop of 100 bars and strong-motion duration of 14 seconds. The peak acceleration of this time history is 0.305 g. By using the MASH computer program, a nonlinear site response analysis is performed to obtain the shear stress time histories at the center of layers 1, 3, 4, and 5. The shear stress time history for layer 3 is shown in figure 3-7. As shown in the figure, the maximum shear stress  $\tau_{max}$  is 546.0 psf (26.14 kN/m<sup>2</sup>). The effective

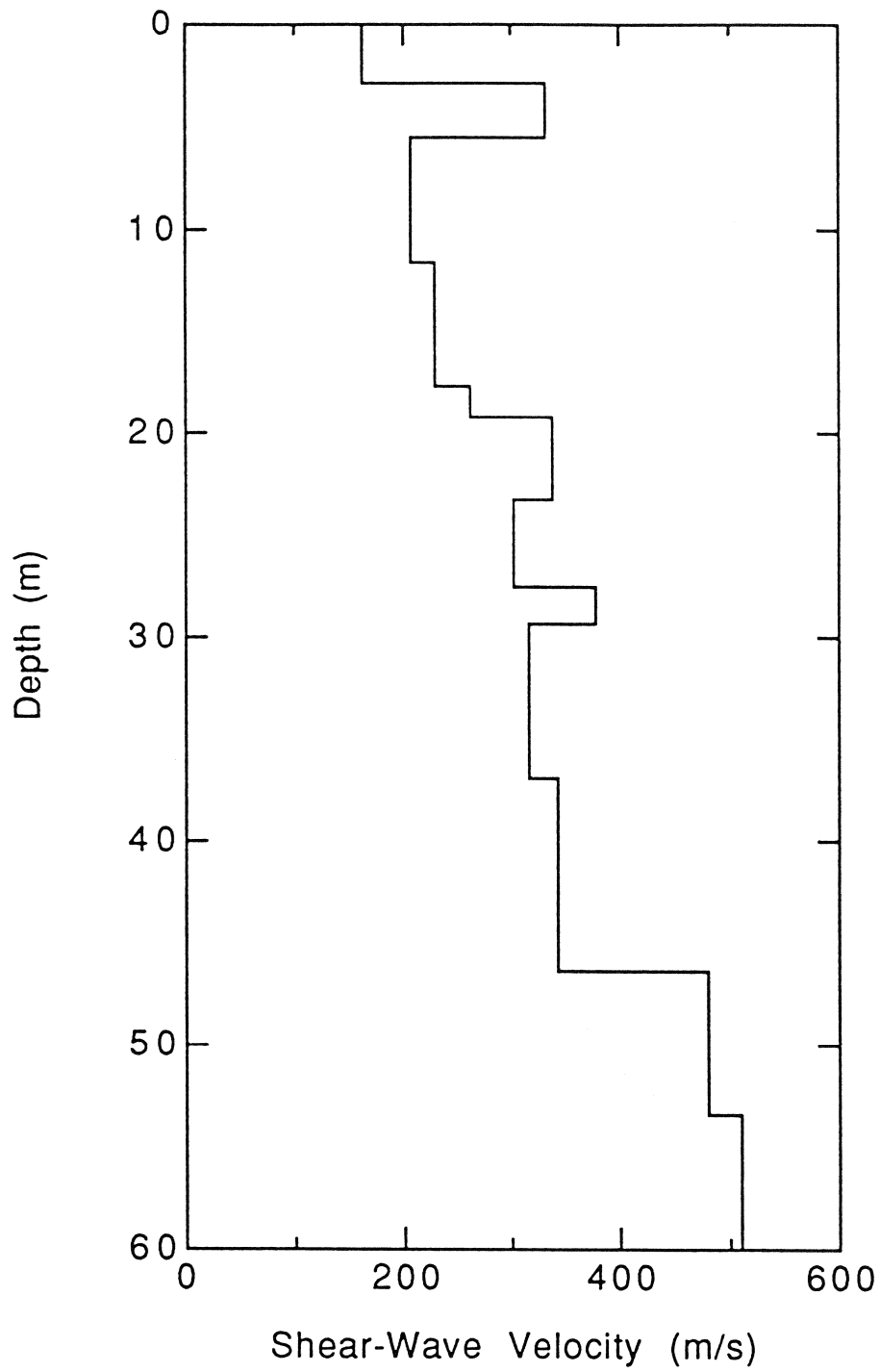


FIGURE 3-5 Shear-Wave Velocity of Soil Profile (Sample 17)

