Deployment Analysis in Underwater Acoustic Wireless Sensor Networks

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ABSTRACT

In this paper, different deployment strategies for two-dimensional and three-dimensional communication architectures for UnderWater Acoustic Sensor Networks (UW-ASNs) are proposed, and statistical deployment analysis for both architectures is provided. The objectives of this paper are to determine the minimum number of sensors needed to be deployed to achieve the optimal sensing and communication coverage, which are dictated by the application; provide guidelines on how to choose the optimal deployment surface area, given a target region; study the robustness of the sensor network to node failures, and provide an estimate of the number of redundant sensors to be deployed to compensate for possible failures.

Categories and Subject Descriptors:

C.2.1 [Computer-Communication Networks]: Network Architecture and Design-Network topology

General Terms: Design, Performance, Reliability.

Keywords: Underwater Acoustic Sensor Networks, Deployment.

1. INTRODUCTION

Underwater sensor networks are envisioned to enable applications for oceanographic data collection, ocean sampling, environmental and pollution monitoring, offshore exploration, disaster prevention, tsunami and seaquake warning, assisted navigation, distributed tactical surveillance, and mine reconnaissance. There is, in fact, significant interest in monitoring aquatic environments for scientific, environmental, commercial, safety, and military reasons. While there is a need for highly precise, real-time, fine grained spatio-temporal sampling of the ocean environment, current methods such as remote telemetry and sequential local sensing cannot satisfy many application needs, which call for wireless underwater acoustic networking. UnderWater Acoustic Sensor Networks (UW-ASN) [1] consist of sensors that are deployed to perform collaborative monitoring tasks over a given region. UW-ASN communication links are based on acoustic wireless technology, which poses unique challenges due to the harsh underwater environment, such

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as limited bandwidth capacity [7], high and variable propagation delays [3], high bit error rates, and temporary losses of connectivity caused by multipath and fading phenomena [8].

We consider two communication architectures for UW-ASNs, i.e., the *two-dimensional architecture*, where sensors are anchored to the bottom of the ocean, and the *three-dimensional architecture*, where sensors float at different ocean depths covering the entire monitored volume region. While the former is designed for networks whose objective is to monitor the ocean bottom, the latter is more suitable to detect and observe phenomena that cannot be adequately observed by means of ocean bottom sensor nodes. We propose different deployment strategies, and provide a mathematical analysis to study deployment issues concerning both architectures, with the objectives below:

- i) Determine the minimum number of sensors needed to be deployed to achieve the target sensing and communication coverage, which are dictated by the application;
- ii) Provide guidelines on how to choose the optimal deployment surface area, given a target region;
- iii) Study the robustness of the sensor network to node failures, and provide an estimate of the number of redundant sensors to be deployed to compensate for possible failures.

The remainder of this paper is organized as follows. In Section 2, we review related literature. In Section 3, we describe the two-dimensional and three-dimensional architectures for UW-ASNs, and discuss the relevant deployment challenges. In Section 4, we derive geometric properties of the triangular-grid deployment, evaluate the trajectory of a sinking device under the presence of ocean currents, compute the deployment surface area to deploy sensors when a 2D bottom target area needs to be covered, and provide an estimate of the number of redundant sensors to compensate for possible failures. In Section 5, we propose and compare through simulation experiments three deployment strategies for 3D UW-ASNs. Finally, in Section 6, we draw the main conclusions.

2. RELATED WORK

The problem of sensing and communication coverage for terrestrial sensor networks has been addresses in several papers. However, to the best of the authors' knowledge, this work is the first to study deployment issues for underwater sensor networks. Many previous deployment solutions and theoretical bounds assuming spatio-temporal correlation, mobile sensors, redeployment of nodes, and particular deployment grid structures may not be feasible for the underwater environment.

In particular, in [6], methods for determining network connectivity and coverage given a node-reliability model are discussed, and an estimate of the minimum required node-reliability for meeting

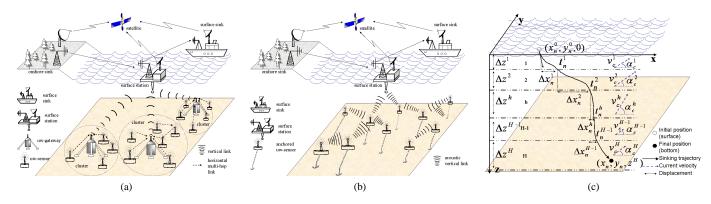


Figure 1: Architectures for two-dimensional (a) and three-dimensional (b) UW-ASNs; (c): Trajectory of a sinking object

a system-reliability objective is provided. An interesting result is that connectivity does not necessarily imply coverage. As the nodereliability decreases, in fact, the sufficient condition for connectivity becomes weaker than the necessary condition for coverage. Although [6] provides useful theoretical bounds and insight into the deployment of wireless terrestrial sensor networks, the analysis is limited to grid structures. In [2], two coordination sleep algorithms are compared, a random and a coordinated sleep scheme. It is shown that when the density of the network increases, the duty cycle of the network can be decreased for a fixed coverage. Although [2] provides sound coverage algorithms for terrestrial sensor networks, its results cannot be directly applied to the underwater environment where the sensor density is much lower than in the terrestrial case, and spatio-temporal correlation cannot often be assumed [1]. In [9], sensor coverage is achieved by moving sensor nodes after an initial random deployment. However, [9] requires either mobile sensor nodes or redeployment of nodes, which may not be feasible for UW-ASNs. In [4], sensing and communication coverage in a three-dimensional environment are rigorously investigated. The diameter, minimum and maximum degree of the reachability graph that describes the network are derived as a function of the communication range, while different degrees of coverage (1coverage and, more in general, k-coverage) for the 3D environment are characterized as a function of the sensing range. Interestingly, it is shown that the sensing range r required for 1-coverage is greater than the transmission range t that guarantees network connectivity. Since in typical applications $t \geq r$, the network is guaranteed to be connected when 1-coverage is achieved. Although these results were derived for terrestrial networks, they can also be applied in the underwater environment. Thus, in this paper, we will focus on the sensing coverage when discussing deployment issues in 3D UW-ASNS, as in three-dimensional networks it implicitly implies the communication coverage.

