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Quintuple Friction Pendulum Isolator Behavior, Modeling and Validation

by Donghun Lee and Michael C. Constantinou



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PREFACE

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MCEER investigators derive support from the State of New York, National Science Foundation, Federal Highway Administration, National Institute of Standards and Technology, Department of Homeland Security/Federal Emergency Management Agency, other state governments, academic institutions, foreign governments and private industry.

This report describes the Quintuple Friction Pendulum Isolator, which is a spherical sliding isolator with six sliding surfaces. Analytical models of behavior are presented to describe the force-displacement loop for two general cases of geometric and frictional parameters. The analytical model is useful in performing simplified calculations and in verifying more complex computational models. Computational models are also presented which may be implemented in commercial software. A model isolator was tested and the results are used to validate the analytical and computational models.

ABSTRACT

This report describes the behavior of the Quintuple Friction Pendulum Isolator, a spherical sliding isolator with six sliding surfaces, five effective pendula and nine regimes of operation that allow for complex multi-stage adaptive behavior, depending on the amplitude of displacement. An analytical model is presented that is capable of tracing the behavior of the isolator in two general configurations of geometric and frictional properties. This analytical model is useful for verifying computational models and in performing simplified calculations for analysis and design. A computational model that can be implemented in program SAP2000 is also presented and verified by comparison to the analytical model. Two configurations of a model Quintuple Friction Pendulum Isolator have been tested and the results have been used to validate the analytical and computational models.

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SECTION 1 INTRODUCTION

The Quintuple Friction Pendulum (FP) Isolator is an extension of the Triple FP Isolator (Morgan, 2007; Fenz and Constantinou, 2008a and 2008b) and consists of six spherical sliding surfaces. It offers a more complex multi-stage behavior and smoother transition between regimes than the Triple FP Isolator. It is envisioned as another isolator in the arsenal of isolators available to the engineer to choose from when very large displacement capacities are needed and when complex multi-stage behavior improves performance.

Table 1-1 illustrates the evolution of the Friction Pendulum Isolator and presents information on the number of effective pendula and the number of sliding regimes (or stages) of behavior. The Single FP Isolator (Zayas et al, 1987; Mokha et al, 1991) is characterized by a single sliding surface, one effective pendulum and has one stage of operation. The Double FP Isolator (Fenz and Constantinou, 2006) offers the important advantages of reduced heating effects and increased displacement capacity for a given plan dimension, and can be configured for limited adaptive behavior (although then with the requirement for articulation, which would reduce the axial load capacity). It has two effective pendula and three sliding regimes. The Triple FP Isolator has the same advantages as the Double FP Isolator and also an increased capability for adaptive behavior. It has three effective pendula and five sliding regimes. The Quintuple FP Isolator will be shown to have five effective pendula and nine sliding regimes. The increased number of pendula and sliding regimes increases the adaptability of behavior at the expense of increased complexity in modeling its behavior. The number of effective pendula denotes the name of each isolator. Note that the schematics of isolators in Table 1-1 show the Double FP Isolator having an articulated slider as it is needed for adaptive behavior (Fenz and Constantinou, 2006). Removal of the articulation requires certain friction and geometric constraints that reduce the isolator to having the same behavior as the Single FP Isolator. Also, the Triple and Quintuple FP Isolators are shown to lack articulation for the inner most part-the rigid slider-as articulation would render the bearings unstable (Sarlis and Constantinou, 2013).

	Single FP	Double FP	Triple FP	Quintuple FP
Configuration				
Number of				
effective	1	2	3	5
pendula				
Number of				
sliding	1	3	5	9
regimes				

 TABLE 1-1 Evolution of Friction Pendulum Isolator and Number of Effective Pendula and Sliding Regimes

The existence of the Quintuple FP Isolator was postulated by Tsai et al (2010) who studied isolators with multiple sliding surfaces and presented a computational plasticity-based model of behavior. Tsai et al (2010) also presented simple algebraic force-displacement relations that only apply for the loading branch and provide no information for unloading.

This paper presents a treatment of the Quintuple Friction Pendulum Isolator that includes:

- 1) Analytical force-displacement relations for all sliding regimes which are valid for the loading and the unloading branches of the hysteresis loop, and for two general configurations of geometric and frictional properties. These relations may be used to perform simplified calculations in accordance with the Equivalent Lateral Force (ELF) procedure of the ASCE 7 Standard (ASCE, 2010). They can also be used to verify computational models for use in response history analysis.
- A computational model that can be readily utilized in commercially available software, with examples developed in program SAP2000 (Computers and Structures, 2014).
- Test results on two configurations of a model Quintuple FP Isolator that are used to validate the analytical and computational models presented.

SECTION 2

ANALYTICAL FORCE-DISPLACEMENT RELATIONS

Figure 2-1 presents a cross section of the Quintuple FP Isolator and defines the geometric and frictional parameters. Note that quantities R_i , i=1 to 6 are the radii of curvature of the six concave surfaces and quantities μ_i , i=1 to 6 are the coefficients of friction at the six sliding interfaces. The analytical force-displacement relations are derived using the approach of Fenz and Constantinou (2008a) and Morgan (2007) in which only equilibrium of horizontal and vertical forces is used. This necessitates certain geometric and frictional constraints. A model for general geometric and frictional parameters further requires consideration of equilibrium of moments and results in a much higher complexity without any practical significance as shown by Sarlis and Constantinou (2013).



FIGURE 2-1 Cross Section of Quintuple Friction Pendulum Isolator

The basic assumptions of the theory for the Quintuple FP Isolators parallel those for the Triple FP Isolator in the model of Fenz and Constantinou (2008a). They are as follows where quantity $R_{eff,i}$ is the effective radius of curvature and d_i^* is the actual displacement capacity.

$$R_{eff,i} = R_i - h_i \tag{1}$$

$$d_i^* = d_i \left(R_{eff,i} / R_i \right) \tag{2}$$

1) The effective radii satisfy the condition: $R_{eff3} = R_{eff4} \ll R_{eff2} \leq R_{eff5} \ll R_{eff1} \leq R_{eff6}$.

- 2) The coefficients of friction satisfy either of the following two conditions:
 - a. Configuration 1, where $\mu_3 = \mu_4 < \mu_5 \le \mu_2 < \mu_6 \le \mu_1$.
 - b. Configuration 2, where $\mu_3 = \mu_4 < \mu_2 \le \mu_5 < \mu_6 \le \mu_1$.

Note that configuration 2 is achieved by interchanging plates C and E of configuration 1 as shown in Figure 2-1. Also, the combination of conditions $\mu_3 = \mu_4$ and $R_{eff3} = R_{eff4}$ ensures that initiation of motion occurs simultaneously on interfaces 3 and 4 (per Figure 2-1). Any other combination of these four parameters would have resulted in behavior that cannot be exactly predicted by the model presented herein and would require a more complex treatment (Sarlis and Constantinou, 2013). Note that configurations 1 and 2 also encompass the simpler configuration where $\mu_3 = \mu_4 < \mu_5 = \mu_2 < \mu_6 \leq \mu_1$, which is characterized by four effective pendula and seven regimes of operation.

3) The displacement capacity of each surface is such that there is gradual stiffening at large displacement. For both configurations, motion on outer surfaces should initiate prior to reaching the restrainers of the inner surfaces (for example, motion on sliding surface 1 should initiate prior to reaching the restrainer of part B, etc.) which leads to the following conditions:

$$\frac{d_{1}^{*}}{R_{eff1}} + \frac{d_{2}^{*}}{R_{eff2}} > \mu_{1} - \mu_{2} , \quad \frac{d_{1}^{*}}{R_{eff1}} + \frac{d_{2}^{*}}{R_{eff2}} + \frac{d_{3}^{*}}{R_{eff3}} > \mu_{2} - \mu_{3}$$

$$\frac{d_{5}^{*}}{R_{eff5}} + \frac{d_{6}^{*}}{R_{eff6}} > \mu_{6} - \mu_{5} , \quad \frac{d_{4}^{*}}{R_{eff4}} + \frac{d_{5}^{*}}{R_{eff5}} + \frac{d_{6}^{*}}{R_{eff6}} > \mu_{5} - \mu_{4}$$

$$(3)$$

 Sliding should initiate on the surface of highest friction prior to the onset of any stiffening (i.e. prior to contacting any of the displacement restrainers). This leads to the requirement that

$$d_6^* > (\mu_1 - \mu_6) R_{eff \, 6} \tag{4}$$

5) For the special case of Configuration 2 where $R_{eff 6}$, the following condition is also needed:

$$\mu_{5} - \mu_{2} > \left(\frac{d_{1}^{*}}{R_{eff1}} + \frac{d_{2}^{*}}{R_{eff2}}\right) - \left(\frac{d_{5}^{*}}{R_{eff5}} + \frac{d_{6}^{*}}{R_{eff6}}\right)$$
(5)

Details of the derivation of the force-displacement relations are presented in Appendix A. Summaries of the relations are presented in Table 2-1 for Configuration 1 and in Table 2-2 for Configuration 2. Details of the unloading branch of each loop are presented in Appendix A. Representative force-displacement relations based on the algebraic equations of Tables 2-1 and 2-2 will be presented in the next section together with results of computational analysis.

Note that configurations 1 and 2 only differ in that regimes 2 and 3 and regimes 8 and 9 are interchanged. This leads to small differences in the loops, which will be illustrated in examples.