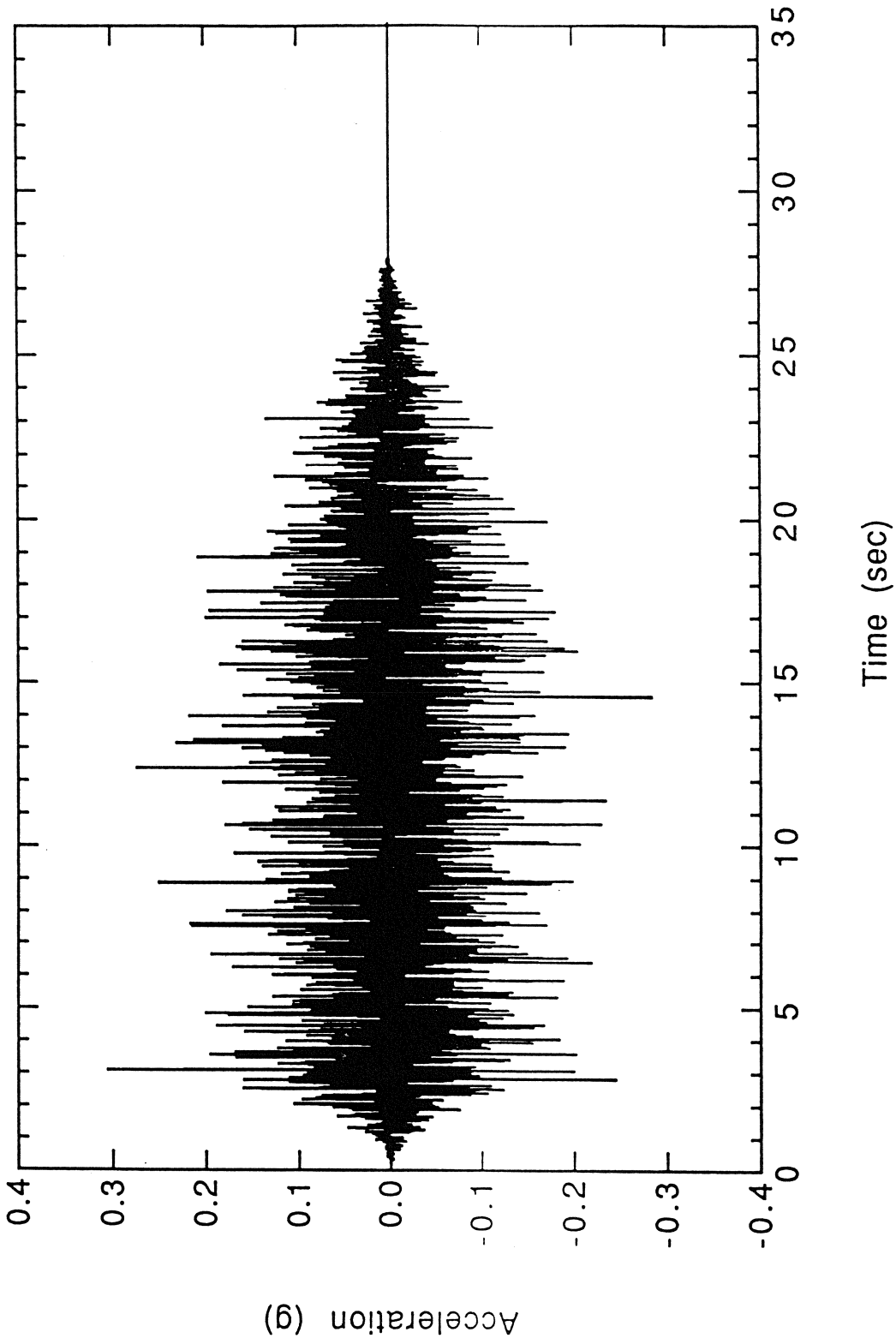


FIGURE 3-6 Base Acceleration Time History (Sample 17)

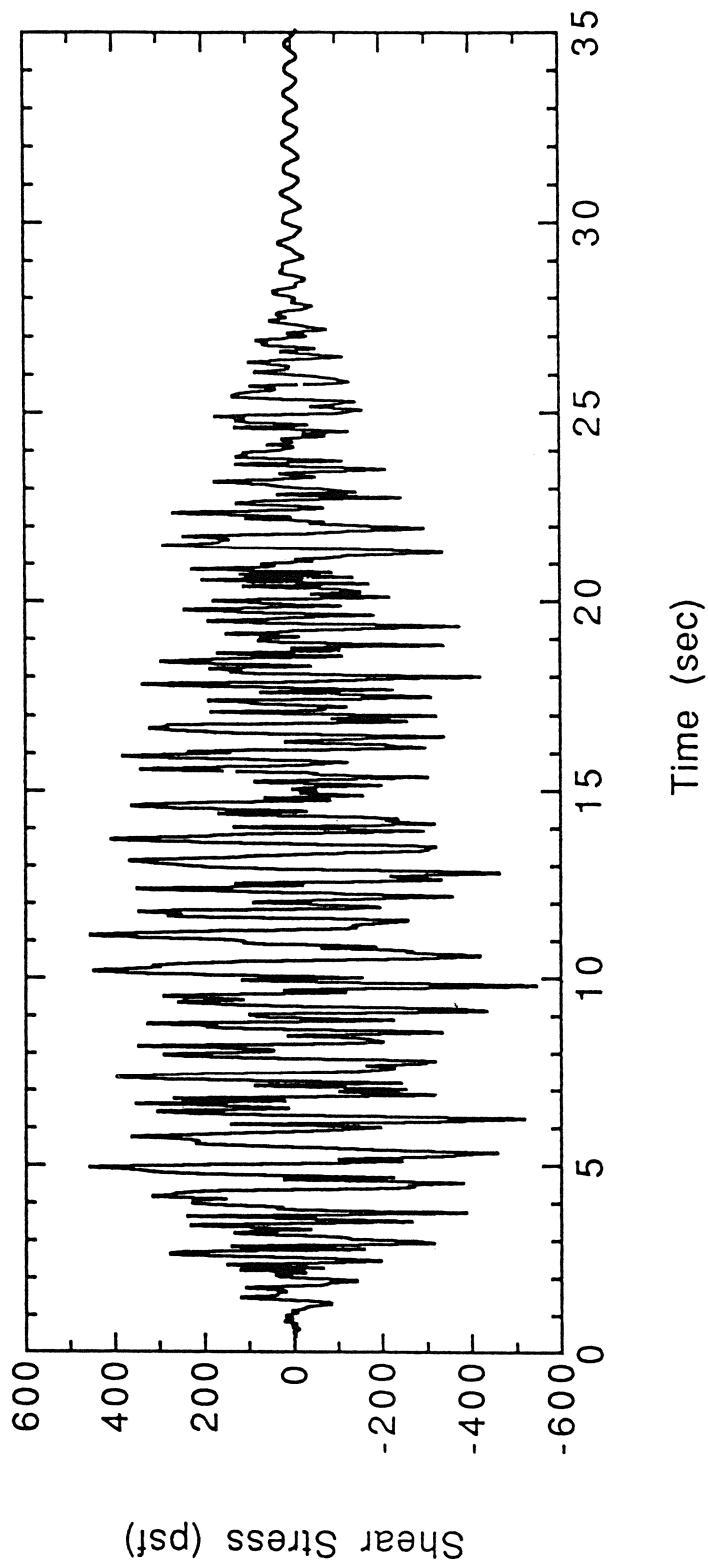


FIGURE 3-7 Shear Stress Time History of Layer 3 (Sample 17)

vertical confining pressure computed at the center of the layer is 2295.6 psf (109.9 kN/m<sup>2</sup>). Using equations (3.2) and (3.3), the earthquake-induced shear stress ratio L is computed as

$$L = (0.65 \times 546.0 / 2295.6) = 0.155$$

For all potentially liquefiable layers, the earthquake-induced shear stress ratios L are shown in table 3-III.