3. COMMUNICATION ARCHITECTURES

We consider two communication architectures for underwater sensor networks, i.e., a *two-dimensional* and a *three-dimensional* architecture [1], and identify the relevant deployment challenges. As in terrestrial sensor networks, in UW-ASNs it is necessary to provide *communication coverage*, i.e., all sensors should be able to establish multi-hop paths to the sink, and *sensing coverage*, i.e., the monitored area should be covered by the sensors. More formally, the *sensing range* r of a sensor is the radius of the sphere that models the region monitored by the sensor (sensing sphere). A portion A_n of the monitored region A is said to be k-covered if every point

in \mathcal{A}_{η} falls within the sensing sphere of at least k sensors. The k-coverage ratio η_k of a monitored region \mathcal{A} is the fraction of the volume/area that is k-covered by a 3D/2D UW-ASN, respectively. In the following, we will consider the case of k=1 both for 2D and 3D networks to obtain simple l-coverage η_1 of the region, since underwater sensors may be expensive devices and spatio-temporal correlation may not be assumed [1].

3.1 Two-dimensional UW-ASNs

A reference architecture for two-dimensional underwater sensor networks is shown in Fig. 1(a), where deployed sensor nodes are anchored to the bottom of the ocean. Underwater sensors may be organized in a cluster-based architecture, and be interconnected to one or more underwater gateways (uw-gateways) by means of wireless acoustic links. Uw-gateways are network devices in charge of relaying data from the ocean bottom network to a surface station. They are equipped with a long-range *vertical* transceiver, which is used to relay data to a surface station, and with a horizontal transceiver, which is used to communicate with the sensor nodes to send commands and configuration data, and to collect monitored data. The surface station is equipped with an acoustic transceiver, which may be able to handle multiple parallel communications with the uw-gateways, and with a long-range radio transmitter and/or satellite transmitter, which is needed to communicate with an onshore sink and/or to a surface sink.

The main challenges that arise with such two-dimensional architecture are: i) determine the minimum number of sensors and uw-gateways that need to be deployed to achieve the target sensing and communication coverage, which are dictated by the application requirements; ii) provide guidelines on how to choose the optimal deployment surface area, given a target bottom area; iii) study the topology robustness of the sensor network to node failures, and provide an estimate of the number of redundant sensor nodes to be deployed to compensate for failures. In Section 4, we discuss in detail these issues and provide solutions.

3.2 Three-dimensional UW-ASNs

Three-dimensional underwater networks are used to detect and observe phenomena that cannot be adequately observed by means of ocean bottom uw-sensor nodes, i.e., to perform cooperative sampling of the 3D ocean environment. In this architecture, sensors float at different depths to observe a given phenomenon. One possible solution would be to attach each sensor node to a surface buoy, by means of wires whose length can be regulated to adjust the depth of each sensor node. However, although this solution enables easy and quick deployment of the sensor network, multi-

ple floating buoys may obstruct ships navigating on the surface, or they can be easily detected and deactivated by enemies in military settings. Furthermore, floating buoys are vulnerable to weather and tampering or pilfering. A different approach is to anchor winch-based sensor devices to the bottom of the ocean, as depicted in Fig. 1(b). Each sensor is anchored to the ocean bottom and is equipped with a floating buoy that can be inflated by a pump. The buoy pulls the sensor towards the ocean surface. The depth of the sensor can then be regulated by adjusting the length of the wire that connects the sensor to the anchor, by means of an electronically controlled engine that resides on the sensor [1].

Many challenges arise with such architecture, which need to be solved in order to enable underwater monitoring, including: i) sensors should collaboratively regulate their depth in order to achieve 3D sensing coverage of the ocean column, according to their sensing ranges; ii) sensors should be able to relay information to the surface station via multi-hop paths, as in 3D underwater networks there may be no notion of uw-gateway. Thus, network devices should coordinate their depths in such a way as to guarantee that the network topology be always connected, i.e., at least one path from every sensor to the surface station always exists, and achieve communication coverage. We discuss sensing and communication coverage in 3D UW-ASNs in Section 5, and propose three deployment solutions.

4. DEPLOYMENT IN A 2D ENVIRONMENT

In this section, we provide a mathematical analysis of the graph properties of sensor devices that are deployed on the surface of the ocean, sink, and reach the ocean bottom. To achieve this, we study the trajectory of sinking devices (sensors and uw-gateways) when they are deployed on the ocean surface with known initial conditions (position and velocity). This allows us to capture both the case when sensor nodes are *randomly deployed* on the ocean surface, e.g., scattered from an airplane, or the case when sensors are *accurately positioned*, e.g., released from a vessel.

To address the deployment challenges presented in the previous section, in Section 4.1 we propose the *triangular-grid* deployment, and derive useful geometric properties. In Section 4.2, we study the dynamics of a sinking object and evaluate its trajectory under the presence of ocean currents. In Section 4.3, we characterize the different sinking behavior of sensors and uw-gateways, with the objective of describing their average horizontal displacement and study the main communication properties of sensor clusters. In Section 4.4, we derive the side margins that should be used to deploy sensors on the ocean surface when a 2D target area needs to be covered on the ocean bottom under the presence of currents. Finally, in Section 4.5, we derive an estimate of the number of redundant sensors to be deployed to compensate for possible failures and provide the network with robustness.

4.1 Triangular-grid Coverage Properties

In this section, we propose the triangular-grid deployment, and derive useful geometric properties. Let us consider the common case of sensors with same sensing range r. The optimal deployment strategy to cover a two-dimensional rectangular area using the minimum number of sensors is to center each sensor at the vertex of a grid of equilateral triangles, as shown in Fig. 2(a). With this configuration, by adjusting the distance d among sensors, i.e., the side of the equilateral triangles, it is possible to achieve full coverage, i.e., $\eta=1$. In addition, this enables to optimally control the coverage ratio η , defined as the ratio between the covered area and the target area. In particular, as it will be mathematically proven in the following, when $d=\sqrt{3}r$ the coverage ratio η is equal to

1, i.e., the uncovered area ABC depicted in Figs. 2(a-b) is zero, and the overlapping areas are minimized. This allows to achieve the full coverage of a target area, but requires the highest number of sensors. Conversely, as the distance among sensors increases, i.e., the number of deployed sensors decreases, the coverage ratio decreases. Therefore, there is a trade-off between the number of deployed sensors and the achievable sensing coverage. We are interested in finding the minimum number of sensors that need to be deployed in order to guarantee a target sensing coverage η^* , which is dictated by the application requirements. To this end, we present the following theorem.