Requirements		$\mu_3 = \mu_4 < \mu_5 \le \mu_2 < \mu_6 \le \mu_1$
Regime	Conditions	Force-displacement relation
Ι	Motion starts on surfaces 3 and 4.	$F = \frac{W}{R_{eff3} + R_{eff4}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4}}{R_{eff3} + R_{eff4}}$
	Motion occurs on surfaces 3 and 4.	Valid until: $F^{I} = F_{f5}$, $u^{I} = (\mu_{5} - \mu_{3})R_{eff3} + (\mu_{5} - \mu_{4})R_{eff4}$
Π	Motion stops on 4 and starts on 5.	$F = \frac{W}{R_{eff3} + R_{eff5}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4} + F_{f5}(R_{eff5} - R_{eff4})}{R_{eff3} + R_{eff5}}$
	Motion occurs on surfaces 3 and 5.	Valid until: $F^{II} = F_{f2}, \ u^{II} = u^{I} + (F_{f2} - F_{f5}) \times [(R_{eff3} + R_{eff5})/W]$
III	Motion stops on 3 and starts on 2.	$F = \frac{W}{R_{eff2} + R_{eff5}} u + \frac{F_{f2} \left(R_{eff2} - R_{eff3}\right) + F_{f3} R_{eff3} + F_{f4} R_{eff4} + F_{f5} \left(R_{eff5} - R_{eff4}\right)}{R_{eff2} + R_{eff5}}$
	Motion occurs on surfaces 2 and 5.	Valid until: $F^{III} = F_{f6}, \ u^{III} = u^{II} + (F_{f6} - F_{f2}) \times [(R_{eff2} + R_{eff5})/W]$

TABLE 2-1 Force-Displacement Relation of Quintuple FP Isolator of Configuration 1

$$\begin{array}{c} {\rm IV} & \begin{array}{l} {\rm Motion \ stops \ on \ 5} \\ {\rm IV} & \begin{array}{l} {\rm Motion \ stops \ on \ 5} \\ {\rm and \ start \ son \ 6.} \end{array} & \begin{array}{l} {\rm F} = \frac{W}{R_{g/2} + R_{g/6}} u + \frac{F_{12}(R_{g/2} - R_{g/3}) + F_{13}R_{g/3}}{R_{g/2} + R_{g/6}} ... \\ + \frac{F_{14}R_{g/4} + F_{15}(R_{g/3} - R_{g/4}) + F_{16}(R_{g/6} - R_{g/3})}{R_{g/2} + R_{g/6}} \end{array} \\ \\ {\rm Valid \ until: \ F^{IV}} = F_{11}, \ u^{IV} = u^{Im} + (F_{11} - F_{14}) \times \left[(R_{g/2} - R_{g/3}) + F_{13}R_{g/3}}{R_{g/2} + R_{g/6}} ... \\ \\ {\rm Advison \ stops \ on \ 2} \\ {\rm and \ start \ son \ 1.} \end{array} \\ \\ {\rm V} & \begin{array}{l} {\rm Motion \ stops \ on \ 2} \\ {\rm and \ start \ son \ 1.} \end{array} \\ \\ {\rm Motion \ stops \ on \ 2} \\ {\rm and \ start \ son \ 1.} \end{array} \\ \\ {\rm Motion \ stops \ on \ 2} \\ {\rm and \ start \ son \ 1.} \end{array} \\ \\ {\rm Valid \ until: \ F^{V}} = F_{g/4} \frac{W}{R_{g/1} + R_{g/5}} u + \frac{F_{12}(R_{g/7} - R_{g/3}) + F_{12}(R_{g/2} - R_{g/3}) + F_{13}R_{g/3}}{R_{g/1} + R_{g/6}} \ldots \\ \\ {\rm Valid \ until: \ F^{V}} = F_{g/6} \frac{W}{R_{g/7} + R_{g/6}} d^{4}_{6} + F_{16}, \\ u^{V} = u_{d/6} = u^{IV} + (F_{d/6} - F_{1}) \times \left[(R_{g/1} + R_{g/6})/W \right] \end{array} \\ \\ {\rm Vi} & \begin{array}{l} {\rm Motion \ reaches \\ end \ on \ 6 \ and \\ stops. \ Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \\ end \ on \ 1 \ and \ stops. \ Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \\ end \ on \ 1 \ and \ stops. \ Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \\ end \ on \ 5 \ and \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \\ end \ on \ 5 \ and \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ stops. \ Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ stops. \ Motion \ starts \ on \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ starts \ and \ 5.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ stops. \ Motion \ starts \ on \ 4.} \end{array} \\ \\ {\rm Motion \ reaches \ end \ on \ 5 \ and \ stop. \ \ Motion \ end \ starts$$

IX
Motion reaches
end on 2 and
stops. Motion
starts on 3.
Motion occurs on
surfaces 3 and 4.

$$F = \frac{W}{R_{eff3} + R_{eff4}} (u - u_{dr2}) + F_{dr2}$$
Valid until: $F^{IX} = \frac{W}{R_{eff3} + R_{eff4}} (u^{IX} - u_{dr2}) + F_{dr2}$

$$u^{IX} = d_1^* + d_2^* + d_3^* + d_4^* + d_5^* + d_6^*$$

TABLE 2-2 Force-Displacement Relation of Quintuple FP Isolator of Configuration 2

Requirements		$\mu_3 = \mu_4 < \mu_2 \le \mu_5 < \mu_6 \le \mu_1$
Regime	Conditions	Force-displacement relation
Ι	Motion starts on surfaces 3 and 4.	$F = \frac{W}{R_{eff3} + R_{eff4}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4}}{R_{eff3} + R_{eff4}}$
	Motion occurs on surfaces 3 and 4.	Valid until: $F^{I} = F_{f2}, \ u^{I} = (\mu_{2} - \mu_{3})R_{eff3} + (\mu_{2} - \mu_{4})R_{eff4}$
II	Motion stops on 3 and starts on 2. Motion occurs on	$F = \frac{W}{R_{eff2} + R_{eff4}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4} + F_{f2} \left(R_{eff2} - R_{eff3}\right)}{R_{eff2} + R_{eff4}}$ Valid until: $F^{II} = F_{f5}, \ u^{II} = u^{I} + \left(F_{f5} - F_{f2}\right) \times \left[\left(R_{eff2} + R_{eff4}\right)/W\right]$
	surfaces 2 and 4.	
III	Motion stops on 4 and starts on 5.	$F = \frac{W}{R_{eff2} + R_{eff5}} u + \frac{F_{f2} \left(R_{eff2} - R_{eff3}\right) + F_{f3} R_{eff3} + F_{f4} R_{eff4} + F_{f5} \left(R_{eff5} - R_{eff4}\right)}{R_{eff2} + R_{eff5}}$
	Motion occurs on surfaces 2 and 5.	Valid until: $F^{III} = F_{f6}, u^{III} = u^{II} + (F_{f6} - F_{f5}) \times [(R_{eff2} + R_{eff5})/W]$
IV	Motion stops on 5 and starts on 6. Motion occurs on surfaces 2 and 6.	$F = \frac{W}{R_{eff2} + R_{eff6}} u + \frac{F_{f2} \left(R_{eff2} - R_{eff3}\right) + F_{f3} R_{eff3}}{R_{eff2} + R_{eff6}} \dots $ + $\frac{F_{f4} R_{eff4} + F_{f5} \left(R_{eff5} - R_{eff4}\right) + F_{f6} \left(R_{eff6} - R_{eff5}\right)}{R_{eff2} + R_{eff6}}$ Valid until: $F^{IV} = F_{f1}, \ u^{IV} = u^{III} + \left(F_{f1} - F_{f6}\right) \times \left[\left(R_{eff2} + R_{eff6}\right) / W\right]$

SECTION 3

MODELING QUINTUPLE FRICTION PENDULUM ISOLATORS FOR RESPONSE HISTORY ANALYSIS

The analytical algebraic model presented in Tables 2-1 and 2-2 is useful in quickly constructing force-displacement loops of the quintuple FP Isolator to better understand its behavior, in performing simplified calculations of response based on the Equivalent Lateral Force (ELF) procedure of the ASCE 7 Standard (ASCE, 2010) and in verifying more complex computational methods used in response history analysis. Moreover, the model may be used to develop a computational tri-axial model (biaxial horizontal motion under varying vertical load) based on the procedures presented in Ray et al (2013). However, of interest to the profession is the availability of a verified computational model of the isolator that can be readily utilized in available commercial software. Two such models are described in this section. Both utilize elements available in program SAP2000 (Computers and Structures, 2014). The first of these models utilizes a combination of five Single Friction Pendulum elements and additional gap elements.

3.1 Series Model Based on Single FP Elements

This model uses a series representation of up to five pendula based on the paradigm of Fenz and Constantinou (2008c) in modeling the Triple FP Isolator in SAP2000, although the model can be implemented in any program. The five pendula are needed in the general case where five different values of friction and/or five different values of the effective radius describe the isolator behavior (say in configuration 1 when $\mu_3 = \mu_4 < \mu_5 < \mu_2 < \mu_6 < \mu_1$). The number of needed pendula reduces depending on the number of friction values and effective radii. For example, a case with $R_{eff3} = R_{eff4}$, $R_{eff1} = R_{eff6}$ and $\mu_3 = \mu_4 < \mu_5 = \mu_2 < \mu_6 = \mu_1$ would require only three pendula as the isolator effectively behaves as a Triple FP Isolator.

Figure 3-1 illustrates the model. Each single FP element is characterized by: (a) a linear elastic spring of stiffness W / \overline{R}_{eff} where W is the instantaneous axial load on the isolator, (b) a friction force $\overline{\mu}W$ where $\overline{\mu}$ is a coefficient of friction that may be dependent on the velocity and (c) a gap element with displacement capacity, \overline{d} , that is related to the displacement capacity of each sliding surface.