Table 3-II Soil Profile for Sample 17

Layer	Soil Type	Thickness (m)	$\gamma_s$ (kN/m <sup>3</sup> )	N <sub>SPT</sub>	D <sub>r</sub>
1	SM-SP	2.9	19.6	12	0.67
2	ML-CL	2.6	19.6	15	-
3	SM-SC	6.1	18.9	13	0.51
4	SP	6.1	19.6	18	0.52
5	SP-GP	1.5	21.2	45	0.76
6	CL	4.0	20.4	16	-
7	SP	4.3	21.2	-	-
8	CL	1.8	20.4	-	-
9	SC	7.6	21.2	-	-
10	SP	9.5	22.0	-	-
11	CL	7.0	20.4	-	-
12	CL	6.6	20.4	-	-

Table 3-III Determination of  $P_L$  Value (Sample 17)

Layer	$N_{eq}$ (cycles)	R	L	$F_L$	$P_L$
1	50	0.146	0.111	1.32	0.00
3	37	0.124	0.155	0.80	6.93
4	36	0.118	0.148	0.80	3.33
5	37	0.170	0.134	1.27	<u>0.00</u>
					$\Sigma = 10.26$

The soil type of layer 3 is medium dense SM-SC; thus, figure 3-3 is used to determine the resistance shear stress ratio R. For the average shear stress ratio of 0.155, the number of equivalent uniform cycles required to cause liquefaction  $N_{ref}$  is 15.2 cycles obtained from the curve corresponding to  $D_r = 0.51$  in figures 3-3. From equation (3.4), the equivalent uniform cycles  $N_{eq}$  for layer 3 is determined to be 37 cycles. On the basis of  $N_{eq} = 37$  cycles and  $D_r = 0.51$ , the resistance shear stress ratio R for layer 3 obtained from figure 3-3 is equal to 0.124. The R values for layers 1, 4, and 5 are obtained by using the same procedure and are listed in table 3-III. From these R and L values, the factor of safety  $F_L$  for layers 1, 3, 4, and 5 are calculated as 1.32, 0.80, 0.80, and 1.27, respectively. On the basis of the  $F_L$  value, depth and thickness of the soil layers, the  $P_L$  value of the site is calculated to be 10.26. The  $P_L$  value of 10.26 indicates that the site will experience moderate liquefaction if an earthquake with moment magnitude of 7.5 occurs at Marked Tree, Arkansas.



## SECTION 4

### PROBABILISTIC LIQUEFACTION ANALYSIS

#### 4.1 Liquefaction Potential Probability Matrix

For a specified moment magnitude  $M_i$ , 81 earthquake-site samples such as those shown in table 2-VIII are analyzed to determine the liquefaction potential index  $P_L$  of each earthquake-site sample. On the basis of the  $P_L$  value, each sample can be classified as either no, minor, moderate, or major liquefaction. Then, the probabilities of no, minor, moderate, and major liquefaction can be calculated as follows:

$$P(\text{no}|M_i) = (N_{\text{no}}|M_i)/N \quad (4.1)$$

$$P(\text{min}|M_i) = (N_{\text{min}}|M_i)/N \quad (4.2)$$

$$P(\text{mod}|M_i) = (N_{\text{mod}}|M_i)/N \quad (4.3)$$

$$P(\text{maj}|M_i) = (N_{\text{maj}}|M_i)/N \quad (4.4)$$

where  $P(\text{no}|M_i)$ ,  $P(\text{min}|M_i)$ ,  $P(\text{mod}|M_i)$ , and  $P(\text{maj}|M_i)$  denote the probability of no, minor, moderate, and major liquefaction, respectively given an  $M_i$  earthquake.  $(N_{\text{no}}|M_i)$ ,  $(N_{\text{min}}|M_i)$ ,  $(N_{\text{mod}}|M_i)$ , and  $(N_{\text{maj}}|M_i)$ , are the number of samples with no, minor, moderate, and major liquefaction due to an  $M_i$  earthquake and  $N$  is the sample size and is equal to 81 in this study. By repeating the same process for various moment magnitudes, the liquefaction potential probability matrix can be constructed.

The liquefaction potential index  $P_L$  of each earthquake-site sample subjected to a moment magnitude 7.5 earthquake is shown in table 4-1. Following the classification shown in table 3-I, the 81  $P_L$  values are classified into no, minor, moderate, and major liquefaction. Then, the probabilities of no, minor, moderate, and major liquefaction are calculated by using equations (4.1) through (4.4) and are listed in table 4-II. The results indicate that if a moment magnitude 7.5 earthquake occurs at Marked Tree, Arkansas, the site at President Island will have a 43.2% chance to experience major liquefaction and a 38.3% chance to experience moderate liquefaction. The chance of minor and no liquefaction at the site is 14.8% and 3.7%, respectively. By repeating the same procedure for moment magnitudes 6.5, 7.0, and 8.0, the liquefaction potential probability matrix of the site is constructed and shown in table 4-II. The mean values of the peak ground acceleration (PGA) of each moment magnitude is also shown in the table. The statistics of the peak ground acceleration are shown in table 4-III.

Table 4-I P<sub>L</sub> Values of Earthquake-Site Samples (M = 7.5)

Sample	PBA (g)	PGA (g)	P <sub>L</sub>	P <sub>L</sub> (Seed)
1	0.414	0.176	7.50	8.13
2	0.464	0.191	0.22	3.92
3	0.362	0.206	0.00	0.47
4	0.379	0.183	18.80	8.45
5	0.403	0.183	8.00	3.37
6	0.401	0.197	3.71	0.00
7	0.458	0.251	20.22	18.37
8	0.474	0.225	11.06	5.78
9	0.443	0.243	7.27	2.92
10	0.249	0.148	12.71	6.57
11	0.312	0.144	1.14	0.00
12	0.261	0.165	0.00	0.00
13	0.321	0.162	15.50	7.43
14	0.302	0.154	6.03	0.92
15	0.241	0.171	3.40	0.00
16	0.264	0.177	19.30	8.18
17	0.305	0.173	10.25	2.60
18	0.243	0.170	2.89	0.00
19	0.252	0.139	11.88	5.95
20	0.237	0.136	1.74	0.00
21	0.233	0.132	0.00	0.00
22	0.261	0.161	16.36	7.34
23	0.241	0.150	7.40	0.51
24	0.242	0.156	0.67	0.00
25	0.237	0.164	17.78	7.51
26	0.253	0.166	9.04	2.04
27	0.228	0.158	3.32	0.00

Table 4-I P<sub>L</sub> Values of Earthquake-Site Samples (M = 7.5) (Continued)