THEOREM 1. In an equilateral grid the sensing coverage $\eta(d,r)$, i.e., the ratio of the covered area and the target area, is

$$\eta(d,r) = \eta\left(\frac{d}{r}\right) = \begin{cases} \frac{A_{DEF} - A_{ABC}}{A_{DEF}} = 1 - \frac{A_{ABC}}{\frac{\sqrt{3}}{4}d^2} & \frac{d}{r} \in [0,2]\\ \frac{3 \cdot \frac{\pi r^2}{\sqrt{3}}}{\frac{\sqrt{3}}{4}d^2} = \frac{2\pi}{\sqrt{3}} \cdot (\frac{d}{r})^{-2} & \frac{d}{r} \in (2,\infty), \end{cases}$$
(1)

where:

$$\mathcal{A}_{ABC} = \frac{\sqrt{3}}{4} \left(\frac{d}{2} - \sqrt{3r^2 - \frac{3}{4}d^2} \right)^2 - 3r^2 \arcsin \frac{\overline{BC}}{2r}$$

$$+ \frac{3}{4} \overline{BC} \sqrt{4r^2 - \overline{BC}^2}, \qquad \overline{BC} = \frac{d}{2} - \sqrt{3r^2 - \frac{3}{4}d^2}.$$
(2)

PROOF. With reference to Fig. 2(b), which represents a zoomed portion of Fig. 2(a), $\overline{AE} = r$ and $\overline{EH} = d/2$, where r is the sensing range and d is the distance between sensors. Since the triangle DEF is equilateral by construction, $\overline{HO} = (\sqrt{3}/6)d$. Consequently, since $\overline{AH} = \sqrt{r^2 - d^2/4}$, it holds $\overline{AO} = \overline{HO} - \overline{AH} =$ $(\sqrt{3}/6)d - \sqrt{r^2 - d^2/4}$. As triangle *DEF* is equilateral, triangle ABC is equilateral too. Since $\overline{AO} = (\sqrt{3}/3)\overline{BC}$, then $\overline{BC} = d/2 - \sqrt{3r^2 - (3/4)d^2}$. Therefore, the area of triangle ABC is $\mathcal{A}_{ABC}^{\triangle}=(\sqrt{3}/4)\overline{BC}^2$. In order to express the sensing coverage $\eta(d,r)$ as a function of d and r, we need to compute the area A_{ABC} of the uncovered region ABC among the circles with centers in D, E, and F, and radius r. This can be computed as $\mathcal{A}_{ABC} = \mathcal{A}_{ABC}^{\triangle} - 3 \cdot \mathcal{A}_{BTCK}$, where \mathcal{A}_{BTCK} coincides with the difference of the areas of the circular sector BTCFand the triangle BCF, i.e., $A_{BTCK} = A_{BTCF} - A_{BCF}^{\triangle} =$ $r^2 \arcsin(\overline{BC}/2r) - (\overline{BC}/4)\sqrt{4r^2 - \overline{BC}^2}$. Consequently, $\mathcal{A}_{ABC} = (\sqrt{3}/4) \left(d/2 - \sqrt{3r^2 - (3/4)d^2}\right)^2 3r^2 \arcsin(\overline{BC}/2r) + (3/4)\overline{BC}\sqrt{4r^2 - \overline{BC}^2}$, where $\overline{BC} = d/2 \sqrt{3r^2-(3/4)d^2}$, which gives (1) in the non-trivial case $d/r \in$ [0,2]. As far as the case $d/r \in (2,\infty)$ is concerned, no overlapping areas are formed, and the coverage η can be computed straightforward.

COROLLARY 1. In an equilateral grid the sensing coverage depends only on the ratio of the inter-sensor distance d and the sensing range r, and not on their absolute values, i.e., $\eta(d,r) = \eta(d/r)$.

Let us note in (1) that, when $d/r \leq \sqrt{3}$, it holds $\mathcal{A}_{ABC}^{\triangle} = \mathcal{A}_{ABC} = 0$, which means that in this case the highest possible coverage is achieved $(\eta = 1)$. Moreover, $\mathcal{A}_{ABC}(d)$ is a monotonically increasing function when d/r ranges in $[\sqrt{3}, 2]$, which makes the coverage $\eta(d, r)$ a monotonically decreasing function when $d/r > \sqrt{3}$. Figure 2(c) reports the sensing coverage as a decreasing function of the ratio of d and r. For a target sensing coverage $\eta^* = 0.95$, it is shown that the optimal ratio is $d^*/r = 1.95$.

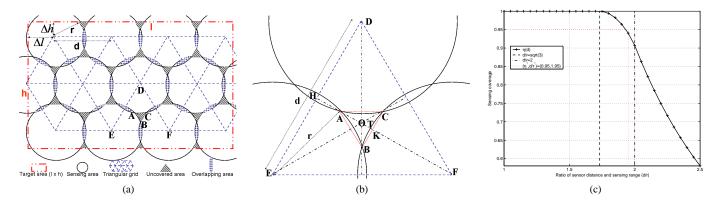


Figure 2: Triangular-grid deployment. (a): Grid structure and side margins; (b): Uncovered area; (c): Sensing coverage

In order to compute the minimum number of sensors that need to be deployed to cover a target area with sides l and h using the proposed equilateral grid, we should first find the optimal $margins\ \Delta l$ and Δh from the center of the upper-left sensing circle, as shown in Fig. 2(a). In particular, given the application-dependent target coverage η^* , from Fig. 2(c) we compute the optimal ratio d^*/r . In order for the uncovered areas on the border of the target area to have the same coverage ratio η^* , the margins should be selected as $\Delta h = \overline{HO} + \overline{OT} = (\sqrt{3}/2)d^* - r$, where $\overline{OT} = \overline{OF} - \overline{TF} = (\sqrt{3}/3)d - r$, and $\Delta l = 2\overline{OH}\cos(\pi/6) = d^*/2$. If we denote as N^* the minimum number of sensors, we have $N^* = N_l^* \cdot N_h^*$, where N_l^* and N_h^* represent the minimum number of sensors deployed along sides l and h, respectively. Consequently, the following relations need to be satisfied,

$$2\Delta l + (N_l^* - 1)d^* \ge l \implies N_l^* = \left\lceil \frac{l - d^*}{d^*} + 1 \right\rceil$$
$$2\Delta h + (N_h^* - 1)d^* \sin(\pi/6) \ge h \implies N_h^* = \left\lceil \frac{2\sqrt{3}h - 6d^* + 4\sqrt{3}r}{3d^*} + 1 \right\rceil$$

Finally, the minimum number of sensors N^* required to cover a target area with sides l and h, under the constraints of providing a ratio d^*/r to satisfy the target coverage ratio η^* is

$$N^*(l, h, d^*, r) = \left\lceil \frac{l - d^*}{d^*} + 1 \right\rceil \cdot \left\lceil \frac{2\sqrt{3}h - 6d^* + 4\sqrt{3}r}{3d^*} + 1 \right\rceil.$$
(3)

In Figs. 3(a-c), (3) is plotted for three different target areas, i.e., $A_1 = 100 \times 100 \text{ m}^2$, $A_2 = 300 \times 200 \text{ m}^2$, and $A_3 = 1000 \times 1000 \text{ m}^2$, and for several sensing ranges r in the interval [10, 35] m.