FIGURE 3-1 Representation of Series Model of Quintuple Friction Pendulum Isolator

 TABLE 3-1a Parameters Used in Series Model with Five Single FP Elements to Represent the Behavior of the Quintuple FP Isolator of Configuration 1

Element	Coefficient of friction	Radius of curvature	Displacement capacity
Single FP1	$\overline{\mu}_1 = \mu_3 = \mu_4$	$\overline{R}_{eff1} = R_{eff3} + R_{eff4}$	$\overline{d}_1 = d_{total}^* - \left(\overline{d}_2 + \overline{d}_3 + \overline{d}_4 + \overline{d}_5 + \overline{d}_6\right)$
Single FP2	$\overline{\mu}_2 = \mu_5$	$\overline{R}_{eff2} = R_{eff5} - R_{eff4}$	$\overline{d}_{2} = \left(\frac{d_{5}^{*}}{R_{eff5}} + \frac{d_{6}^{*}}{R_{eff6}}\right) \left(R_{eff5} - R_{eff4}\right)$
Single FP3	$\overline{\mu}_3 = \mu_2$	$\overline{R}_{eff3} = R_{eff2} - R_{eff3}$	$\overline{d}_{3} = \left(\frac{d_{1}^{*}}{R_{eff1}} + \frac{d_{2}^{*}}{R_{eff2}}\right) \left(R_{eff2} - R_{eff3}\right)$
Single FP4	$\overline{\mu}_4 = \mu_6$	$\overline{R}_{eff4} = R_{eff6} - R_{eff5}$	$\overline{d}_4 = d_6^* \left(1 - rac{R_{eff5}}{R_{eff6}} ight)$
Single FP5	$\overline{\mu}_5 = \mu_1$	$\overline{R}_{eff5} = R_{eff1} - R_{eff2}$	$\overline{d}_5 = d_1^* \left(1 - \frac{R_{eff2}}{R_{eff1}} \right)$

Note: $d_{total}^* = d_1^* + d_2^* + d_3^* + d_4^* + d_5^* + d_6^*$ is the displacement capacity of the isolator

The parameters in the series model are selected to represent the actual behavior of the isolator as revealed in the analytical model of Tables 2-1 and 2-2. The force-displacement relation of the series model of Figure 3-1 may be easily constructed and is shown in Figure 3-2. Comparison of this loop to the model described in Tables 2-1 and 2-2 leads to relations presented in Table 3-1a and 3-1b that define the parameters of the model.

Coefficient of Element Radius of curvature Displacement capacity friction $\overline{d}_1 = d_{total}^* - \left(\overline{d}_2 + \overline{d}_3 + \overline{d}_4 + \overline{d}_5 + \overline{d}_6\right)$ $\overline{R}_{eff\,1} = R_{eff\,3} + R_{eff\,4}$ Single FP1 $\overline{\mu}_1 = \mu_3 = \mu_4$ $\overline{d}_{2} = \left(\frac{d_{1}^{*}}{R_{eff\,1}} + \frac{d_{2}^{*}}{R_{eff\,2}}\right) \left(R_{eff\,2} - R_{eff\,3}\right)$ $\overline{R}_{eff\,2} = R_{eff\,2} - R_{eff\,3}$ Single FP2 $\overline{\mu}_2 = \mu_2$ $\overline{d}_{3} = \left(\frac{d_{5}^{*}}{R_{eff\,5}} + \frac{d_{6}^{*}}{R_{eff\,6}}\right) \left(R_{eff\,5} - R_{eff\,4}\right)$ $\overline{R}_{eff\,3} = R_{eff\,5} - R_{eff\,4}$ $\overline{\mu}_3 = \mu_5$ Single FP3 $\overline{\overline{d}_4} = d_6^* \left(1 - \frac{R_{eff\,5}}{R_{eff\,6}} \right)$ $\overline{R}_{e\!f\!f\,4}=R_{e\!f\!f\,6}-R_{e\!f\!f\,5}$ Single FP4 $\overline{\mu}_4 = \mu_6$ $R_{eff 2}$ $\overline{R}_{eff\,5} = R_{eff\,1} - R_{eff\,2}$ $\overline{d}_{5} = d_{1}^{*} | 1 -$ Single FP5 $\overline{\mu}_5 = \mu_1$ R_{eff1}

 TABLE 3-1b Parameters Used in Series Model with Five Single FP Elements to Represent the Behavior of the Quintuple FP Isolator of Configuration 2



FIGURE 3-2 Force-Displacement Relation of Series Model with Five Single FP Elements

The series model with five single FP elements shown in Figure 3-1 can be implemented as an assembly of vertically-connected single FP elements and gap elements in commercial software SAP2000. Admittedly, however, this modeling approach is complicated because it would require 37 nodes, 27 rigid beam elements, four additional boundary supports, five single FP elements and at least 16 gap elements to model the tri-axial behavior of the bearing (see Fenz and Constantinou, 2008c for the similar case of the Triple FP Isolator). Figure 3-3 illustrates the model with five single FP elements. The figure also shows that this element may be reduced to a pair of one Triple FP and one Double FP elements, of which the Triple FP element exist in the most recent version of program SAP2000, and the Double FP Element may be simulated as a subversion of the Triple FP element in program SAP2000.



FIGURE 3-3 Series Model of Quintuple FP Isolator with (a) Five Single FP Elements in Series and (b) Pair of Double and Triple FP Elements

3.2 Series Model Based on Combination of Triple FP and Double FP Elements

The series model with five Single FP elements shown in Figure 3-3 can be represented by a pair of one Double and one Triple FP Isolator element as shown in Figure 3-4. These two elements are already available in program SAP2000 (the Double FP element is a subversion of the Triple FP element). However, their use in modeling the Quintuple FP Isolator requires that the Double and Triple FP element parameters be correctly specified.

The Triple FP element will be used to represent the behavior of an idealized Triple FP Isolator with the parameters shown in Figure 3-4(a) and the Double FP element will be used to represent the behavior of an idealized Double FP element with the parameters shown in Figure 3-4(b). Note that the parameters of this idealized isolator will be determined so that the two elements represent the behavior of the actual isolator. The assembly of these two elements consists of five pendula that produce the same behavior as the series model of Figure 3-1.



FIGURE 3-4 Parameters of (a) Triple FP Element and (b) Double FP Element Representing a Quintuple FP Isolator

 TABLE 3-2 Parameters Used in Series Model with One Triple and One Double FP Element to

 Represent the Behavior of the Quintuple FP Isolator

Element	Surface	Coefficient of friction	Radius of curvature	Displacement capacity
	Inner surfaces	$\tilde{\mu}_2(=\tilde{\mu}_3) \\ = \mu_3(=\mu_4)$	$\begin{split} \tilde{R}_{eff\ 2} \left(= \tilde{R}_{eff\ 3} \right) \\ = R_{eff\ 3} \left(= R_{eff\ 4} \right) \end{split}$	$\tilde{d}_2 = \tilde{d}_3 = \left[d_{total}^* - \left(\tilde{d}_1 + \tilde{d}_4 + \tilde{d}_5 + \tilde{d}_6\right)\right]/2$
Triple FP element	Outer top surface	$\tilde{\mu}_4 = \mu_5$	$\tilde{R}_{eff4} = R_{eff5}$	${ ilde d}_4^* = {d_5^*} + rac{R_{eff5}}{R_{eff6}} {d_6^*}$
	Outer bottom surface	$\tilde{\mu}_1 = \mu_2$	$\tilde{R}_{eff1} = R_{eff2}$	$\tilde{d}_1 = d_2^* + \frac{R_{eff2}}{R_{eff1}} d_1^*$
Double FP element	Upper surface	$\tilde{\mu}_5 = \mu_6$	$\tilde{R}_{eff5} = R_{eff6} - R_{eff5}$	$\tilde{d}_5 = d_6^* \left(1 - \frac{R_{eff5}}{R_{eff6}} \right)$
	Lower surface	$\tilde{\mu}_6 = \mu_1$	$\tilde{R}_{eff6} = R_{eff1} - R_{eff2}$	$\tilde{d}_6 = d_1^* \left(1 - \frac{R_{eff2}}{R_{eff1}} \right)$

 $d_{total}^* = d_1^* + d_2^* + d_3^* + d_4^* + d_5^* + d_6^*$

The parameters of Triple FP and Double FP elements are derived using the actual parameters of the Quintuple FP Isolator are presented in Table 3-2. For the Triple FP element, the parameters are derived by use of the following: (a) the relation between the actual parameters of the Triple FP Isolator and the series model with three single FP pendula presented in Fenz and Constantinou (2008c), and (b) the relation between the first three pendula of the series model in Figure 3-1 to the actual parameters of Quintuple FP Isolator.

3.3 Model Verification

To verify the computational models presented, a case of the Quintuple FP Isolator in Configuration 1 is modeled in program SAP2000, analyzed to obtain force-displacement relations and then compared to the predictions of the analytical model. Table 3-3 presents the parameters of the example Quintuple FP Isolator. For the analysis, a simple seismically-isolated structure was constructed and analyzed in SAP2000. The lateral force-displacement relation was obtained by imposing a history of displacement at a control point. Details are provided in Appendix B. A second example of Configuration 2 will also be presented and discussed. The second example consists of an isolator with the same geometric and frictional characteristics as the example of Configuration 1, but with μ_2 =0.03 and μ_5 =0.06.