Sample	PBA (g)	PGA (g)	P <sub>L</sub>	P <sub>L</sub> (Seed)
28	0.524	0.195	19.31	9.01
29	0.442	0.185	6.39	3.54
30	0.495	0.205	1.92	0.39
31	0.452	0.256	25.16	18.99
32	0.511	0.246	13.62	7.91
33	0.453	0.213	9.40	0.98
34	0.440	0.253	31.02	18.71
35	0.539	0.244	19.06	7.55
36	0.509	0.235	12.60	2.41
37	0.325	0.184	18.32	8.49
38	0.380	0.176	8.62	2.82
39	0.365	0.198	4.15	0.00
40	0.341	0.199	21.91	9.73
41	0.357	0.210	14.24	5.04
42	0.388	0.182	7.17	0.00
43	0.345	0.245	33.15	17.66
44	0.403	0.210	17.07	5.05
45	0.348	0.209	12.16	0.70
46	0.278	0.150	16.04	6.70
47	0.300	0.174	7.64	2.67
48	0.263	0.160	0.95	0.00
49	0.305	0.175	22.68	8.07
50	0.291	0.193	13.71	4.03
51	0.300	0.178	9.45	0.00
52	0.273	0.198	27.60	9.63
53	0.360	0.219	16.10	5.50
54	0.287	0.195	12.30	0.00

Table 4-I P<sub>L</sub> Values of Earthquake-Site Samples (M = 7.5) (Continued)

Sample	PBA (g)	PGA (g)	P <sub>L</sub>	P <sub>L</sub> (Seed)
55	0.500	0.214	19.08	12.78
56	0.526	0.213	12.00	5.22
57	0.551	0.185	4.62	0.00
58	0.596	0.235	28.82	16.13
59	0.695	0.230	17.26	6.00
60	0.582	0.242	12.80	2.86
61	0.597	0.276	38.17	21.42
62	0.732	0.233	19.74	6.16
63	0.618	0.280	16.76	4.67
64	0.462	0.195	20.07	8.93
65	0.421	0.207	12.79	4.87
66	0.408	0.185	6.01	0.00
67	0.419	0.276	27.51	21.39
68	0.548	0.210	16.70	5.03
69	0.470	0.199	12.29	0.00
70	0.430	0.214	31.86	12.67
71	0.445	0.217	18.88	5.38
72	0.408	0.225	15.71	1.85
73	0.335	0.193	20.43	8.84
74	0.347	0.179	12.41	3.08
75	0.376	0.168	6.20	0.00
76	0.413	0.190	26.91	8.76
77	0.348	0.241	17.20	7.07
78	0.352	0.186	12.02	0.00
79	0.405	0.201	32.15	10.11
80	0.363	0.223	20.43	5.72
81	0.329	0.220	13.50	1.51

Table 4-II Liquefaction Potential Probability Matrix (Proposed Method)

M	Mean PGA (g)	Probability of Liquefaction (%)			
		No	Minor	Moderate	Major
6.5	0.128	90.12	8.64	1.23	0.00
7.0	0.164	45.68	27.16	18.52	8.64
7.5	0.198	3.70	14.81	38.27	43.21
8.0	0.238	0.00	0.00	12.35	87.65

Table 4-III Statistics of Peak Ground Accelerations

M	Range (g)	Mean (g)	SD (g)	COV
6.5	0.084-0.213	0.128	0.027	0.207
7.0	0.109-0.245	0.164	0.030	0.182
7.5	0.132-0.280	0.198	0.034	0.173
8.0	0.164-0.332	0.238	0.043	0.180

## 4.2 Fragility Curves

The fragility curves express the probabilities that a site will have at least minor, at least moderate, and major liquefaction at various moment

magnitude earthquakes. For a specified moment magnitude  $M_i$ , these probabilities can be determined as follows:

$$F_r(\text{min}|M_i) = P(\text{min}|M_i) + P(\text{mod}|M_i) + P(\text{maj}|M_i) \quad (4.5)$$

$$F_r(\text{mod}|M_i) = P(\text{mod}|M_i) + P(\text{maj}|M_i) \quad (4.6)$$

$$F_r(\text{maj}|M_i) = P(\text{maj}|M_i) \quad (4.7)$$

where  $F_r(\text{min}|M_i)$ ,  $F_r(\text{mod}|M_i)$ , and  $F_r(\text{maj}|M_i)$  denote the probability that the site will have at least minor, at least moderate, and major liquefaction, respectively, if an earthquake of moment magnitude  $M_i$  occurs. From the liquefaction potential probability matrix (table 4-II), the fragility data is calculated and shown in table 4-IV. Then, the fragility curves corresponding to at least minor, at least moderate, and major liquefaction is constructed as shown in figure 4-1.

Table 4-IV Fragility Data (Proposed Method)

M	Mean PGA (g)	Probability of Liquefaction (%)		
		Minor	Moderate	Major
6.5	0.13	9.87	1.23	0.00
7.0	0.16	54.32	27.16	8.64
7.5	0.20	96.30	81.48	43.21
8.0	0.24	100.00	100.00	87.65