4.2 Trajectory of a Sinking Object

In this section, we study the dynamics of a sinking object and evaluate its trajectory under the presence of ocean currents. In particular, we first consider the ideal case in which the velocity of the ocean current does not change with depth; then, we extend the model to capture the more realistic case in which the velocity of the current depends on depth.

According to Newton's first law of motion, the acceleration $\vec{\mathbf{a}}$ describing the sinking in the water of an object with a density ρ and volume V is determined by the following vectorial motion law,

$$\vec{\mathbf{F}}_{\mathbf{W}} + \vec{\mathbf{F}}_{\mathbf{B}} + \vec{\mathbf{F}}_{\mathbf{B}} + \vec{\mathbf{F}}_{\mathbf{C}} = \rho V \cdot \vec{\mathbf{a}},\tag{4}$$

where:

• $\vec{\mathbf{F}}_{\mathbf{W}} = \rho V \cdot \vec{\mathbf{g}}$ is the *weight force*, which depends on the density $\rho \left[\mathrm{Kg/m^3}\right]$ and volume $V \left[\mathrm{m^3}\right]$ of the sinking object, and on the terrestrial gravitational acceleration $g = 9.81\,\mathrm{m/s^2}$;

- $\vec{\mathbf{F}}_{\mathbf{B}} = -\rho_w V \cdot \vec{\mathbf{g}}$ is the buoyant force due to the Archimede's principle, which is equal to the weight of the displaced fluid, where $\rho_w = 1050 \, \mathrm{Kg/m^3}$ represents the average density of salty water;
- F
 _R = -Kρ_wμA_R· v

 is the fluid resistance force, which is proportional through the constant K = 0.2 Nm²s/Kg [5] to the velocity v

 [m/s] of the object, to its cross-section A_R [m²], and to a parameter μ accounting for the resistance caused by the object shape;
- $\vec{\mathbf{F}}_{\mathbf{C}} = C\sigma A_C \cdot (\vec{\mathbf{v}}_{\mathbf{c}} \vec{\mathbf{v}})$ is the force of the current, which is proportional through the constant $C = 721.7 \, \mathrm{Ns/m^3}$ [5] to the difference between the velocity of the ocean current $\vec{\mathbf{v}}_{\mathbf{c}} \, [\mathrm{m/s}]$ and the object velocity $\vec{\mathbf{v}} \, [\mathrm{m/s}]$, to the cross-section $A_C \, [\mathrm{m^2}]$ of the object facing the current, and to an object-dependent shape factor σ .

We project (4) onto the x-, y-, and z- axes, which are directed as shown in Fig. 1(c), and we denote the dynamic position of the sinking object as $\mathbf{P}=(x,y,z)$, its velocity as $\vec{\mathbf{v}}=(\dot{x},\dot{y},\dot{z})$, and its acceleration as $\vec{\mathbf{a}}=(\ddot{x},\ddot{y},\ddot{z})$. We then consider the velocity of the current $\vec{\mathbf{v}}_c=(v_c^x,v_c^y,v_c^z)$, which, for the sake of clarity, is first assumed to be independent on the ocean depth (we will then relax this assumption). Under the assumption that no significant vertical movement of ocean water is observed, i.e., the considered area is neither an *upwelling* nor a *downwelling area*, the current along the z-axes can be neglected $(v_c^z\approx 0)$, and (4) leads to three scalar laws,

$$x: F_C^x = \rho V \ddot{x}; \quad y: F_C^y = \rho V \ddot{y}; \quad z: F_W^z + F_B^z + F_R^z = \rho V \ddot{z}.$$

Specifically, we obtain the following dynamic system equations,

$$\begin{cases}
\ddot{x} + \frac{C\sigma A^{xy}}{\rho V} \dot{x} = \frac{C\sigma A^{xy}}{\rho V} v_c^x \\
\ddot{y} + \frac{C\sigma A^{xy}}{\rho V} \dot{y} = \frac{C\sigma A^{xy}}{\rho V} v_c^y \\
\ddot{z} + \frac{K\mu\rho_V A^z}{\rho V} \dot{z} = g^{\frac{\rho}{\rho}\rho_W},
\end{cases} (6)$$

where A^{xy} and A^z represent the horizontal and vertical cross-sections, respectively. By solving this dynamic system, with the initial conditions of the object on the surface at time t^0 , i.e., its position $\mathbf{P}(t^0) = (x(t^0), y(t^0), 0)$ and velocity $\vec{\mathbf{v}}(t^0) = (\dot{x}(t^0), \dot{y}(t^0), \dot{z}(t^0))$, we obtain the solution,

$$\begin{cases} x(t) = x(t^{0}) + v_{c}^{x} \cdot (t - t^{0}) + \frac{\dot{x}(t^{0}) - v_{c}^{x}}{C\sigma A^{xy}/\rho V} \cdot [1 - e^{-\frac{C\sigma A^{xy}}{\rho V} \cdot (t - t^{0})}] \\ y(t) = y(t^{0}) + v_{c}^{y} \cdot (t - t^{0}) + \frac{\dot{y}(t^{0}) - v_{c}^{y}}{C\sigma A^{xy}/\rho V} \cdot [1 - e^{-\frac{C\sigma A^{xy}}{\rho V} \cdot (t - t^{0})}] \\ z(t) = v_{\infty}^{z} \cdot (t - t^{0}) + [\dot{z}(t^{0}) - v_{\infty}^{z}] \cdot [1 - e^{-\frac{K\rho_{w}\mu A^{z}}{\rho V} \cdot (t - t^{0})}], \end{cases}$$

$$(7)$$

where we denoted as $v_{\infty}^z = \frac{gV(\rho - \rho_w)}{K\rho_w\mu A^z}$ [m/s] the terminal velocity along z, which is computed by imposing in (5) the following force equilibrium, $F_W^z + F_B^z + F_R^z = 0$, i.e., $\ddot{z} = 0$ in (6).