Radius (inch)		Height (inch)		Friction Coefficient		Displacement Capacity (inch)		
	R_1	238	h_1	8	μ_1	0.10	d_1	14
	R_2	50	h_2	6	μ_2	0.06	d_2	6
	R_{3}	24	h_3	4	μ_3	0.01	d_3	2.25
	R_4	24	h_4	4	$(=\mu_4)$	0.01	d_4	2.25
	R_5	50	h_5	6	μ_5	0.03	d_5	6
	R_6	156	h_6	8	μ_6	0.07	d_6	14

TABLE 3-3 Parameters of Analyzed Quintuple FP Isolator of Configuration 1

Figure 3-5 compares force-displacement loops obtained by the computational SAP2000 model to that constructed using the analytical model of Table 2-1 for the example of Configuration 1. The five Single FP element model and the Triple-Double FP element model gave exactly the same results so only the results of the latter are shown in Figure 3-5. The loops were constructed to a displacement of 40inch, which is in regime IX and just short of the displacement capacity of 41.1inch. Loops at intermediate amplitudes of displacement are also shown in Figure 3-5. The transition points between regimes are identified in the graphs. Evidently, the SAP2000 computational model predicts exactly the behavior of the isolator as determined by the analytical model of Table 2-1.



DISPLACEMENT (inch)

FIGURE 3-5 Comparison of Analytical and Computational Force-Displacement Loops for Example of Configuration 1 in Table 3-3

The example of Configuration 2 also resulted in identical analytical and computational forcedisplacement loops. However, the behavior of the isolator of Configuration 2 was the same as that of Configuration 1 except for some small difference in the stiffening regimes which are related to differences in the sliding regimes as revealed in Tables 2-1 and 2-2. Accordingly, only results of the analytical model are presented in order to expose differences between the two configurations. The comparison of loops for the configurations is presented in Figure 3-6. The small difference between the two configurations is highlighted by zooming on the stiffening regimes. Analysis of isolators with different geometric and frictional properties revealed generally small differences in the force-displacement loops between the two configurations. An example of the largest differences calculated is for a case for which the loops are presented in Figure 3-7. Configurations 1 is the same as that of Table 3-3 in terms of frictional and geometric properties but for the radius of surface 5 being R₅=120inch instead of 50inch and coefficient of friction μ_5 =0.02 instead of 0.03. Configuration 2 has the properties of surfaces 2 and 5 interchanged.



DISPLACEMENT (inch)

FIGURE 3-6 Comparison of Analytical Force-Displacement Loops for Examples of Configurations 1 and 2 per Table 3-3



FIGURE 3-7 Comparison of Analytical Force-Displacement Loops for Examples of Configurations 1 and 2 per Table 3-3 but with R_5 =120in. and μ_5 =0.02

The results in Figures 3-6 and 3-7 demonstrate small differences between configurations 1 and 2. Nevertheless, the force-displacement relations of the two configurations are governed by different sets of equations, respectively given in Tables 2-1 and 2-2.

The presented results provide verification for the computational model in program SAP2000. Nevertheless, the analytical model and the computational model in program SAP2000 require validation by comparison to experimental data. This is provided in the next section where test results are presented.

SECTION 4 MODEL VALIDATION

A model Quintuple FP Isolator was tested in the bearing test machine at the University at Buffalo (Kasalanati and Constantinou, 1999). Table 4-1 presents the properties of the tested isolator. Two configurations were tested, 1 and 2. Configuration 2 was created by simply interchanging the position of parts C and E per Figure 2-1 and resulted in a change in the distribution of friction values. Note the values of the friction coefficient in Table 4-1 were measured in the experiments and are typical of very low speed conditions and an axial load W=20kip. The values of friction varied a little during the testing as will be discussed later. An image of the tested isolator, deformed in the bearing testing machine is shown in Figure 4-1. Its basic dimensions (height of 3.8in is for the un-deformed position) and the seven parts of the bearings are shown in the figure (also, see Figure B-3 for detailed dimensions).

Radius (inch)		Height (inch)		Friction Coefficient		Displacement Capacity (inch)	
R_{I}	18	h_1	1.4	μ_1	0.12 (0.12)	d_1	1.5
R_2	8	h_2	1.2	μ_2	0.085 (0.035)	d_2	1.3
R ₃	2	h3	0.9	μ₃	0.015 (0.015)	d_3	0.55
R_4	2	h_4	0.9	$(=\mu_4)$		d_4	0.55
<i>R</i> 5	8	h_5	1.2	μ_5	0.035 (0.085)	d_5	1.3
R_6	18	h_6	1.4	μ_6	0.11 (0.11)	d_6	1.5

TABLE 4-1 Parameters of Tested Quintuple FP Isolator (Values of Friction are for Configuration 1.Values in Parenthesis are for Configuration 2.)



FIGURE 4-1 Image of Deformed Quintuple FP Isolator in Testing Machine

Testing of the isolator was first conducted under quasi-static conditions (harmonic motion of frequency equal to 0.005Hz, peak velocity of 0.16in/sec) so that the coefficient of friction remained essentially constant (Coulomb friction). Accordingly, the tested isolator clearly exhibited the nine regimes of operation and allowed for comparison to the analytical model. Subsequently testing was conducted under dynamic conditions to reveal the smooth behavior that results from the velocity dependence of the coefficient of friction.

Testing of the isolator was conducted under a specified constant load W=20kip. Table 4-2 presents the conducted test program. The peak displacement was 5.0inch that represented a limit of the test machine. The displacement capacity of the isolator was 5.58inch. The isolator was deformed up to regime VIII.

Configuration	Test no.	Vertical load (kip)	Displacement amplitude (in)	Frequency (Hz)	No. of cycles	Regime
1	1	20	0.5	0.005	2	III
	2	20	1.5	0.005	2	V
	3	20	3.0	0.005	2	V
	4	20	4.5	0.005	2	VII
	5	20	5.0	0.005	2	VIII
2	6	20	5.0	0.005	2	VIII

 TABLE 4-2 Test Matrix for Quintuple FP Isolator
During testing it was observed that parts of the isolator exhibited some rotation about the vertical axis and, as a result of that, they had small out-of-plane motion. This resulted in slight variation of the displacement at each of the transition points between regimes (uncertainty on what the displacement exactly is).

Figure 4-2 presents a comparison of experimental and analytical results for the tests of Configuration 1 in Table 4-1. Only the results of the analytical model are presented since the computational model obtained in SAP2000 produces exactly the same results as the analytical model. The values of friction coefficients used in the analytical model are those in Table 4-1. In reality the values of friction varied in the loops at various amplitudes as a result of the velocity dependence of the coefficient of friction. Note that velocity in the five tests shown in Figure 4-2 varied from a peak value of 0.016 to 0.16in/sec, a range over which there is some effect of velocity. This explains the observed "smoothness" of the experimental loops whereas the analytical loops show sharper transition from one regime to the next. Nevertheless, the analytical results are in good agreement with the experimental results.

The experimental results of Figure 4-2 (and also in results presented later in this report under faster motion conditions) show an uneven behavior as if there is a momentary stop of motion in the stiffening regime of operation. It is not precisely known what caused this behavior but experimental results and advanced theory presented in Sarlis and Constantinou (2013) indicate that this may be caused by small differences in the values of friction at surfaces 3 and 4. Note that the theory presented in this report is based on the assumption that these two values of friction are equal.

The single test of the isolator in Configuration 2 produced practically the same force-displacement loop as that of Configuration 1, and both were accurately predictable by the analytical model. Instead of comparing the force-displacement loops for the two configurations in this slow test, a comparison is made when the two isolators were tested under dynamic conditions.



FIGURE 4-2 Experimental and Analytical Force-Displacement Loops of Isolator in Configuration 1

Additional tests were conducted on the isolators of Configuration 1 and 2 under the same load but larger velocity of motion in order to reveal the behavior of the isolators under dynamic conditions. Test results are presented in Figures 4-3 and 4-4. Testing was conducted by first imposing a slow motion to the maximum displacement over a period of 70sec, then pausing for 10sec and then imposing two and a half cycles of harmonic motion of frequency of 0.1Hz and amplitude of either 3 or 5inch. The peak velocity of motion was either 1.9 or 3.1 in/sec. Figure 4-3 shows the results for Configuration 1 in the test at peak velocity of 1.9in/sec, and Figures 4-4 and 4-5 show the results in Configurations 1 and 2 in the tests at peak velocity of 3.1in/sec. The history of imposed motion is included in the graphs of Figures 4-3 to 4-5. The graphs also include the loops obtained in the quasi-static testing at the same amplitude of motion for comparison. The results clearly illustrate the effect of velocity in affecting friction (increase) and in causing the loops to have smooth transitions between regimes.



FIGURE 4-3 Experimental Force-Displacement Loops of Isolator in Configuration 1 for Quasi-Static Test and at Peak Velocity of 1.9in/sec



FIGURE 4-4 Experimental Force-Displacement Loops of Isolator in Configuration 1 for Quasi-Static Test and at Peak Velocity of 3.1in/sec



FIGURE 4-5 Experimental Force-Displacement Loops of Isolator in Configuration 2 for Quasi-Static test and at Peak Velocity of 3.1in/sec

Prediction by the computational model of the force-displacement loops under dynamic conditions requires (a) knowledge of the coefficient of friction-velocity relations for each sliding surface, and (b) a procedure for specifying these properties in the Triple-Double model of the isolator in program SAP2000. It is generally assumed that the coefficient of friction follows the relation

$$\mu = \mu_{FAST} - (\mu_{FAST} - \mu_{SLOW}) e^{-aV}$$
(6)

where μ_{FAST} and μ_{SLOW} are values of the coefficient of sliding friction valid for large velocity and for quasi-static conditions, respectively, *V* is the velocity of sliding, and "a" is the rate parameter used to describe the velocity-dependence of friction.