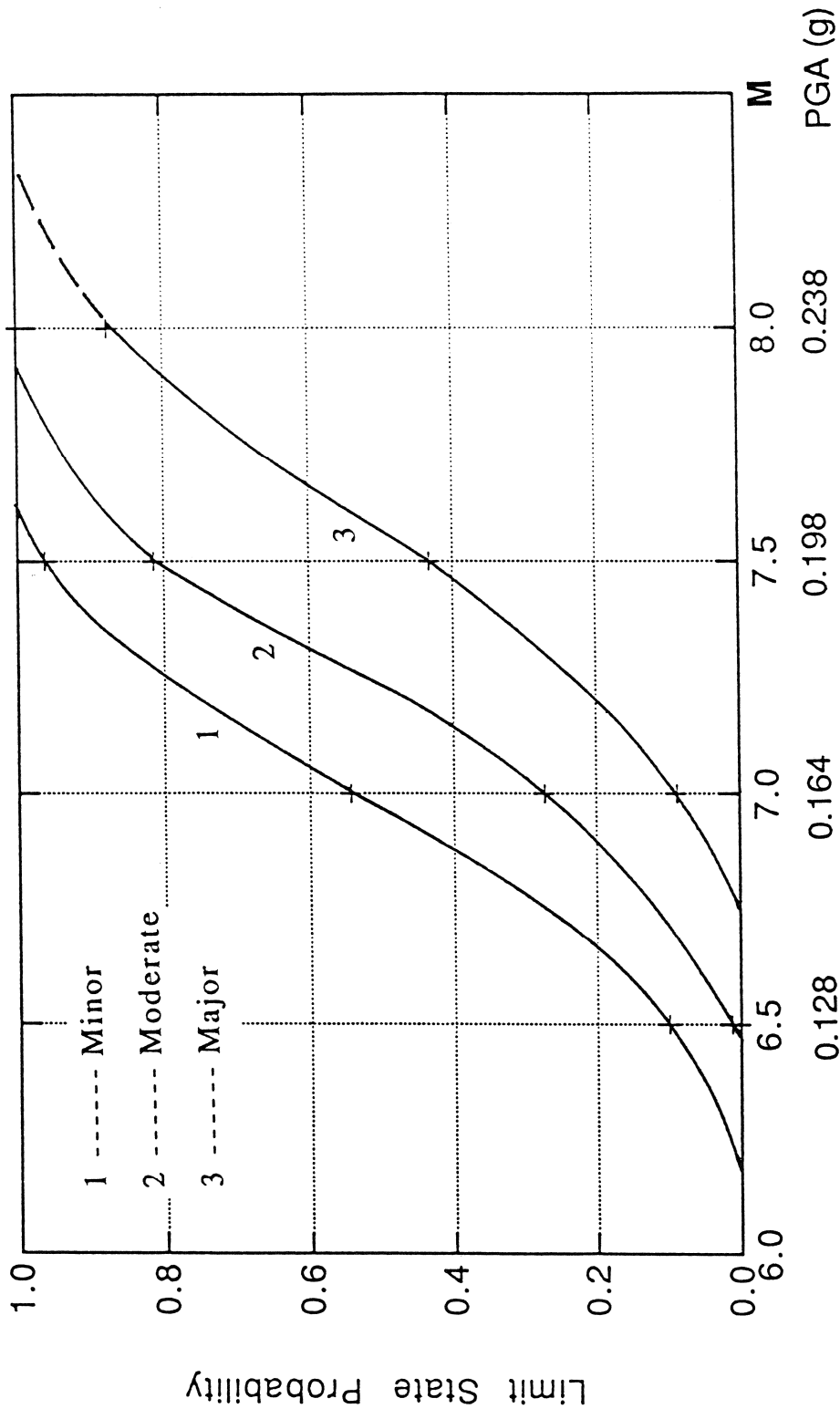


FIGURE 4-1 Fragility Curves for President Island Site (Proposed Method)

## SECTION 5

### COMPARISON OF RESULTS

In this section, the results obtained from the proposed method are compared with those obtained by using the simplified procedure developed by Seed and Idriss [6,7]. This simplified procedure is briefly described below.

#### 5.1 Simplified Procedure

For the factor of safety against liquefaction  $F_L$ , the earthquake-induced shear stress ratio  $L$  is determined from the following equation.

$$L = 0.65 a_{\max} \times \left( \frac{\sigma_0}{\sigma'_0} \right) \times r_d \quad (5.1)$$

where  $a_{\max}$  is the peak ground acceleration in g. In this study, the peak ground accelerations shown in table 4-I are determined from nonlinear site response analysis.  $\sigma_0$  and  $\sigma'_0$  are the total and effective vertical confining pressure, respectively.  $r_d$  is the stress reduction factor and can be obtained from figure 5-1 [7] or from the following formula [4].

$$r_d = 1 - 0.011 z \quad (5.2)$$

where  $z$  is the depth in meter measured from the ground level.

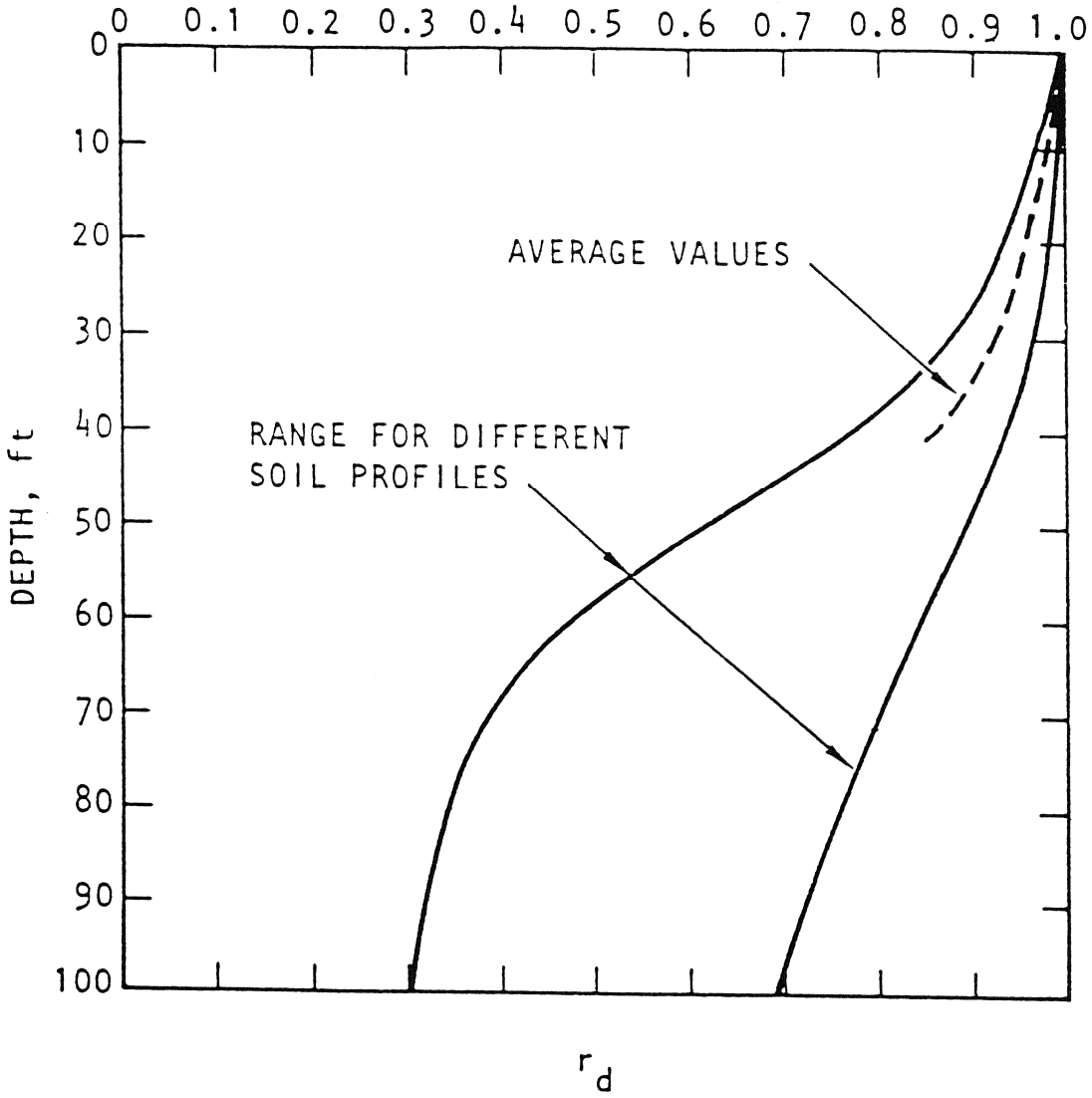


FIGURE 5-1 Range of  $r_d$  Values (after Seed and Idriss 1982)