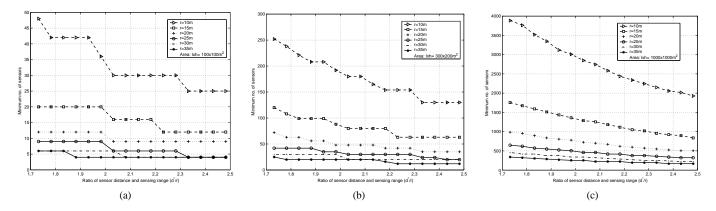


Figure 3: Minimum no. of sensors in triangular-grid deployment vs. sensor distance over sensing range. (a): $A_1 = 100 \times 100 \text{ m}^2$; (b): $A_2 = 300 \times 200 \text{ m}^2$; (c): $A_3 = 1000 \times 1000 \text{ m}^2$

Let us now generalize this result by considering the more realistic case in which the velocity of the ocean current depends on depth, i.e., $\vec{\mathbf{v}}_{\mathbf{c}} = (v_c^x(z), v_c^y(z), 0)$. There are two types of marine currents each caused by a range of distinct drivers, non tidal ocean currents, such as the Gulf Stream, and tidal streams. The complex hydrodynamic system of currents is powered by many forces, the crux being the playoff between the joint forces of solar heating of tropical surface waters and the polar contributions of cold fresh water ice-melt flooding into the ocean and the general cooling of the salty ocean water. While studying the global current systems makes up the larger part of the science of oceanography, in this paper we focus on the effect of *local streams* in the monitored volume region. In particular, we consider an ocean volume with constant depth z^H (flat bottom), and H different ocean current layers h = 1, ..., H, of width Δz^h . We model the current on each plane xy in a layer h to be a piecewise constant function with module v_c^h and angular deviation from the x-axes α_c^h , as depicted in Fig. 1(c). This allows us to model the thermohaline circulation (also known as the ocean's conveyor belt), i.e., deep ocean current, sometimes called submarine rivers, that flows with constant velocity and direction within certain depths, driven by density and temperature gradients.

Given these assumptions, our objective is to calculate the horizontal displacement of a sinking object on the x- and y-axes in each of the layers it sinks through. To accomplish this, we recursively apply the solution (7) to the dynamic system (6) to each layer, using as initial conditions of the object the final position and velocity computed in the previous layer. If we denote the initial position of object n as $(x_n^0, y_n^0, 0)$ and its velocity as $(\dot{x}_n^0, \dot{y}_n^0, \dot{z}_n^0)$, given all its physical characteristics such as volume V_n , density ρ_n , cross-sections A_n^{xy} and A_n^z , and horizontal and vertical shape factors, μ_n and σ_n , respectively, we can track the position of n while it sinks. Specifically, we have

$$\begin{cases} x_{n}(t) = x_{n}^{0} + \sum_{i=1}^{h-1} \Delta x_{n}^{i} + v_{c}^{h} \cos \alpha_{c}^{h} \cdot (t - t_{n}^{h-1}) + \\ + \frac{\dot{x}_{n}(t_{n}^{h-1}) - v_{c}^{h} \cos \alpha_{c}^{h}}{C\sigma_{n}A_{n}^{xy}/\rho_{n}V_{n}} \cdot [1 - e^{-\frac{C\sigma_{n}A_{n}^{xy}}{\rho_{n}V_{n}} \cdot (t - t_{n}^{h-1})}] \\ y_{n}(t) = y_{n}^{0} + \sum_{i=1}^{h-1} \Delta y_{n}^{i} + v_{c}^{h} \sin \alpha_{c}^{h} \cdot (t - t_{n}^{h-1}) + \\ + \frac{\dot{y}_{n}(t_{n}^{h-1}) - v_{c}^{h} \sin \alpha_{c}^{h}}{C\sigma_{n}A_{n}^{xy}/\rho_{n}V_{n}} \cdot [1 - e^{-\frac{C\sigma_{n}A_{n}^{xy}}{\rho_{n}V_{n}} \cdot (t - t_{n}^{h-1})}] \\ t_{n}^{h-1} \leq t \leq t_{n}^{h} \\ z_{n}(t) = \min\{v_{\infty n}^{z} \cdot (t - t_{n}^{0}) + \\ + [\dot{z}_{n}^{0} - v_{\infty n}^{z}] \cdot [1 - e^{-\frac{K\rho_{\nu}\mu_{n}A_{n}^{z}}{\rho_{n}V_{n}} \cdot (t - t_{n}^{0})}]; z^{H}\}, \end{cases}$$

where t_n^0 and t_n^h are the instants object n is released on the ocean

surface and exits layer h, respectively. More precisely, t_n^h is the instant for which it holds $z_n(t_n^h) = z^h = \sum_{i=1}^h \Delta z^i$, i.e., the depth of the object coincides with the sum of the width Δz^i of each layer i the object sank through, as shown in Fig. 1(c).

In (8), the total displacement on the x- and y-axes when the sinking object is inside layer h is *recursively* computed as the sum of the displacements in each of the h-1 previously crossed layers i=1,...,h-1, plus the displacement in layer h itself. These displacements are determined as partial solution of the dynamic system (6) in each layer, and have the following structure,

$$\begin{cases}
\Delta x_n^i = v_c^i \cos \alpha_c^i \cdot (t_n^i - t_n^{i-1}) + \\
+ \frac{\dot{x}_n(t_n^{t-1}) - v_c^i \cos \alpha_c^h}{C\sigma_n A_n^{xy}/\rho_n V_n} \cdot [1 - e^{-\frac{C\sigma_n A_n^{xy}}{\rho_n V_n} \cdot (t_n^i - t_n^{i-1})}] \\
\Delta y_n^i = v_c^i \sin \alpha_c^i \cdot (t_n^i - t_n^{i-1}) + \\
+ \frac{\dot{y}_n(t_n^{t-1}) - v_c^h \sin \alpha_c^h}{C\sigma_n A_n^{xy}/\rho_n V_n} \cdot [1 - e^{-\frac{C\sigma_n A_n^{xy}}{\rho_n V_n} \cdot (t_n^i - t_n^{i-1})}].
\end{cases} (9)$$

Finally, in order to be able to determine the position of object n from (8), we need to substitute in (8) and (9) the x- and y-component of the velocity the object has when it enters layer h=1,...,H, i.e., $(\dot{x}_n(t_n^{h-1}),\dot{y}_n(t_n^{h-1}))$, which can be computed as exit velocity from layer h-1 by solving (6). We report these velocities in the following,

$$\begin{cases} \dot{x}_{n}(t_{n}^{h-1}) = v_{c}^{h-1}\cos\alpha_{c}^{h-1} + \\ +[\dot{x}_{n}(t_{n}^{h-2}) - v_{c}^{h-1}\cos\alpha_{c}^{h-1}] \cdot e^{-\frac{C\sigma_{n}A_{n}^{xy}}{\rho_{n}V_{n}} \cdot (t_{n}^{h-1} - t_{n}^{h-2})} \\ \dot{y}_{n}(t_{n}^{h-1}) = v_{c}^{h-1}\sin\alpha_{c}^{h-1} + \\ +[\dot{y}_{n}(t_{n}^{h-2}) - v_{c}^{h-1}\sin\alpha_{c}^{h-1}] \cdot e^{-\frac{C\sigma_{n}A_{n}^{xy}}{\rho_{n}V_{n}} \cdot (t_{n}^{h-1} - t_{n}^{h-2})}, \end{cases}$$

$$(10)$$

which can be recursively computed given that $\dot{x}_n(t_n^0)$ and $\dot{y}_n(t_n^0)$ are the known initial velocities on the surface.