Specification of the three parameters of the model for each sliding surface is complicated by the fact that the Triple FP bearing model in program SAP2000 (also the models of Morgan, 2007 and Fenz and Constantinou, 2008a) does not truly trace the motion on the four sliding surfaces but rather simulates the behavior through the motion of the three effective pendula. The result is that the sliding velocity is not precisely known at each sliding surface but it can be estimated by the

procedure described in Fenz and Constantinou (2008c) and with details provided in Sarlis and Constantinou (2010). This requires the specification of fictitious values for the rate parameter for the three effective pendula. This is further complicated by the fact that the manual of program SAP2000 does not provide details and does not present verification examples. A comparison of the results produced by the Triple FP element in the program and the validated series model of Fenz and Constantinou (2008c) implemented in SAP2000 resulted in essentially the same results and, therefore, it is believed that the values of the rate parameter for the Triple FP element in SAP2000 should be specified using the approach outlined in Fenz and Constantinou (2008a) and Sarlis and Constantinou (2010).

 TABLE 4-3 Values of Friction Coefficient and Rate Parameter Used in Analysis of Isolator of Configuration 1 (Top Table Reports Properties of Isolator; Bottom Table Reports Parameters of Computational Model)

Quintuple Isolator	μ_1	μ_2	$\mu_3 = \mu_4$	μ_5	μ_6
$\mu_{\scriptscriptstyle SLOW}$	0.12	0.085	0.015	0.035	0.11
$\mu_{\scriptscriptstyle FAST}$	0.16	0.11	0.04	0.09	0.15
Rate parameter <i>a</i> (sec/inch)	4.0	3.6	3.0	3.6	4.0
Triple-Double Model	$ ilde{\mu}_1$	$\tilde{\mu}_2 = \tilde{\mu}_3$	$ ilde{\mu}_4$	$ ilde{\mu}_{5}$	$ ilde{\mu}_{_6}$
$ ilde{\mu}_{\scriptscriptstyle SLOW}$	0.085	0.015	0.035	0.11	0.12
$ ilde{\mu}_{\scriptscriptstyle FAST}$	0.11	0.04	0.09	0.15	0.16
Rate parameter \tilde{a} (sec/inch)	3.0	1.5	3.0	2.0	2.0

The computational model of the Quintuple FP Isolator described in Appendix B requires the use of three nodes interconnected by two Triple FP elements, one of which has been reduced to behave as a Double FP element (this is done by specifying artificial values of the radius and friction to impede motion of the inner sliding surfaces-see Table B-2b). Accordingly, the division of velocity for the sliding surfaces of the Quintuple FP model should be based on approach described in Fenz and Constantinou (2006) for the Double FP element and in Fenz and Constantinou (2008c) for the Triple FP element. Table 4-3 presents values of friction and the rate parameter used in an analysis

of the tested isolator of Configuration 1. Note that the values of the rate parameter were assumed for each sliding surface to have a value in a range consistent with what is typically assumed in analysis (e.g., Sarlis and Constantinou, 2010).

There are three sources of uncertainty in the data of Table 4-3: (a) unlike the case of quasi-static conditions, the actual values of friction at high velocity (μ_{FAST}) are not directly measured (uncertain due to the smoothness of the experimental loops) but assumed although some information was obtained from the recorded loops, (b) the actual values of the rate parameter for each sliding surface are not known but rather assumed, and (c) the values of the rate parameter in the computational model are approximate as the velocities are not directly computed but rather estimated on the basis of a simplified theory.

Figure 4-6 presents comparisons of experimental and computational force-displacement loops of the tested isolator of Configuration 1 (with the properties of Table 4-3–also see Table B-2 for other details) in the two tests at velocities of 1.9 and 3.1in/sec. The comparison is good given the several sources of uncertainty in the values of the model parameters and the fact that the sliding velocities are small (portions of the peak velocity of testing) so that there is considerable variability of friction, which would not be dominant in testing with much higher velocity. (Unfortunately, testing at higher velocities could not be performed due to instabilities in the control mechanism of the testing machine). Nevertheless, it is noted that changes in the specified values of the rate parameter resulted in noticeable changes in the computed loops for the motions used in the testing (up to 3.1in/sec) but the effects where minor or insignificant when the peak velocity was larger than 10in/sec.



FIGURE 4-6 Comparison of Experimental and Computational Force-Displacement Loops of Isolator in Configuration 1 at Peak Test Velocities of 1.9 and 3.1in/sec

SECTION 5 CONCLUSIONS

The behavior of the Quintuple Friction Pendulum Isolator has been investigated. This isolator has six spherical sliding surfaces, five effective pendula and nine regimes of operation that allow for complex adaptive behavior and smooth transition between regimes of operation. Analytical models of behavior have been presented for two configurations that are envisioned to include all cases of interest in applications. Moreover, a computational model has been developed that is readily implementable in computer program SAP2000. Comparison of results obtained by the computational and analytical model provided verification of the computational model.

A model isolator was tested and the results were compared to predictions of the analytical and computational models. The comparison demonstrated the validity of the analytical model and of the computational model. It is believed that this isolator will be a useful addition to the arsenal of isolators available to the engineer for use in the seismic protection of structures.

SECTION 6

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APPENDIX A

DERIVATION OF FORCE-DISPLACEMENT RELATIONS FOR CONFIGURATION 1

The derivation of the force-displacement relation of the quintuple FP Isolator is presented in detail for configuration 1. The force-displacement relation is derived from the equilibrium and geometric considerations following the paradigm of Fenz and Constantinou (2006 and 2008a) and distinguishing the relation in accordance with the sliding regime. In what follows, *W* is the normal load acting at the center of the top plate of the bearing, *F* is the horizontal force, $F_f = \mu W$ is the friction force, μ is assumed constant and independent of the conditions of motion (Coulomb friction) and *S* is the resultant force acting perpendicularly to a sliding surface. Moreover, the following quantities are defined in which *i*=1 to 6:

The effective radius of curvature

$$R_{eff,i} = R_i - h_i \tag{A-1}$$

The actual displacement capacity of each sliding surface:

$$d_i^* = d_i \left(R_{eff,i} / R_i \right) \tag{A-2}$$

A-1 Sliding Regime I

Sliding Regime I begins with sliding on surfaces 3 and 4 which are characterized by the least friction forces. Motion initiates when horizontal force is equal to friction force on surface 2 and 3 $(F = F_{f3} = F_{f4})$. The displaced shape (with the sliding surfaces highlighted in red) and the free body diagram (FBD) of parts C and E during Sliding Regime I are shown in Figure A-1.

Equilibrium in the vertical and horizontal directions of the FBD of part C in Figure A-1 (b) results in:

$$W + F_{f^3}\sin\theta_3 - S_3\cos\theta_3 = 0 \tag{A-3a}$$

$$F_{f^3}\cos\theta_3 + S_3\sin\theta_3 - F = 0 \tag{A-3b}$$

From geometry, the relative displacement of slider C, u_3 , is

$$u_3 = R_{eff\,3}\sin\theta_3 \tag{A-4}$$

Assuming small rotations (so that $\cos\theta \approx 1$ and $\sin\theta \approx \theta$) and rearranging equations (A-3) and (A-4), the following is derived for force *F*:

$$F = \frac{W}{R_{eff3}}u_3 + F_{f3} \tag{A-5}$$



(b)



FIGURE A-1 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime I

Similarly, equilibrium for part E leads to:

$$F = \frac{W}{R_{eff\,4}} u_4 + F_{f\,4} \tag{A-6}$$

Since $u = u_3 + u_4$ and $u_1 = u_2 = u_5 = u_6 = 0$, combination of equations (A-5) and (A-6) results in

$$F = \frac{W}{R_{eff3} + R_{eff4}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4}}{R_{eff3} + R_{eff4}}$$
(A-7)

The force-displacement loop in regime I is shown in Figure A-2. Note that on reversal motion the force drops by $2F_{f3}(=2F_{f4})$. This regime is valid until a displacement $u=u^{I}$ is reached.



FIGURE A-2 Force-Displacement Relationship in Sliding Regime I

A-2 Sliding Regime II

Sliding regime II initiates when the lateral force $F = F_{f5}$, motion on surface 4 stops, motion initiates on surface 5 and motion continues on surface 3 as shown in Figure A-3(a). This sequence of motion is required for compatibility of displacements and is consistent with what occurs in the Triple FP Isolator.

The transition displacement between sliding regimes I and II, u^{I} , is obtained by solving equation (A-7) for the displacement u when force $F = F_{f5}$:



FIGURE A-3 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime II

Based on the FBD of Figure A-3(b) and geometric considerations in similarity to the presentation for regime I, the following is obtained:

$$u_4 = R_{eff\,4} \sin \theta_4 \tag{A-9a}$$

$$u_5 = R_{eff5} \sin \theta_5 \tag{A-9b}$$

$$F = \frac{W}{R_{eff3}} u_3 + F_{f3} \tag{A-10a}$$

$$F = \frac{W}{R_{eff5}} u_5 + F_{f5} \tag{A-10b}$$

$$S_5 \cos\theta_5 + F_{f_4} \sin(\theta_4 + \theta_5) - S_4 \cos(\theta_4 + \theta_5) - F_{f_5} \sin\theta_5 = 0$$
(A-11a)

$$S_4 \sin(\theta_4 + \theta_5) + F_{f4} \cos(\theta_4 + \theta_5) - S_5 \sin\theta_5 - F_{f5} \cos\theta_5 = 0$$
 (A-11a)

Assuming small rotations, the force-displacement relation is obtained as,

$$F = W \left(\frac{u_4}{R_{eff\,4}} + \frac{u_5}{R_{eff\,5}} \right) + F_{f\,4}$$
(A-12)

Combining equations (A-10) and (A-12) and using $u = u_3 + u_4 + u_5$, the force-displacement relation in regime II is obtained:

$$F = \frac{W}{R_{eff3} + R_{eff5}} u + \frac{F_{f3}R_{eff3} + F_{f4}R_{eff4} + F_{f5}(R_{eff5} - R_{eff4})}{R_{eff3} + R_{eff5}}$$
(A-13)

This relationship is shown in Figure A-4 together with that of regime I for completeness. This regime is valid until a displacement $u=u^{II}$ is reached.