The resistance shear stress ratio  $R$  is determined from the resistance curves (figure 5-2) for sand and silty sand on the basis of the corrected blowcount  $(N_1)_{60}$ . The resistance curves shown in figure 5-2 are applicable for magnitude 7.5 and are established based on actual field data from earthquakes around the world. For magnitude other than 7.5, the curves need to be multiplied by a factor (table 5-I) as suggested by Seed and Idriss [7].

Table 5-I Scaling Factor for Various Magnitudes

Magnitude	Scaling Factor
8.50	0.89
7.50	1.00
6.75	1.13
6.00	1.32
5.25	1.50

From the  $R$  and  $L$  values, the factor of safety  $F_L$  of each potentially liquefiable layer can be determined. Then, the liquefaction potential index  $P_L$  of the site is computed from equation (3.5). The 81  $P_L$  values obtained by using the simplified procedure for an  $M = 7.5$  earthquake are also shown in table 4-I. The liquefaction potential probability matrix and fragility curves are calculated using the same approach as the proposed method. For the selected site, the liquefaction potential probability matrix obtained by using the simplified procedure is shown in table 5-II. The

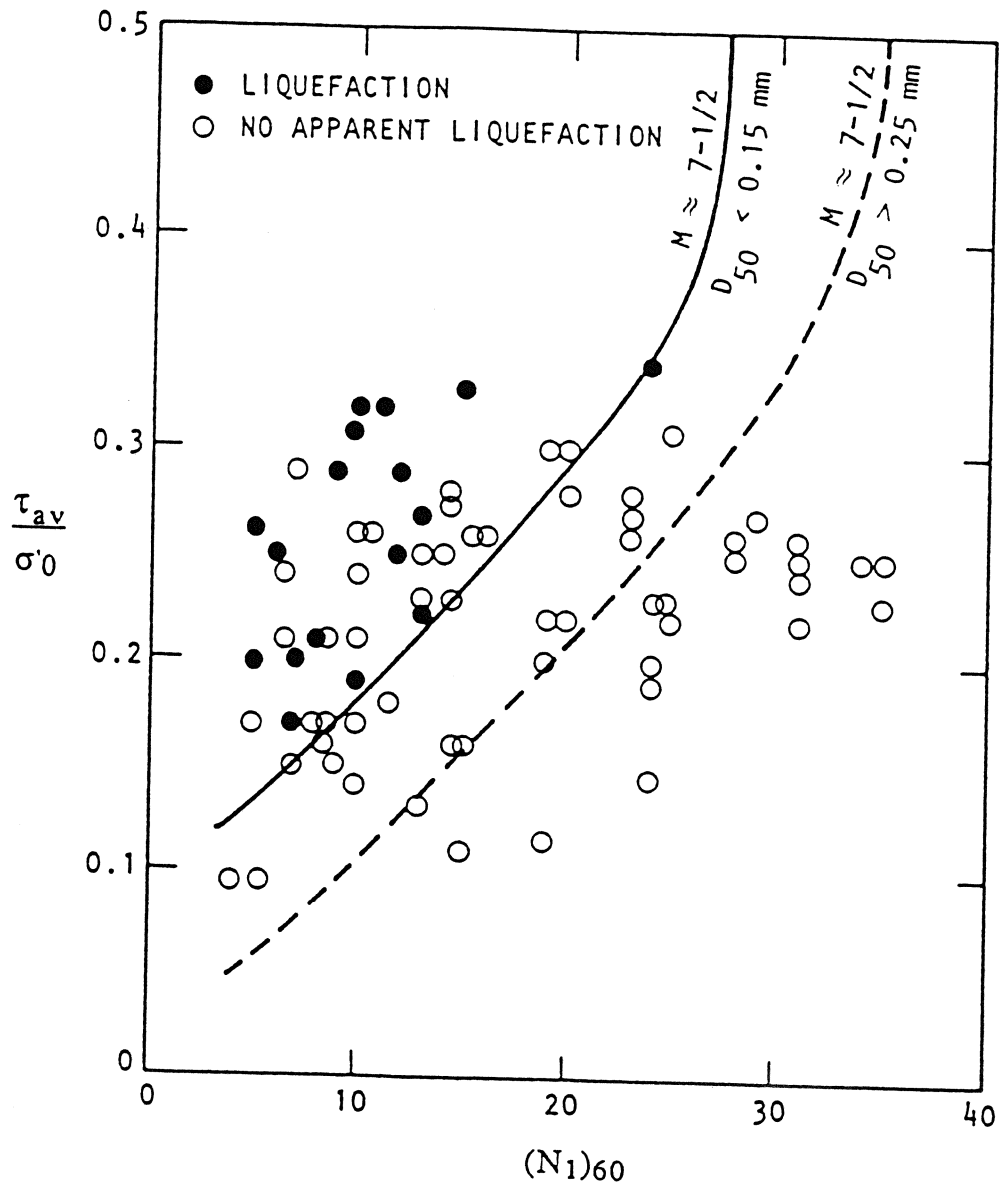


FIGURE 5-2 Liquefaction Resistance Curves for Sand and Silty Sand (after Seed and Idriss 1982)

fragility data and the corresponding fragility curves are shown in table 5-III and figure 5-3, respectively.