Equations (8), (9), and (10) allow us to track the dynamic position of object n while it sinks, given complete knowledge about the structure of the currents in the volume of interest. In practice, however, we may only leverage some statistical information on the currents, which can be used to estimate the final position of a deployed object. While this offers a mathematical tool to study the dynamic of a sinking object, our ultimate objective is to be able to infer the statistical sensing and communication properties of a two-dimensional sensor network that reaches the ocean bottom, as will be discussed in the following section.

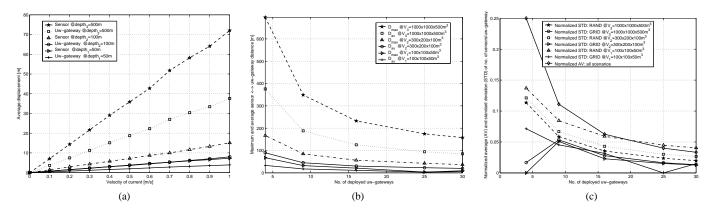


Figure 4: (a): Average horizontal displacement of sensors and uw-gateways vs. current velocity (for three different depths); (b): Maximum and average sensor-gateway distance vs. no. of deployed gateways (in three different volumes, and with $v_c^{max}=1\,\mathrm{m/s}$); (c): Normalized average and standard deviation of no. of sensors per uw-gateway vs. no. of deployed gateways (for grid and random deployment strategies, in three different volumes, and with $v_c^{max}=1\,\mathrm{m/s}$)

4.3 Communication Properties of 2D UW-ASNs

In this section, we characterize the different sinking behavior of sensors and uw-gateways, with the objective of describing: i) the average horizontal displacement of sensors and uw-gateways when different depths and current velocities are considered; ii) the main properties of the clusters that have an uw-gateway as cluster head, e.g., study the maximum and average sensor-gateway distance when the number of deployed gateways varies; iii) the average and standard deviation of number of sensors in each cluster.

Let us consider a set of sensors \mathcal{S} with cardinality $S = |\mathcal{S}|$ characterized by the same density $\rho_{\mathcal{S}}$, volume $V_{\mathcal{S}}$, cross-sections $A_{\mathcal{S}}^{xy}$ and $A_{\mathcal{S}}^z$, and shape factors $\mu_{\mathcal{S}}$ and $\sigma_{\mathcal{S}}$, and a set of uw-gateways \mathcal{G} with $G = |\mathcal{G}|$, in general with different values of $\rho_{\mathcal{G}}$, $V_{\mathcal{G}}$, $A_{\mathcal{G}}^{xy}$, $A_{\mathcal{G}}^z$, $\mu_{\mathcal{G}}$, and $\sigma_{\mathcal{G}}$. Given the matrices of the known initial positions of the deployed sensors and uw-gateways, $\mathbf{P}_{\mathbf{S}}^0 = [\mathbf{P}_{\mathbf{1}}^0|\cdots|\mathbf{P}_{\mathbf{S}}^0|\cdots|\mathbf{P}_{\mathbf{S}}^0]^T$ and $\mathbf{P}_{\mathbf{G}}^0 = [\mathbf{P}_{\mathbf{1}}^0|\cdots|\mathbf{P}_{\mathbf{S}}^0]^T$, respectively, where $\mathbf{P}_{\mathbf{S}}^0 = [x_s^0 \ y_s^0 \ 0]^T \ \forall s \in \mathcal{S}$ and $\mathbf{P}_{\mathbf{g}}^0 = [x_g^0 \ y_g^0 \ 0]^T \ \forall g \in \mathcal{G}$ are position column vectors, and the matrices of their known initial velocities, $\mathbf{v}_{\mathbf{S}}^0 = [\mathbf{v}_{\mathbf{1}}^0|\cdots|\mathbf{v}_{\mathbf{S}}^0]^T \ \text{vol} = [\mathbf{v}_{\mathbf{I}}^0|\cdots|\mathbf{v}_{\mathbf{G}}^0]^T$, where $\mathbf{v}_{\mathbf{S}}^0 = [\dot{x}_s^0 \ \dot{y}_s^0 \ \dot{z}_s^0]^T \ \forall s \in \mathcal{S}$ and $\mathbf{v}_{\mathbf{g}}^0 = [\dot{x}_s^0 \ \dot{y}_g^0 \ \dot{z}_g^0]^T \ \forall g \in \mathcal{G}$ are velocity column vectors, the final positions on the ocean bottom of the sensors and uw-gateways, $\mathbf{P}_{\mathbf{S}}^f$ and $\mathbf{P}_{\mathbf{G}}^f$, respectively, can be derived using (8), (9), and (10) when all deployed devices have reached the bottom, i.e., when $t = t^f \geq \max_{\mathbf{S} \in \mathcal{S}} t_s^H$; $\max_{g \in \mathcal{G}} t_g^H$ }. Specifically,

$$\underline{P_{\mathcal{S}}^{\mathbf{f}}} = \underline{P_{\mathcal{S}}^{\mathbf{0}}} + \underline{\Delta P_{\mathcal{S}}}(\underline{\mathbf{v}_{\mathcal{S}}^{\mathbf{0}}}), \quad \underline{P_{\mathcal{G}}^{\mathbf{f}}} = \underline{P_{\mathcal{G}}^{\mathbf{0}}} + \underline{\Delta P_{\mathcal{G}}}(\underline{\mathbf{v}_{\mathcal{G}}^{\mathbf{0}}}) \tag{11}$$

where $\Delta P_{\mathcal{S}}(\mathbf{v}_{\mathcal{S}}^{\mathbf{0}})$ and $\Delta P_{\mathcal{G}}(\mathbf{v}_{\mathcal{G}}^{\mathbf{0}})$ are matrices accounting for the total displacements accumulated while the sensors and uw-gateways, respectively, were sinking through the ocean current layers, i.e.,

