

a.)

- By checking the final slop (- 40 db/dec), we know the difference of orders (Denominator – Numerator) is 2. Besides, no rising for phase plot but all the way through to – 180°, therefore, we conclude "no zeros" and with damping ratio less than 0.707 (due to the peak on the magnitude plot).
- 2. The Transfer Function should have the form as:  $\frac{K}{\omega_n^2 \left[ \left( \frac{S^2}{\omega_n^2} \right) + \left( \frac{2\zeta S}{\omega_n} \right) + 1 \right]}$
- 3. Substitute  $S = i\omega$  into T.F., we have our F.R.F.
- 4. From 90° crossing, we know  $\omega_n \cong 3 \text{ (rad/sec)}$ .
- 5. For  $\omega \ll \omega_n$ ,  $20\log(FRF) \cong 20\log(\frac{K}{3^2}) \cong -4(db)$ .  $\Rightarrow K \cong 5.7$
- 6. For  $\omega = \omega_n$ ,  $20\log(FRF) \cong 20\log(\frac{K}{3^2}) 20\log(2\xi) \cong -4 20\log(2\xi)$  $\cong 4.5(db), \Rightarrow \xi \cong 0.19$

7. Therefore, our T.F. is approximately:  $\frac{5.7}{S^2 + 1.14S + 9}$ 

[Note: The Bode plot above is actually generated by  $T.F. = \frac{5}{S^2 + S + 9}$ ]

b.) When  $\omega = 4$ , and from plot we know that  $20\log(\frac{Output}{Input}) \approx -4.13 (db)$ ,

$$\left|\frac{Output}{Input}\right| = 10^{-\frac{4.13}{20}} \cong 0.6216$$
; hence,  $|Output| = 5 * 0.6216 \cong 3.1$ . From the phase

plot, we know the  $\phi \cong -150^{\circ}$ . Therefore,  $Output \equiv 3.1 \sin(4t - 150^{\circ})$ .

[Note: the phase angle is in "rad" for "4t" part.]

- c.) Output = Input  $\Rightarrow$  find 0 (db). From Magnitude plot, we have  $\omega \approx 2.1 \& 3.5 (rad / sec)$ .
- d.) From Magnitude plot, the "peak" happens at  $\omega \approx 2.9(rad/sec)$ .
- e.) One-tenth of the peak  $\Rightarrow -20(db)$  from the peak. From Magnitude plot, it happens at  $\omega \cong 6.2(rad/sec)$ .
- f.) Exactly out of phase  $\Rightarrow$  Phase angle has 180° difference. From Phase plot, it happens at  $\omega \cong \ge 10(rad/sec)$ .



a.) T.F. is given.

b.) When  $\omega = 4$ , and from plot we know that  $20\log(\left|\frac{Output}{Input}\right|) \approx -10.5 (db)$ ,

 $\left|\frac{Output}{Input}\right| = 10^{-\frac{10.5}{20}} \cong 0.3$ ; hence,  $|Output| = 5*0.3 \cong 1.5$ . From the phase plot, we

know the  $\phi \cong 9.9^{\circ}$ . Therefore,  $Output \equiv 1.5 \sin(4t + 9.9^{\circ})$ . [Note: the phase angle is in "rad" for "4t" part.]

- c.) Output = Input  $\Rightarrow$  find 0 (db). From Magnitude plot, we have NONE.
- d.) From Magnitude plot, the "peak" happens at  $\omega \approx 4.91 (rad/sec)$ .
- e.) One-tenth of the peak  $\Rightarrow -20(db)$  from the peak. From Magnitude plot, it happens at  $\omega \cong 28.7(rad/sec)$ .
- f.) Exactly out of phase ⇒ Phase angle has 180° difference. From Phase plot, we have NONE.



a.) T.F. is given.

b.) When  $\omega = 4$ , and from plot we know that  $20\log(\frac{Output}{Input}) \cong -42.4 (db)$ ,

 $\left|\frac{Output}{Input}\right| = 10^{-\frac{42.4}{20}} \cong 0.0076$ ; hence,  $|Output| = 5 * 0.0076 \cong 0.038$ . From the phase

plot, we know the  $\phi \cong 8.5^{\circ}$ . Therefore,  $Output \equiv 0.038 \sin(4t + 8.5^{\circ})$ . [Note: the phase angle is in "rad" for "4t" part.]

- c.) Output = Input  $\Rightarrow$  find 0 (db). From Magnitude plot, we have  $\omega \cong 59 \& \omega \ge 1000 (rad / sec)$ .
- d.) From Magnitude plot, the "peak" happens at  $\omega \cong 82.7 (rad/sec)$ .
- e.) One-tenth of the peak  $\Rightarrow -20(db)$  from the peak. From Magnitude plot, it happens at  $\omega \cong 37.8(rad/sec)$ .
- f.) Exactly out of phase ⇒ Phase angle has 180° difference. From Phase plot, we have NONE.



a.) T.F. is given.

b.) When  $\omega = 4$ , and from plot we know that  $20\log(\frac{Output}{Input}) \cong -72.4 (db)$ ,

$$\left|\frac{Output}{Input}\right| = 10^{-\frac{72.4}{20}} \approx 0.00024$$
; hence,  $|Output| = 5*0.00024 \approx 0.012$ . From the

phase plot, we know the  $\phi \cong 143^{\circ}$ . Therefore,  $Output \equiv 0.012 \sin(4t + 143^{\circ})$ .

[Note: the phase angle is in "rad" for "4t" part.]

- c.) Output = Input  $\Rightarrow$  find 0 (db). From Magnitude plot, we have NONE.
- d.) From Magnitude plot, the "peak" happens at  $\omega \cong 84(rad/sec)$ .
- e.) One-tenth of the peak  $\Rightarrow -20(db)$  from the peak. From Magnitude plot, it happens at  $\omega \cong 21.1 \& \omega \cong 332(rad/sec)$ .
- f.) Exactly out of phase ⇒ Phase angle has 180° difference. From Phase plot, we have NONE.