Table 5-II Liquefaction Potential Probability Matrix (Simplified Method)

M	Probability of Liquefaction (%)			
	No	Minor	Moderate	Major
6.5	71.60	22.22	6.17	0.00
7.0	43.21	30.86	25.93	0.00
7.5	23.46	27.16	40.74	8.64
8.0	0.00	29.63	35.80	34.57

Table 5-III Fragility Data (Simplified Method)

M	Probability of Liquefaction(%)		
	Minor	Moderate	Major
6.5	28.39	6.17	0.00
7.0	56.79	25.93	0.00
7.5	76.54	49.38	8.64
8.0	100.0	70.37	34.57

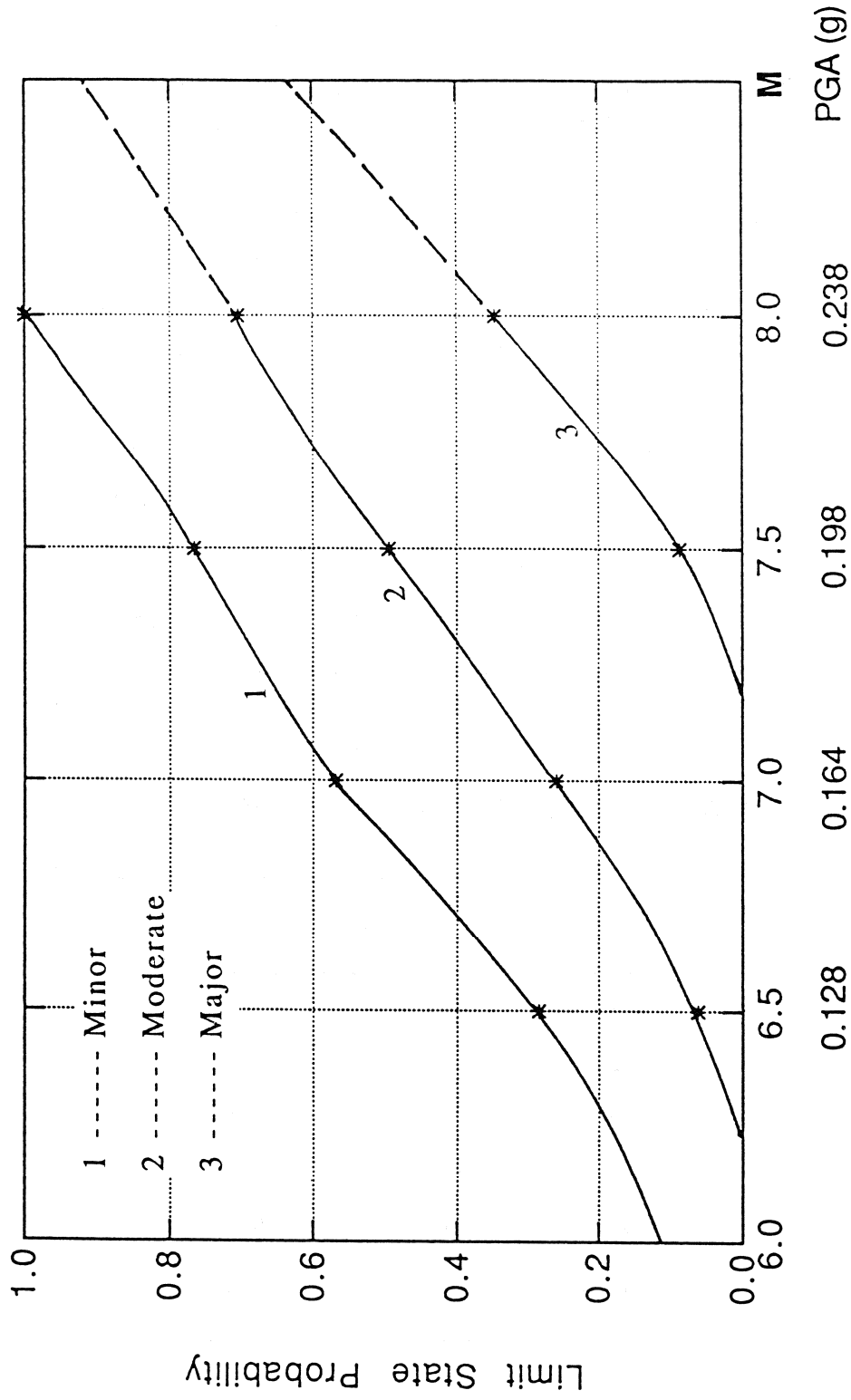


FIGURE 5-3 Fragility Curves for President Island Site (Simplified Method)

The earthquake-induced shear stress ratios  $L$  obtained from the simplified method are close to those obtained from site response analysis in the proposed method. It is noted that the peak ground acceleration used in the simplified formula is also from the results of nonlinear site response analysis. Thus, the  $L$  values computed by both methods are expected to be close. The resistance shear stress ratios  $R$  evaluated by both methods are quite different. In the proposed method, the  $R$  is computed based on the equivalent uniform cycles  $N_{eq}$ , relative density of sand  $D_r$ , and the laboratory test data, while the  $R$  value obtained by using the simplified procedure is based on the field data and corrected blowcount  $(N_1)_{60}$ . The equivalent uniform cycles  $N_{eq}$  as suggested by Seed and Idriss [7] in the simplified method are quite different from those obtained under New Madrid earthquakes. The difference in the equivalent uniform cycles contributes significantly to the difference in  $R$  values.

The fragility curves obtained from the proposed method (solid line) and those obtained by the simplified method (dashed line) are shown in figure 5-4. For an  $M = 7.0$  earthquake, the results predicted by both methods are comparable. For an  $M \geq 7.5$  earthquake, the chance of liquefaction evaluated by the proposed method is much larger than that obtained by the simplified method. However, the reverse is true for an  $M = 6.5$  earthquake.