$$\underline{\boldsymbol{\Delta}}\underline{\mathbf{P}}_{\underline{\mathcal{S}}} = \begin{bmatrix} \cdot & \sum_{h=1}^{H} \Delta x_{s}^{h} & \cdot \\ \cdot & \sum_{h=1}^{H} \Delta y_{s}^{h} & \cdot \\ \cdot & z^{H} & \cdot \end{bmatrix}^{T}, \underline{\boldsymbol{\Delta}}\underline{\mathbf{P}}_{\underline{\mathcal{G}}} = \begin{bmatrix} \cdot & \sum_{h=1}^{H} \Delta x_{g}^{h} & \cdot \\ \cdot & \sum_{h=1}^{H} \Delta y_{g}^{h} & \cdot \\ \cdot & z^{H} & \cdot \end{bmatrix}$$
(12)

In (12), each element can be computed as in (9). Note that the dependence on the initial velocity in (12) has been omitted for the sake of notation simplicity.

In Fig. 4(a), we show the expected horizontal displacement $\Delta d=\sqrt{\Delta x^2+\Delta y^2}$ of sensors and uw-gateways when different depths

and current velocities are considered. In particular, we consider $\rho_s=2000\,{\rm kg/m^3},~\rho_g=2500\,{\rm kg/m^3},~V_s=0.5\cdot 10^{-3}\,{\rm m^3},$ and $V_g=10^{-3}\,{\rm m^3}$ to account for the common physical characteristics of underwater sensor nodes and uw-gateways, which reflect into different sinking properties, as formalized in (11). Note that gateways accumulate smaller displacements than sensors since their sinking times are shorter. In Fig. 4(b), we depict the maximum and average sensor-gateway distance when the number of deployed gateways increases. In particular, we consider three deployment volumes ($V_1 = 100 \times 100 \times 50 \text{ m}^3$, $V_2 = 300 \times 200 \times 100 \text{ m}^3$ and $V_3 = 1000 \times 1000 \times 500 \text{ m}^3$) and a one-layer current scenario (H=1) with $v_c^{max}=1\,\mathrm{m/s}$. According to the specific sensor transmission range t, Fig. 4(b) allows setting the minimum number of uw-gateways that need to be deployed. In Fig. 4(c), we present the normalized average and standard deviation of number of sensors per uw-gateway when two deployment strategies are considered, the random and the grid deployment. Interestingly, while the average number of sensors does not depend on the deployment strategy, the sensor dispersion is much lower in a grid structure, independently on the number of gateways deployed. This is a general result that does not depend on the considered scenario.

4.4 Deployment Surface Area: Side Margins

In this section, we compute the deployment surface area where sensors should be deployed, when a 2D target area needs to be covered on the bottom of the ocean. As described in Sections 4.2 and 4.3, ocean currents may significantly modify the sinking trajectories of sensors and uw-gateways. Therefore, the surface deployment should take into account the effect of the currents, in order to position as many deployed sensors inside the target area as possible. To achieve this, in the following we consider a worst-case scenario where the effect of currents, in terms of sensor displacements, is captured. The objective is to dimension the deployment surface area, i.e., to asses proper surface side margins.

. With reference to Fig. 5, we consider a bottom target area with sides l and h, and analyze the two cases of unknown current direction (a), where we denote as $\Delta d_{max} = \sqrt{\Delta x_{max}^2 + \Delta y_{max}^2}$ the maximum horizontal displacement a sinking sensor can experience, i.e., how far in the horizontal plane xy a sensor can drift (see Fig. 1(c)), and known current direction (b), where we denote as Δd_{max} the same metric used in the previous case and as $\Delta \alpha_{max}$ the maximum angular deviation of the current from its known direction β ,

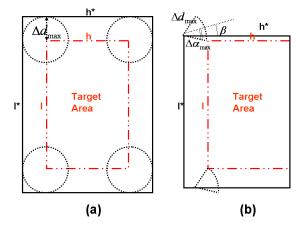


Figure 5: Deployment surface area for unknown (a) and known (b) current direction β , given a bottom target area lxh

which is the angle the direction of the current forms with side h of the target area, as depicted in Fig. 5(b). Note that, without loss in generality, it always holds that $\beta \in [0, \pi/2)$. More specifically, the dotted *circular sector* in Fig. 5(b), characterized by radius Δd_{max} and angle $2\Delta\alpha_{max}$, represents the region of the ocean bottom that may be reached by a sensor that is deployed on the ocean surface exactly on the vertex of the circular sector itself. This region represents the statistical uncertainty in the final anchor position of a sensor caused by drifting due to ocean currents during the sinking.

As far as the side margins in the unknown current direction case are concerned, from geometric properties of Fig. 5(a) it holds,

$$\begin{cases} l^* = l + 2\Delta d_{max} \\ h^* = h + 2\Delta d_{max}, \end{cases}$$
 (13)

while for the known current direction case (Fig. 5(b)) it holds,

$$\begin{cases} l^* = l + \Delta d_{max} \cdot \{ \max \left[0; \sin(\beta - \Delta \alpha_{max}) \right] + \sin(\beta + \Delta \alpha_{max}) \} \\ h^* = h + \Delta d_{max} \cdot \{ \max \left[\cos(\beta - \Delta \alpha_{max}) ; \cos(\beta + \Delta \alpha_{max}) \right] \}. \end{cases} \end{cases}$$
(14)

In (13) and (14), the worst-case maximum displacement and maximum angular deviation a sensor can experience are,

$$\Delta d_{max} = \frac{z^H}{H \cdot v_{\infty}^z} \cdot \sum_{h=1}^H v_c^{h,max}$$
 (15)

$$\Delta \alpha_{max} = \arctan \frac{\sum_{h=1}^{H} v_c^{h,max} \cdot \sin \alpha_c^{h,max}}{\sum_{h=1}^{H} v_c^{h,max} \cdot \cos \alpha_c^{h,max}}, \quad (16)$$

where z^H is the ocean depth, H is the number of ocean current layers, v_∞^z is the terminal velocity (see Section 4.2), and $v_c^{h,max}$ and $\alpha_c^{h,max}$ are the maximum current velocity and angular deviation in layer h, respectively. The mathematical derivation of (14), (15), and (16) is omitted for lack of space. Interestingly, given the same target area, the side surface margins in the unknown current direction case (13) are larger than those computed if some information about the current direction can be leveraged (14). This is also shown in Fig. 5, where the surface areas (outside solid rectangles) in the two cases are noticeably different, while the target area (inside dotted rectangle) is the same.