FIGURE A-4 Force-Displacement Relationship in Sliding Regime II

A-3 Sliding Regime III

The sliding regime III initiates when the lateral force $F = F_{f_2}$, motion stops on surface 3, motion begins on surface 2 and motion continues on surface 4 as shown in Figure A-5(a). The transition occurs at a displacement u^{II} obtained by solving equation (A-13) for displacement u when $F = F_{f_2}$:

$$u^{\rm II} = u^{\rm I} + (F_{f2} - F_{f5}) \times \left[(R_{eff3} + R_{eff5}) / W \right]$$
 (A-14)



FIGURE A-5 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime III

Based on the FBD of Figure A-5(b) and geometric considerations in similarity to the presentation for regimes I and II, the following is obtained:

$$u_2 = R_{eff\,2}\sin\theta_2 \tag{A-15a}$$

$$u_3 = R_{eff3} \sin \theta_3 \tag{A-15b}$$

$$F = \frac{W}{R_{eff\,2}} u_2 + F_{f\,2} \tag{A-16}$$

$$F = W \left(\frac{u_2}{R_{eff\,2}} + \frac{u_3}{R_{eff\,3}} \right) + F_{f\,3}$$
(A-17)

The force-displacement relationship in sliding regime III is finally obtained by combining equations (A-10b), (A-12), (A-16) and (A-17) and using $u = u_2 + u_3 + u_4 + u_5$:

$$F = \frac{W}{R_{eff\,2} + R_{eff\,5}} u + \frac{F_{f\,2} \left(R_{eff\,2} - R_{eff\,3}\right) + F_{f\,3} R_{eff\,3} + F_{f\,4} R_{eff\,4} + F_{f\,5} \left(R_{eff\,5} - R_{eff\,4}\right)}{R_{eff\,2} + R_{eff\,5}} \tag{A-18}$$

This relationship is shown in Figure A-6 together with those for regimes II and III. This regime is valid until a displacement $u=u^{III}$ is reached.



FIGURE A-6 Force-Displacement Relationship in Sliding Regime III

A-4 Sliding Regime IV

The sliding regime IV initiates when the lateral force $F = F_{f6}$, motion stops on surface 5, motion begins on surface 6 and motion continues on surface 2 as shown in Figure A-7(a). The transition occurs at a displacement u^{III} obtained by solving equation (A-18) for displacement u when $F = F_{f6}$:



FIGURE A-7 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime IV

Based on the FBD of Figure A-7(b) and geometric considerations in similarity to the presentation for regimes I to III, the following is obtained:

$$u_6 = R_{eff \, 6} \sin \theta_6 \tag{A-20}$$

$$F = \frac{W}{R_{eff6}} u_6 + F_{f6}$$
 (A-21)

$$F = W \left(\frac{u_5}{R_{eff5}} + \frac{u_6}{R_{eff6}} \right) + F_{f5}$$
 (A-22)

The equilibrium equations for part E are obtained by considering the FBD shown in Figure A-7(b) and accounting for the its rotation:

$$S_{5}\cos(\theta_{5}+\theta_{6})+F_{f4}\sin(\theta_{4}+\theta_{5}+\theta_{6})-S_{4}\cos(\theta_{4}+\theta_{5}+\theta_{6})-F_{f5}\sin(\theta_{5}+\theta_{6})=0 \quad (A-23a)$$

$$S_{4}\sin(\theta_{4}+\theta_{5}+\theta_{6})+F_{f4}\cos(\theta_{4}+\theta_{5}+\theta_{6})-S_{5}\sin(\theta_{5}+\theta_{6})-F_{f5}\cos(\theta_{5}+\theta_{6})=0$$
 (A-23b)

Assuming small displacements, equations (A-23) can be solved for force F:

$$F = W\left(\frac{u_4}{R_{eff\,4}} + \frac{u_5}{R_{eff\,5}} + \frac{u_6}{R_{eff\,6}}\right) + F_{f\,4} \tag{A-24}$$

Inspection of free body diagrams of parts B and C in Figure A-7(b) shows that parts B and C experience in regime IV only an increase in angle θ_2 by comparison to regime III. Thus, the forcedisplacement relationships for parts B and C are still governed by equations (A-16) and (A-17). Therefore, the force and total displacement relationship in sliding regime IV can be obtained by combining equations (A-16), (A-17), (A-21), (A-22), and (A-24) and using $u = u_2 + u_3 + u_4 + u_5 + u_6$:

$$F = \frac{W}{R_{eff\,2} + R_{eff\,6}}u + \frac{F_{f\,2}\left(R_{eff\,2} - R_{eff\,3}\right) + F_{f\,3}R_{eff\,3} + F_{f\,4}R_{eff\,4} + F_{f\,5}\left(R_{eff\,5} - R_{eff\,4}\right) + F_{f\,6}\left(R_{eff\,6} - R_{eff\,5}\right)}{R_{eff\,2} + R_{eff\,6}}$$
(A-25)

This relationship is shown in Figure A-8 together with those for the previous regimes. This regime is valid until a displacement $u=u^{IV}$ is reached.



FIGURE A-8 Force-Displacement Relationship in Sliding Regime IV

A-5 Sliding Regime V

The sliding regime V initiates when the lateral force $F = F_{f_1}$, motion stops on surface 2, motion begins on surface 1 and motion continues on surface 6 as shown in Figure A-9(a). The transition occurs at a displacement u^{IV} obtained by solving equation (A-25) for displacement u when $F = F_{f_1}$:

$$u^{\rm IV} = u^{\rm III} + (F_{f1} - F_{f6}) \times \left[(R_{eff2} + R_{eff6}) / W \right]$$
(A-26)

Based on the FBD of Figure A-9(b) and geometric considerations in similarity to the presentation for regimes I to IV, the following is obtained:

$$u_1 = R_{eff1} \sin \theta_1 \tag{A-27}$$

$$F = \frac{W}{R_{eff1}} u_1 + F_{f1}$$
 (A-28)

$$F = W \left(\frac{u_1}{R_{eff1}} + \frac{u_2}{R_{eff2}} \right) + F_{f2}$$
 (A-29)

$$F = W\left(\frac{u_1}{R_{eff1}} + \frac{u_2}{R_{eff2}} + \frac{u_3}{R_{eff3}}\right) + F_{f3}$$
(A-30)



FIGURE A-9 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator in Sliding Regime V

The force-displacement relation in regime V is obtained by combining equations (A-21), (A-22), (A-24), (A-28), (A-29) and (A-30) and using $u = u_1 + u_2 + u_3 + u_4 + u_5 + u_6$:

$$F = \frac{W}{R_{eff1} + R_{eff6}} u + \frac{F_{f1} \left(R_{eff1} - R_{eff2} \right) + F_{f2} \left(R_{eff2} - R_{eff3} \right) + F_{f3} R_{eff3} + F_{f4} R_{eff4} + F_{f5} \left(R_{eff5} - R_{eff4} \right) + F_{f6} \left(R_{eff6} - R_{eff5} \right)}{R_{eff1} + R_{eff6}}$$
(A-31)

This relationship is shown in Figure A-10 together with those for the previous regimes. This regime is valid until a displacement $u = u_{dr6}$ is reached.



FIGURE A-10 Force-Displacement Relationship in Sliding Regime V

A-6 Sliding Regime VI

The sliding regime VI initiates when part F of the isolator contacts the restrainer of part G so that motion on surface 6 stops, motion starts on surface 5 and motion continues on surface 1 as shown in Figure A-11(a). This occurs at a displacement equal to u_{dr6} .



FIGURE A-11 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator in Sliding Regime VI

At the point of transition, the displacement on surface 6 is $u_6 = d_6^*$ and the horizontal force *F* is given by the following equation and termed F_{dr6}

$$F_{dr6} = \frac{W}{R_{eff6}} d_6^* + F_{f6}$$
 (A-32)

Displacement u_{dr_6} is obtained by solving equation (A-31) for the displacement and using $F = F_{dr_6}$:

$$u_{dr6} = u^{\rm IV} + (F_{dr6} - F_{f1}) \times \left[(R_{eff1} + R_{eff6}) / W \right]$$
(A-33)

Based on the FBD of Figure A-11(b) and geometric considerations in similarity to the presentation for regimes I to V, the following equations are obtained:

$$F = \frac{W}{R_{eff\,6}} d_6^* + F_{f\,6} + F_{r\,6} \tag{A-34}$$

$$F = W\left(\frac{u_5}{R_{eff5}} + \frac{d_6^*}{R_{eff6}}\right) + F_{f5}$$
(A-35)

$$F = W\left(\frac{u_4}{R_{eff\,4}} + \frac{u_5}{R_{eff\,5}} + \frac{d_6^*}{R_{eff\,6}}\right) + F_{f\,4}$$
(A-36)

The force-displacement relation in regime VI is obtained by combining equations (A-28), (A-29), (A-30), (A-35) and (A-36) and using $u = d_1^* + u_2 + u_3 + u_4 + u_5 + u_6$:

$$F = \frac{W}{R_{eff1} + R_{eff5}} (u - u_{dr6}) + F_{dr6}$$
(A-37)

This relationship is shown in Figure A-12 together with those for the previous regimes. This regime is valid until a displacement $u=u_{dr1}$ is reached. The unloading process is same as regime V until the lateral force drops by amount $2F_{f2}$. Motion then starts on surface 6 when the horizontal force drops by $F_{r6} + 2F_{f6}$, that is, when the horizontal force is equal to

$$F = F_{dr6} - 2F_{f6} \tag{A-38}$$

For this to occur, the condition $F_{dr6} - 2F_{f6} > F - 2F_{f1}$ must be valid or, otherwise, motion will start on surface 1 instead of 6. Accordingly, motion occurs on surface 1 when the displacement satisfies the following condition

$$u > u_{dr6} + 2(\mu_1 - \mu_6)(R_{eff1} + R_{eff5})$$
(A-39)

However, based on equation (A-41b) that follows, for typical configurations with $d_1^* = d_6^*$ and $R_{eff1} = R_{eff6}$, equation (A-39) will not be satisfied prior to the start of sliding regime VII. Thus for typical configurations, motion will start on surface 6 prior to surface 1, as shown in Figure A-12.