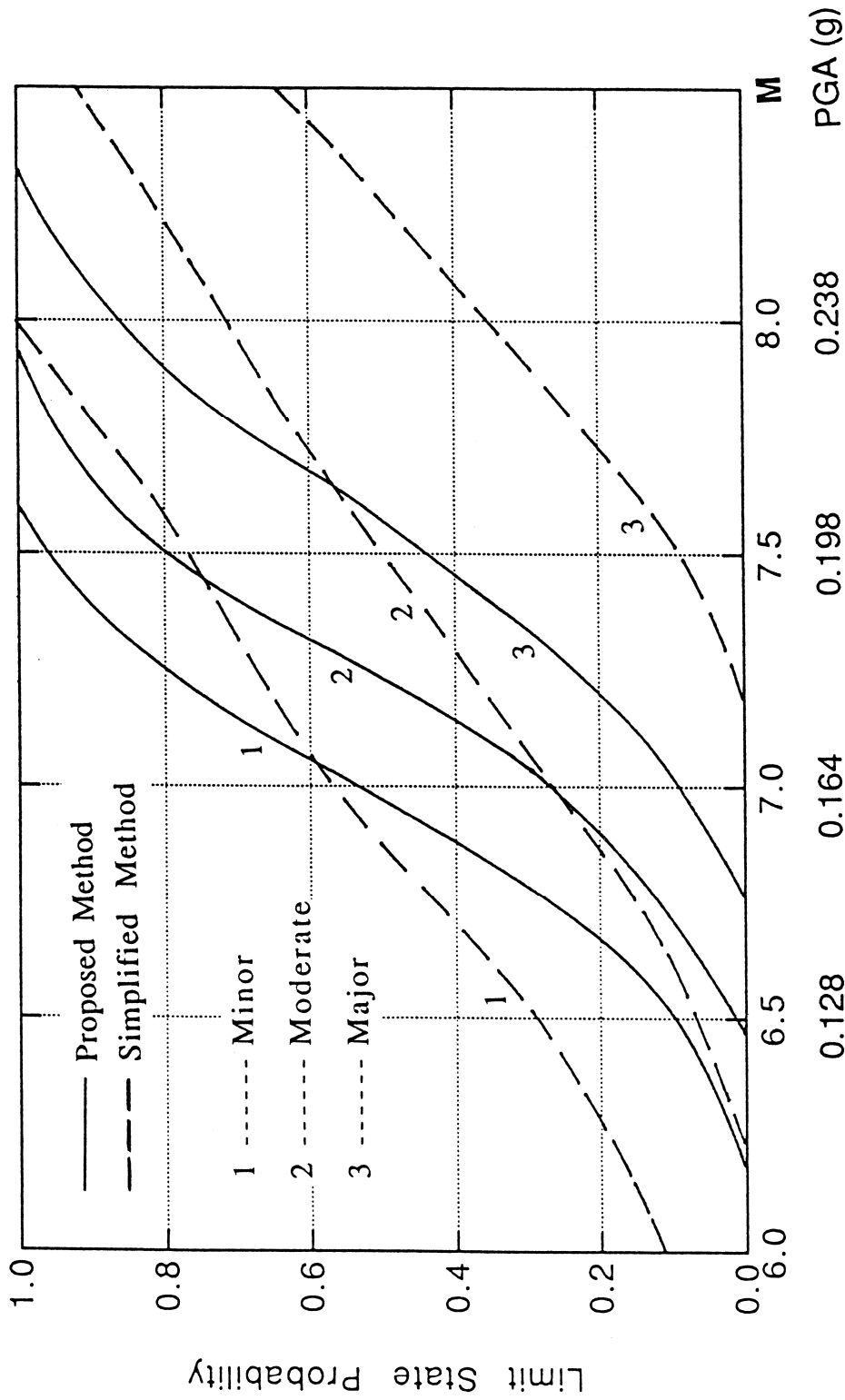


FIGURE 5-4 Comparison of Fragility Curves

## SECTION 6

### CONCLUSIONS

The liquefaction potential of a saturated sand site is affected by site parameters such as relative density, percentage of clay, and effective confining pressure. In addition, it is also affected by seismic parameters such as the magnitude, frequency content, and duration of an earthquake. In this study, a probabilistic approach for evaluating liquefaction potential of a site is presented and illustrated by using a site at President Island, Memphis, Tennessee, which is close to the New Madrid seismic zone. The results are presented in terms of the liquefaction potential probability matrix and fragility curves. The major conclusions are as follows:

1. The proposed method incorporates local site conditions and regional seismicity in the evaluation of the liquefaction potential of a site. In addition, uncertainties in seismic and site parameters can be easily included in the analysis. Thus, the proposed method is appropriate for evaluating the liquefaction potential of a specific site.
2. The site at President Island, Memphis, probably will not be liquefied if a moderate New Madrid earthquake (e.g.,  $M = 6.5$ ) occurs at Marked Tree, Arkansas. On the other hand, when the site is subject to a large earthquake, for example, a 7.5 moment magnitude earthquake, the probability that the site will have major liquefaction is 43%; at least moderate liquefaction is about 80%; and the site is almost certain to have at least minor liquefaction. Thus, the liquefaction potential at

President Island should be carefully evaluated if a critical facility is to be constructed there.

3. The fragility curves obtained from this study are compared with those using the simplified method proposed by Seed and Idriss [6,7]. For an  $M = 7.0$  earthquake, the results predicted by both methods are comparable. For an  $M \geq 7.5$  earthquake, the chance of liquefaction evaluated by means of the proposed method is much larger than that obtained by means of the simplified method. However, the reverse is true for an  $M = 6.5$  earthquake. The earthquake-induced shear stress predicted by using both methods are close, since both methods use the results from nonlinear site response analysis. However, the resistance shear stress ratio  $R$  evaluated by using both methods is quite different. In the proposed method, the  $R$  value is evaluated based on the equivalent uniform cycles  $N_{eq}$ , relative density of sand  $D_r$ , and the laboratory test data, while the  $R$  value obtained by using the simplified method is based on the field data and corrected blowcount  $(N_1)_{60}$ . The equivalent uniform cycles  $N_{eq}$  as suggested by Seed and Idriss [7] in the simplified method are quite different from those obtained from the proposed method for New Madrid earthquakes. This contributes significantly to the difference in both methods.

In the proposed method for evaluating liquefaction potential of a site, the resistance shear stress ratio  $R$  is evaluated based on laboratory test data. However, tests performed on reconstituted samples with identical values of  $D_r$  have shown a tremendous sensitivity to, among other factors, the exact method of sample preparation. Since test results may have large

variation unless use of undisturbed soil samples, the resistance shear stress ratio  $R$  will be established by other means in the future. For example, the  $R$  value may be obtained from field data. Furthermore, the nonlinear site response is obtained by performing the MASH computer code in this study. Since various codes for nonlinear site response do not usually give identical results for the same problem. Other computer codes such as SHAKE and DYNA1D will also be used in the future to compare the results of nonlinear site response analysis.

The proposed method is appropriate for evaluating the liquefaction potential of a specific site; however, it may be too cumbersome for evaluating liquefaction potential of a region. Further study is needed to develop a method that is applicable to a region.



## SECTION 7

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State University of New York at Buffalo  
Red Jacket Quadrangle  
Buffalo, New York 14261  
Telephone: 716/645-3391  
FAX: 716/645-3399

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