4.5 Reliability Margin

In this section, we provide an estimate of the number of redundant sensors required to endow the network with robustness to node

Table 1: Redundant sensors ΔN^* to compensate for failures

	Obs. Time T [days]	30	60	90	120	150	180
ĺ	$\Gamma_1^* = 0.90$	2	4	5	7	8	9
ĺ	$\Gamma_2^* = 0.95$	3	5	6	7	9	10
I	$\Gamma_3^* = 0.99$	4	6	8	9	11	12

failures, which in the underwater may be caused by fouling and corrosion. In particular, we study the required topology redundancy to statistically compensate for node failures within a predetermined observation period, i.e., the length of the monitoring mission. If we assume node failures to be independent and occurring according to a Poisson distribution, the minimum number of redundant sensors ΔN^{\ast} to be deployed to compensate for Poissonian failures is,

$$\sum_{n=0}^{\Delta N^*} \frac{(\lambda T)^n \cdot e^{-\lambda T}}{n!} \ge \Gamma^*,\tag{17}$$

where $\lambda \, [{\rm day}^{-1}]$ represents the sensor failure rate, $T \, [{\rm day}]$ the observation time, n the number of sensors that experience a failure within the observation time, and Γ^* the target success probability, i.e., the probability that no more than ΔN^* failures be experienced during the observation time. Table 1 reports the number of redundant sensors that need to be deployed to compensate for Poisson sensor failures occurring during several observation times under three different success probabilities, when $\lambda = 1/(365/12)\,{\rm day}^{-1}$, i.e., in average a sensor experiences one failure every month.

5. DEPLOYMENT IN A 3D ENVIRONMENT

In this section, we propose three deployment strategies for threedimensional UW-ASNs to obtain a target 1-coverage $\eta_1^* = \eta^*$ of the 3D region, i.e., the 3D-random, the bottom-random, and the bottom-grid strategies. As previously discussed, it is shown in [4] that the sensing range r required for 1-coverage is greater than the transmission range t that guarantees network connectivity. Since in typical applications t > r, the network is guaranteed to be connected when 1-coverage is guaranteed. Thus, in the following we focus on the sensing coverage. In all these deployment strategies, winch-based sensor devices are anchored to the bottom of the ocean in such a way that they cannot drift with currents. Sensor devices are equipped with a floating buoy that can be inflated by a pump by means of an electronically controlled engine that resides on the sensor. This way, they can adjust their depth and float at different depths in order to observe a given phenomenon, as described in Section 3.2. In all the proposed deployment strategies, described hereafter, sensors are assumed to know their final positions by exploiting localization techniques.

3D-random. This is the simplest deployment strategy, and does not require any form of coordination from the surface station. Sensors are randomly deployed on the bottom of the 3D volume, where they are anchored. Then, each sensor randomly chooses its depth, and, by adjusting the length of the wire that connects it to the anchor, it floats to the selected depth. Finally, each sensor informs the surface station about its final position.

Bottom-random. As in the previous strategy, sensors are randomly deployed on the bottom, where they are anchored. Differently from the 3D-random scheme, the surface station is informed about their position on the bottom. Then, the surface station calculates the depth for each sensor in order to achieve the target 1-coverage ratio η^* . Finally, each sensor is assigned its target depth and floats to the desired position.

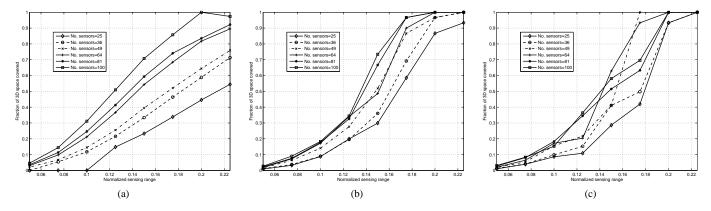


Figure 6: Three-dimensional scenario. (a): 3D coverage with a 3D random deployment; (b): Optimized 3D coverage with a 2D bottom-random deployment; (c): Optimized 3D coverage with a 2D bottom-grid deployment

Bottom-grid. This deployment strategy needs to be assisted by one or multiple AUVs, which deploy the underwater sensors to predefined target locations to obtain a grid deployment on the bottom of the ocean. Each sensor is also assigned a desired depth by the AUV and accordingly floats to achieve the target coverage ratio η^* .

As shown in Figs. 6(a-c), given a fixed number of sensors we achieve a better coverage ratio with increasing complexity of the deployment strategy. In fact, the coverage ratio obtained with the bottom-grid strategy is greater than the coverage ratio obtained with the bottom-random strategy, which is in turn greater than the coverage ratio of the 3D-random strategy. Moreover, given a target coverage ratio, the minimum number of sensors needed to achieve the desired coverage ratio decreases with the complexity of the deployment strategy. Figure 7 shows a comparison between the minimum normalized sensing range that guarantees coverage ratios of 1 and 0.9 with the bottom-random strategy and the theoretical bound on the minimum normalized sensing range derived in [4], where the authors investigate sensing and communication coverage in a 3D environment. According to Theorem 4 in [4], the 3D volume is guaranteed to be asymptotically almost surely 1-covered iff $\frac{4}{3}\pi \frac{n}{V}r^3 = \ln n + \ln \ln n + \omega(n)$, with $1 << \omega(n) << \ln \ln n$, where V is the volume of the region to be covered, n the number of deployed sensors, and r their sensing range. Hence, to draw Fig. 7 we set $\omega(n) = \frac{1 + \ln \ln n}{2}$. This shows that the bottom-random deployment strategy very closely approximates the theoretically predicted bound, i.e., the minimum sensing range that guarantees 1coverage with probability 1 is almost the same as that predicted by the model in [4].

6. CONCLUSIONS

In this paper, deployment strategies for two-dimensional and threedimensional architectures for underwater sensor networks were proposed, and deployment analysis was provided. The objectives were to determine the minimum number of sensors to be deployed to achieve the application-dependent target sensing and communication coverage; provide guidelines on how to choose the deployment surface area, given a target region; study the robustness of the sensor network to node failures, and provide an estimate of the number of required redundant sensors.

Acknowledgments

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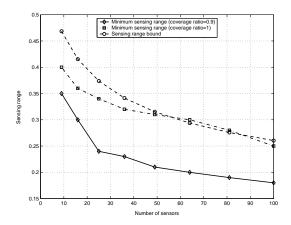


Figure 7: Theoretical and experimental sensing range

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