FIGURE A-12 Force-Displacement Relationship During Sliding Regime VI

A-7 Sliding Regime VII

The sliding regime VII initiates when part B of the isolator contacts the restrainer of part A so that motion on surface 1 stops, motion starts on surface 2 and motion continues on surface 5 as shown in Figure A-13(a). This occurs at a displacement equal to u_{dr1} .



FIGURE A-13 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime VII

At the transition point, the displacement on surface 1 is $u_1 = d_1^*$ and the horizontal force *F* is given by the following equation and termed F_{dr1}

$$F_{dr1} = \frac{W}{R_{eff1}} d_1^* + F_{f1}$$
 (A-40)

Displacement u_{dr1} is obtained by solving equation (A-37) for the displacement and using $F=F_{dr1}$:

$$u_{dr1} = u_{dr6} + (F_{dr1} - F_{dr6}) \times \left[(R_{eff1} + R_{eff5}) / W \right]$$
 (A-41a)

or

$$u_{dr1} = u_{dr6} + \left[\left(\frac{d_1^*}{R_{eff1}} + \mu_1 \right) - \left(\frac{d_6^*}{R_{eff6}} + \mu_6 \right) \right] \left(R_{eff1} + R_{eff5} \right)$$
(A-41b)

Based on the FBD in Figure A-13(b) and geometric considerations in similarity to the presentation for regimes I to VI, the followings is obtained:

$$F = \frac{W}{R_{eff1}} d_1^* + F_{f1} + F_{r1}$$
(A-42)

$$F = W\left(\frac{d_1^*}{R_{eff1}} + \frac{u_2}{R_{eff2}}\right) + F_{f2}$$
(A-43)

$$F = W\left(\frac{d_1^*}{R_{eff1}} + \frac{u_2}{R_{eff2}} + \frac{u_3}{R_{eff3}}\right) + F_{f3}$$
(A-44)

The force-displacement relation in regime VII is obtained by combining equations (A-34), (A-35), (A-36), (A-43) and (A-44) and using $u = d_1^* + u_2 + u_3 + u_4 + u_5 + d_6^*$:

$$F = \frac{W}{R_{eff\,2} + R_{eff\,5}} \left(u - u_{dr1} \right) + F_{dr1} \tag{A-45}$$

This relationship is shown in Figure A-14 together with those for the previous regimes. This regime is valid until a displacement u_{dr5} is reached. The unloading process is the same as that of regime VI until the lateral force drops by $2F_{f2}$. Motion then starts on surface 6 to be followed by

motion on surface 1. For this to occur, the condition $F_{dr6} - 2F_{f6} > F_{dr1} - 2F_{f1}$ must be valid or, otherwise, motion will start on surface 1 and will be followed by motion on surface 6. For typical configurations ($d_1^* = d_6^*$ and $R_{eff1} = R_{eff6}$), motion will start on surface 6 prior to surface 1, as shown in Figure A-14.



FIGURE A-14 Force-Displacement Relationship During Sliding Regime VII

A-8 Sliding Regime VIII

The sliding regime VIII initiates when part E of the isolator contact to the restrainer of slider F so that motion on surface 5 stops, motion resumes on surface 4 and motion continues on surface 2 as shown in Figure 15(a). This occurs at a displacement equal to u_{dr5} .



FIGURE A-15 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime VIII

At the transition point, the displacement on surface 5 is $u_5 = d_5^*$ and the horizontal force *F* is given by the following equation and termed F_{dr5}

$$F_{dr5} = W \left(\frac{d_5^*}{R_{eff5}} + \frac{d_6^*}{R_{eff6}} \right) + F_{f5}$$
(A-46)

Displacement u_{dr5} is determined by solving equation (A-46) for the displacement and using $F = F_{dr5}$:

$$u_{dr5} = u_{dr1} + (F_{dr5} - F_{dr1}) \times \left[(R_{eff\,2} + R_{eff\,5}) / W \right]$$
(A-47)

From the FBD in Figure A-15(b) and geometric considerations in similarity to the presentation for regimes I to VII, the followings is obtained:

$$F = \frac{W}{R_{eff\,6}} d_6^* + F_{f\,6} + F_{r\,6} \tag{A-48}$$

$$F = W\left(\frac{d_5^*}{R_{eff\,5}} + \frac{d_6^*}{R_{eff\,6}}\right) + F_{f\,5} + F_{r\,5}$$
(A-49)

$$F = W\left(\frac{u_4}{R_{eff\,4}} + \frac{d_5^*}{R_{eff\,5}} + \frac{d_6^*}{R_{eff\,6}}\right) + F_{f\,4} \tag{A-50}$$

The force-displacement relation in regime VIII is obtained combining equations (A-43), (A-44) and (A-50) and using $u = d_1^* + u_2 + u_3 + u_4 + d_5^* + d_6^*$:

$$F = \frac{W}{R_{eff\,2} + R_{eff\,4}} \left(u - u_{dr5} \right) + F_{dr5}$$
(A-51)

This relationship is shown in Figure A-16 together with those for the previous regimes. This regime is valid until a displacement u_{dr2} is reached. Upon reversal of motion, the lateral force drops by $2F_{f3}(=2F_{f4})$. Motion then starts on surface 5 when the horizontal force is equal to $F_{dr5} - 2F_{f5}$. For this to occur, the condition $F_{dr5} - 2F_{f5} > F - 2F_{f2}$ must be valid or, otherwise,

motion will start on surface 2 instead of 5. Based on the similar analysis in regime VI, motion will start on surface 5 prior to surface 2 for typical configurations ($R_{eff\,2} = R_{eff\,5}$ and $d_2^* = d_5^*$), as shown in Figure A-16. Motion then follows on the surfaces 1 and 6, as presented in regime VII.



FIGURE A-16 Force-Displacement Relationship During Sliding Regime VIII

A-9 Sliding Regime IX

The sliding regime IX begins when part C of the isolator contacts the restrainer of part B, so that motion stops on surface 2, motion resumes on surface 3 and motion continues on surface 4, as shown in Figure A-17(a). This occurs at a displacement equal to u_{dr2} .



FIGURE A-17 Displaced Shape (a) and Free Body Diagrams (b) of the Quintuple FP Isolator During Sliding Regime IX

At the transition point, the displacement on surface 2 is $u_2 = d_2^*$ and the horizontal force *F* is given by the following equation and termed F_{dr2}

$$F_{dr2} = W\left(\frac{d_1^*}{R_{eff1}} + \frac{d_2^*}{R_{eff2}}\right) + F_{f2}$$
(A-52)

Displacement u_{dr^2} is obtained by solving equation (A-51) for the displacement and using $F = F_{dr^2}$:

$$u_{dr2} = u_{dr5} + (F_{dr2} - F_{dr5}) \times \left[(R_{eff2} + R_{eff4}) / W \right]$$
(A-53)

Based on FBD in Figure A-17 (b) and geometric considerations in similarity to the presentation for regimes I to VIII, the followings are obtained:

$$F = \frac{W}{R_{eff1}} d_1^* + F_{f1} + F_{r1}$$
(A-54)

$$F = W \left(\frac{d_1^*}{R_{eff1}} + \frac{d_2^*}{R_{eff2}} \right) + F_{f2} + F_{r2}$$
(A-55)

$$F = W\left(\frac{d_1^*}{R_{eff1}} + \frac{d_2^*}{R_{eff2}} + \frac{u_3}{R_{eff3}}\right) + F_{f3}$$
(A-56)

The force-displacement relation in regime IX is obtained by combining equations (A-50) and (A-56) and using $u = d_1^* + d_2^* + u_3 + u_4 + d_5^* + d_6^*$:

$$F = \frac{W}{R_{eff3} + R_{eff4}} \left(u - u_{dr5} \right) + F_{dr2}$$
(A-57)

This relationship is shown in Figure A-18 together with those for the previous regimes. This regime is valid until total displacement capacity is reached. Upon reversal of motion, the lateral force drops by $2F_{f3}(=2F_{f4})$. Motion then starts on surface 5 instead of surface 2. For this to occur, the condition F_{dr5} - $2F_{f5}$ > F_{dr2} - $2F_{f2}$ must be valid or, otherwise, motion will start on surface 2 instead of surface 5 prior to surface 2. For typical configurations ($R_{eff2} = R_{eff5}$ and $d_2^* = d_5^*$), motion will start on surface. Motion then follows on the surfaces 1 and 6, as presented in regime VII.


FIGURE A-18 Force-Displacement Relationship During Sliding Regime IX

APPENDIX B

DETAILS OF COMPUTATIONAL MODEL IN PROGRAM SAP2000

B-1 Computational Model for the Isolator in Table 3-3

Figure B-1 presents a section of the analyzed isolator that shows the dimensional and the frictional parameters (friction is constant in this analysis). This is the isolator of Configuration 1 with the properties presented in Table 3-3 and with force-displacement loops shown in Figure 3-5.



FIGURE B-1 Geometrical and Frictional Properties of Analyzed Quintuple FP Isolator

Figure B-2 illustrates the model of the isolator used in program SAP2000 for simulating the behavior of a single isolator under imposed gravity load *W* and lateral history of prescribed displacement. A rigid massless bar was used to connect two identical isolators and impose motion through a control point. Each of the two isolators in the model represented the analyzed isolator carrying the load *W*. The model depicted in Figure B-2 is for the case of using the Triple FP element of SAP2000. Table B-1a presents the effective properties of the analyzed isolator that were used to calculate the properties of elements used in the computational model.



FIGURE B-2 Model of Quintuple FP Isolator for Analysis in Program SAP2000

The input parameters for each of the Triple FP and the Double FP elements in program SAP2000 utilized in the simulation are presented in Table B-1b. These parameters include the radii of curvature, the friction coefficient values, and the displacement capacities (defined as stop distances in SAP2000). It is noted that the "fast" and "slow" values of the coefficient of friction were specified equal and the rate parameter in the SAP2000 elements was defined as zero (or an arbitrary value) so that there is no velocity dependence of the coefficient of friction. Other parameters such as element mass, effective stiffness and rotational moment of inertia did not have any noticeable effect in the analysis results as long as they were selected to reasonably represent properties of the isolator. The values for element mass and rotational moment of inertia were properly estimated considering the isolator geometry. The effective stiffness in SAP2000 was selected to be half of that of the isolator at a displacement equal to half of the isolator displacement capacity. This stiffness was then assigned to the triple FP and double FP elements in a series. The vertical stiffness was calculated as the stiffness of a column having the height of the isolator (19 inch) and diameter equal to the diameter of part D of the isolator (18 inch) and distributed on the basis of the details provided in the document of Sarlis and Constantinou (2010). The rotational and torsional stiffness were specified to be zero.

TABLE B-1a Effective Properties of Quintuple FP Isolator and Properties in Computational Modelin SAP2000 per Table 3-3 (Top Table Reports Properties of Isolator; Bottom Table ReportsParameters of SAP2000 Model)

Sliding surface		Radius of curvature (in)	adius of curvature Coefficient of friction (in)		
Surface 1		$R_{eff1} = 230$	$\mu_1 = 0.10$	$d_1^* = 13.53$	
Surface 2		$R_{eff 2} = 44$	$\mu_2 = 0.06$	$d_2^* = 5.28$	
Surface 3		$R_{eff3} = 20$	$\mu_3 = 0.01$	$d_3^* = 1.875$	
Surface 4		$R_{eff 4} = 20$	$\mu_4 = 0.01$	$d_4^* = 1.875$	
Surface 5		$R_{eff5}=44$	$\mu_{5} = 0.03$	<i>d</i> [*] ₅ =5.28	
Surface 6		$R_{eff6} = 148$ $\mu_6 = 0.07$		$d_{6}^{*}=13.28$	
Sliding surface		Radius of curvature (in)	Coefficient of friction	Displacement capacity (in)	
	Lower surface	$ ilde{R}_{eff1} = 44$	$ ilde{\mu}_1 = 0.06$	$\tilde{d}_1 = 7.868$	
Triple FP Element	Inner surfaces	$\tilde{R}_{eff2,3} = 20$	$\tilde{\mu}_{2,3} = 0.01$	\tilde{d}_2 , $\tilde{d}_3 = 1.875$	
	Upper surface	$ ilde{R}_{e\!f\!f4} = 44$	$\tilde{\mu}_4 = 0.03$	$\tilde{d}_4 = 9.229$	
Double FP Element	Upper surface	$\tilde{R}_{eff5} = 104$	$\tilde{\mu}_5 = 0.07$	$\tilde{d}_5 = 9.333$	
	Lower surface	$ ilde{R}_{eff6} = 186$	$\tilde{\mu}_6 = 0.10$	$\tilde{d}_6 = 10.941$	

TABLE B-1b Values of Parameters of Elements in Program SAP2000 in Case without Velocity-Dependence of Friction per Table 3-3

Models	Triple FP			Double FP		
Sliding surface	Lower	Inner Surfaces	Upper	Upper	¹ Inner Surfaces	Lower
Radius of sliding surface (inch)	44	20	44	104	0	186
Friction coefficient (FAST and SLOW)	0.03	0.01	0.06	0.07	1	0.10
Rate parameter (sec/in)	0	0	0	0	0	0
Stop distance (inch)	9.229	1.875	7.868	9.333	0	10.941
Supported weight (kip)	900	900	900	900	900	900
Yield displacement (inch)	0.01	0.01	0.01	0.01	0.01	0.01
Stiffness (elastic) (kip/in)	1350	450	2700	3150	² 3825	4500
Effective stiffness (kip/in)	5.6			5.6		
Rotational moment of inertia (kip-in-sec ²)	0.05			0		
Element height (inch)	9.5			9.5		
Shear deformation location (in)-(distance from top joint of FP element)	4.75			4.75		
Element mass (kip-s ² /in)	0.001		0.001			
Vertical stiffness (kip/in)		323,667		485,500		
Rotational / torsional stiffness (R1,R2,R3)	0		fixed			

¹Values of parameters specified for inner surfaces in Double FP element are artificial and intend to impede motion at the inner sliding surfaces, specifically (a) zero for radius and stop distance and (b) unity for friction.

 2 Value arbitrarily selected to be average of values for upper and lower parts. Very large values should not be used as they result in convergence problems.

B-2 Computational Model for the Isolator in Table 4-1

Figure B-3 presents a section of the tested isolator that shows the dimensional and frictional parameters (friction values are for quasi-static conditions). This is the isolator with the properties presented in Table 4-1 and with force-displacement loops shown in Figure 4-2.

A computational model of the tested isolator was also constructed based on the approach described above. The properties for the tested isolator used in computational model are presented in Tables B-2a (actual properties) and B-2b (input parameters for each of the Triple FP and Double FP elements).



FIGURE B-3 Geometrical and Frictional Properties of Tested Quintuple FP Isolator

TABLE B-2a Effective Properties of the Tested Isolator and Properties in Computational Model in SAP2000 per Table 4-1 (Top Table Reports Properties of Isolator; Bottom Table Reports Parameters of SAP2000 Model)

Sliding surface		Radius of curvature (in)	adius of curvature Coefficient of friction (in)		
Surface 1		$R_{eff1} = 16.6$	$\mu_1 = 0.12$	$d_1^* = 1.383$	
Surface 2		$R_{eff2} = 6.8$	$\mu_2 = 0.085$	$d_2^* = 1.105$	
Surface 3		$R_{eff3} = 1.1$	$\mu_3 = 0.015$	$d_3^* = 0.303$	
Surface 4		$R_{eff4} = 1.1$ $\mu_4 = 0.015$		$d_4^* = 0.303$	
Surface 5		$R_{eff5}=6.8$	$\mu_{5} = 0.035$	$d_5^* = 1.105$	
Surface 6		$R_{eff6} = 16.6$	$\mu_6 = 0.11$	$d_6^* = 1.383$	
Sliding surface		Radius of curvature (in)	Coefficient of friction	Displacement capacity (in)	
	Lower surface	$\tilde{R}_{eff1} = 6.8$	$\tilde{\mu}_1 = 0.085 (0.11)$	$\tilde{d}_1 = 1.672$	
Triple FP Element	Inner surfaces	$\tilde{R}_{eff2,3} = 1.1$	$\tilde{\mu}_{2,3} = 0.015(0.04)$	$\tilde{d}_2, \; \tilde{d}_3 = 0.303$	
	Upper surface	$\tilde{R}_{eff4} = 6.8$	$\tilde{\mu}_4 = 0.035(0.09)$	$\tilde{d}_1 = 1.672$	
Double FP Element	Upper surface	$\tilde{R}_{eff5} = 9.8$	$\tilde{\mu}_5 = 0.11(0.15)$	$\tilde{d}_5 = 0.816$	
	Lower surface	$\tilde{R}_{eff6} = 9.8$	$\tilde{\mu}_6 = 0.12 \ (0.16)$	$\tilde{d}_6 = 0.816$	

TABLE B-2b Values of Parameters of Elements in Program SAP2000 in Case without Velocity-Dependence of Friction per Table 4-1 (Values in Parenthesis are for Case with Velocity-Dependence of Friction)

Models	Triple FP			Double FP		
Sliding surface	Lower	Inner Surfaces	Upper	Upper	Inner Surfaces	Lower
Radius of sliding surface (inch)	6.8	1.1	6.8	9.8	0	9.8
Friction coefficient SLOW	0.085	0.015	0.035	0.11	1	0.12
Friction coefficient FAST	0.085 (0.11)	0.015 (0.04)	0.035 (0.09)	0.11 (0.15)	1 (1)	0.12 (0.16)
Rate parameter (sec/in)	0 (3.0)	0 (1.5)	0 (3.0)	0 (2.0)	0 (0)	0 (2.0)
Stop distance (inch)	1.672	0.303	1.672	0.816	0	0.816
Supported weight (kip)	20	20	20	20	20	20
Yield displacement (inch)	0.01	0.01	0.01	0.01	0.01	0.01
Stiffness (elastic) (kip/in)	110	40	90	150	155	160
Effective stiffness (kip/in)	1.25			1.25		
Rotational moment of inertia (kip-in-sec ²)	1.455×10 ⁻⁴			0		
Element height (inch)	1.95		1.95			
Shear deformation location (in)- (distance from top joint of FP element)	0.975		0.975			
Element mass (kip-s ² /in)	0.0001		0.0001			
Vertical stiffness (kip/in)	10,945		16,417			
Rotational / torsional stiffness (R1,R2,R3)	s 0			fixed		

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